

**Curs 10**

2023/2024

# Dispozitive și circuite de microunde pentru radiocomunicații

# Disciplina 2023/2024

- 2C/1L (+1), **DCMR (CDM)**
- Minim 7 prezente (curs+laborator)
- Curs - **conf. Radu Damian**
  - Miercuri 08(:**15**)-17, ~~Online~~/**Video (istoric)**, P5
  - E – **50%** din nota
  - probleme + (2p prez. curs) + (3 teste) + (bonus activitate)
    - primul test L1: 04.10.2023 (t2 si t3 neanuntate la **curs**)
    - 3pz (C)  $\approx$  +0.5p (**2p** max)
  - toate materialele permise

# Disciplina 2023/2024

- 2C/1L, **DCMR (CDM)**
- Laborator – **conf. Radu Damian**
  - Miercuri/Joi/Vineri, par/impar, **II.13**
  - L – **25%** din nota
    - ADS, 4 sedinte aplicatii
    - prezenta + **rezultate personale!**
  - P – **25%** din nota
    - ADS, 3 sedinte aplicatii (-1? 21-22.12.2022)
    - tema personala

# Cuprins

- Linii de transmisie
- Adaptarea de impedanță
- Cuploare direcționale
- Divizoare de putere
- Amplificatoare de microunde
- Filtre de microunde
- Oscilatoare de microunde ?



# Bibliografie

- <http://rf-opto.etti.tuiasi.ro>
- Irinel Casian-Botez: "Microunde vol. 1: Proiectarea de circuit", Ed. TEHNOPRES, 2008
- **David Pozar, Microwave Engineering, Wiley; 4th edition , 2011, ISBN : 978-1-118-29813-8 (E), ISBN : 978-0-470-63155-3 (P)**

# Examen: Reprezentare logaritmică

$$\text{dB} = 10 \cdot \log_{10} (P_2 / P_1)$$

$$0 \text{ dB} = 1$$

$$+ 0.1 \text{ dB} = 1.023 (+2.3\%)$$

$$+ 3 \text{ dB} = 2$$

$$+ 5 \text{ dB} = 3$$

$$+ 10 \text{ dB} = 10$$

$$-3 \text{ dB} = 0.5$$

$$-10 \text{ dB} = 0.1$$

$$-20 \text{ dB} = 0.01$$

$$-30 \text{ dB} = 0.001$$

$$\text{dBm} = 10 \cdot \log_{10} (P / 1 \text{ mW})$$

$$0 \text{ dBm} = 1 \text{ mW}$$

$$3 \text{ dBm} = 2 \text{ mW}$$

$$5 \text{ dBm} = 3 \text{ mW}$$

$$10 \text{ dBm} = 10 \text{ mW}$$

$$20 \text{ dBm} = 100 \text{ mW}$$

$$-3 \text{ dBm} = 0.5 \text{ mW}$$

$$-10 \text{ dBm} = 100 \mu\text{W}$$

$$-30 \text{ dBm} = 1 \mu\text{W}$$

$$-60 \text{ dBm} = 1 \text{ nW}$$

$$[\text{dBm}] + [\text{dB}] = [\text{dBm}]$$

$$[\text{dBm/Hz}] + [\text{dB}] = [\text{dBm/Hz}]$$

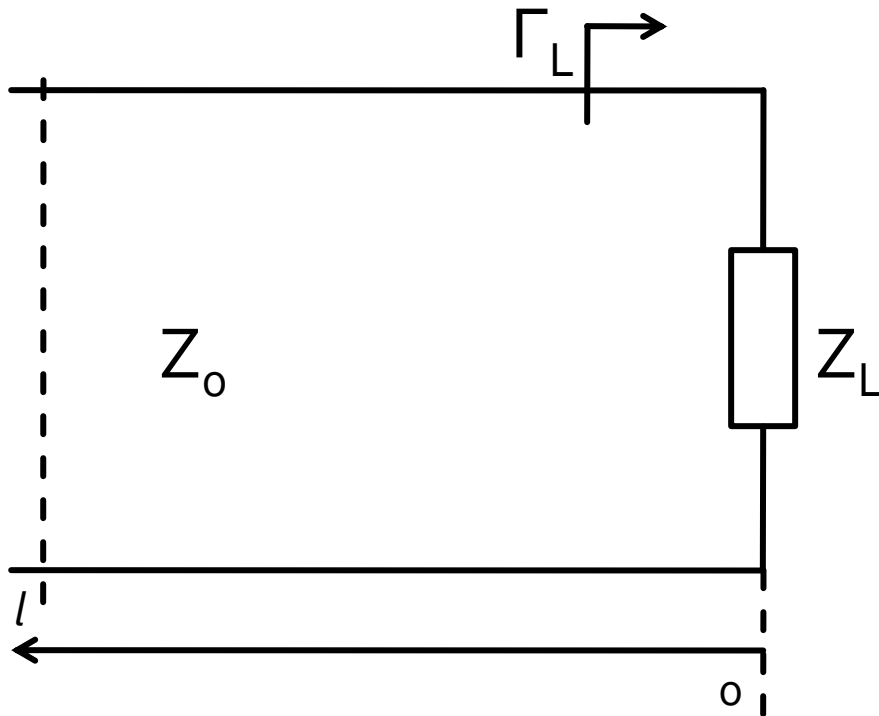
$$[x] + [\text{dB}] = [x]$$

# Linii de transmisie in mod TEM

# Cuprins

- **Linii de transmisie**
- **Adaptarea de impedanță**
- **Cuploare direcționale**
- **Divizoare de putere**
- **Amplificatoare de microunde**
- **Filtre de microunde**
- **Oscilatoare de microunde ?**

# Linie fara pierderi



$$V(z) = V_0^+ e^{-j\beta \cdot z} + V_0^- e^{j\beta \cdot z}$$

$$I(z) = \frac{V_0^+}{Z_0} e^{-j\beta \cdot z} - \frac{V_0^-}{Z_0} e^{j\beta \cdot z}$$

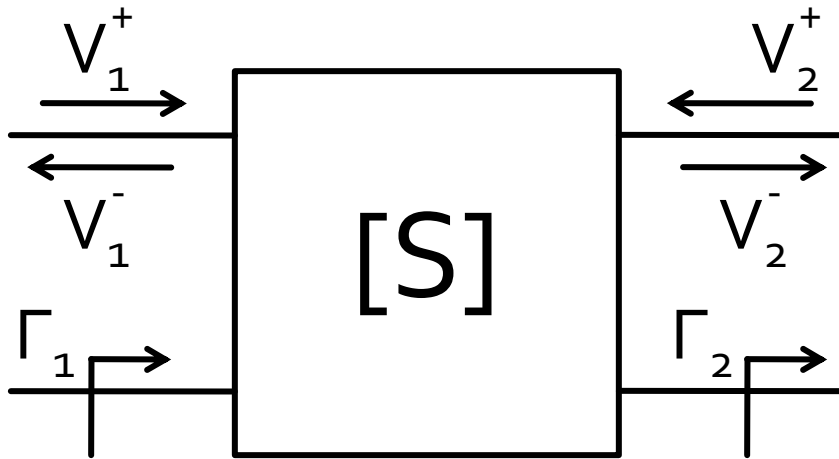
$$Z_L = \frac{V(0)}{I(0)} \quad Z_L = \frac{V_0^+ + V_0^-}{V_0^+ - V_0^-} \cdot Z_0$$

- coeficient de reflexie in tensiune

$$\Gamma = \frac{V_0^-}{V_0^+} = \frac{Z_L - Z_0}{Z_L + Z_0}$$

- $Z_0$  real

# Matricea S (repartitie)



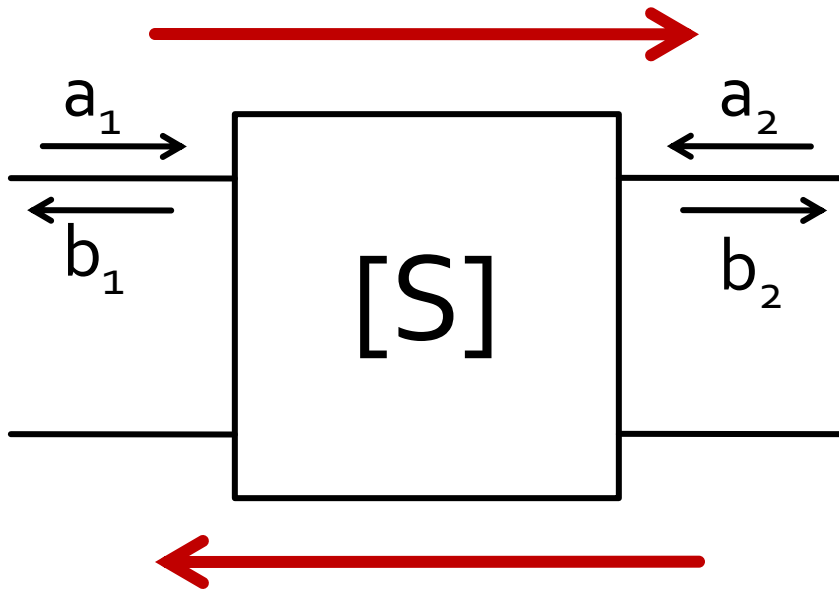
$$\begin{bmatrix} V_1^- \\ V_2^- \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} V_1^+ \\ V_2^+ \end{bmatrix}$$

$$S_{11} = \left. \frac{V_1^-}{V_1^+} \right|_{V_2^+=0} = \Gamma_1|_{\Gamma_2=0}$$

$$S_{21} = \left. \frac{V_2^-}{V_1^+} \right|_{V_2^+=0} = T_{21}|_{\Gamma_2=0}$$

- $S_{11}$  este coeficientul de reflexie la portul **1** cand cand portul **2** este terminat pe impedanta care realizeaza adaptarea
- $S_{21}$  este coeficientul de transmisie de la portul **1** (**al doilea** indice!) la portul **2** (**primul** indice!) cand se depune semnal la portul **1** si portul **2** este terminat pe impedanta care realizeaza adaptarea

# Matricea S (repartitie)



$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$|S_{21}|^2 = \frac{\text{Putere sarcina } Z_0}{\text{Putere sursa } Z_0}$$

- $a, b$ 
  - informatia despre putere **SI** faza
- $S_{ij}$ 
  - influenta circuitului asupra puterii semnalului incluzand informatiile relativ la faza

# Cuprins

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# Adaptare dpdv al puterii

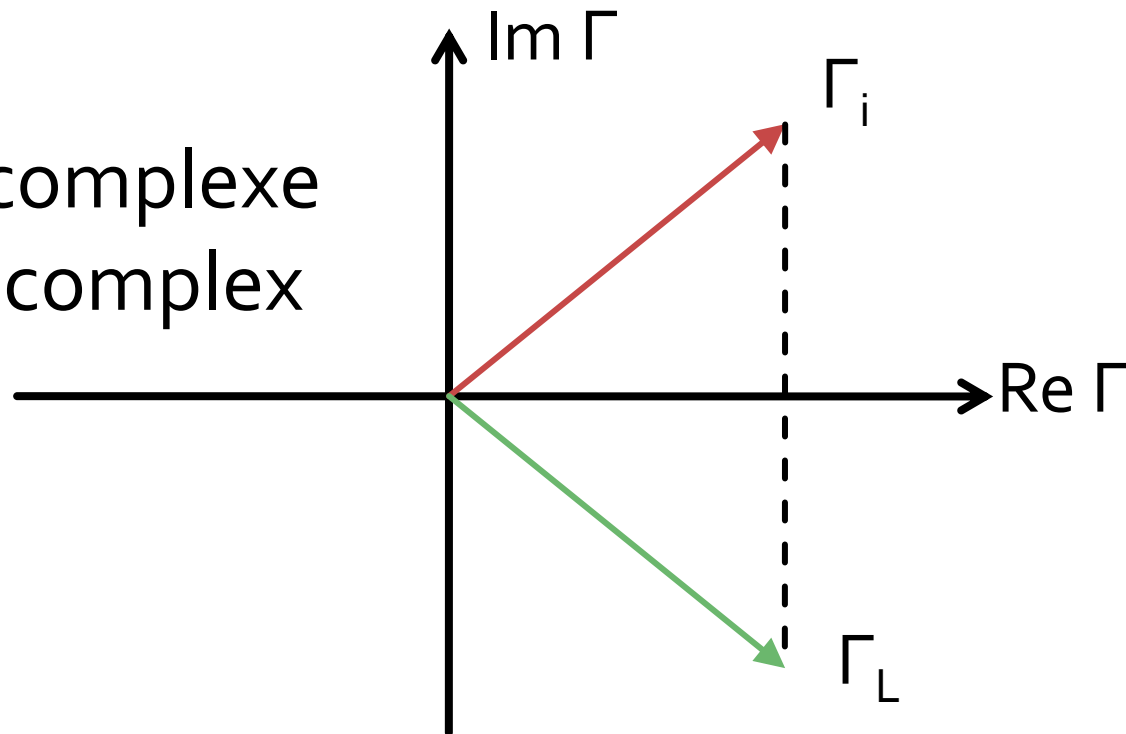
Daca se alege un  $Z_0$  real

$$Z_L = Z_i^*$$

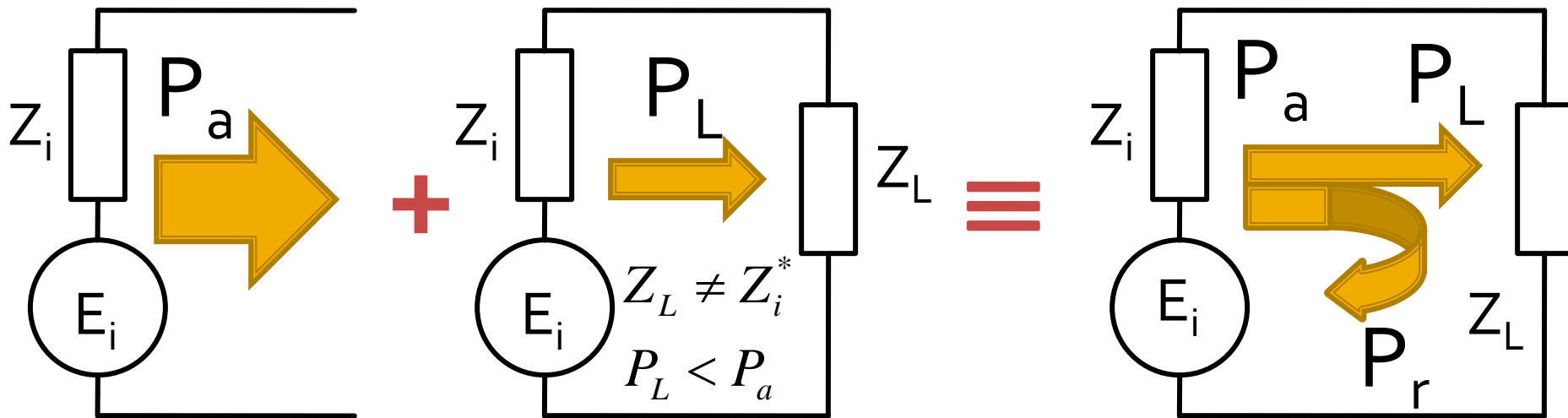
$$\Gamma = \frac{Z - Z_0}{Z + Z_0}$$

$$\Gamma_L = \Gamma_i^*$$

- numere complexe
- in planul complex



# Reflexie de putere / Model



- Generatorul are posibilitatea de a oferi o anumita putere maxima de semnal  $P_a$
- Pentru o sarcina oarecare, acestuia i se ofera o putere de semnal mai mica  $P_L < P_a$
- Se intampla **"ca si cum"** (model) o parte din putere se reflecta  $P_r = P_a - P_L$
- Puterea este o marime **scalara!**

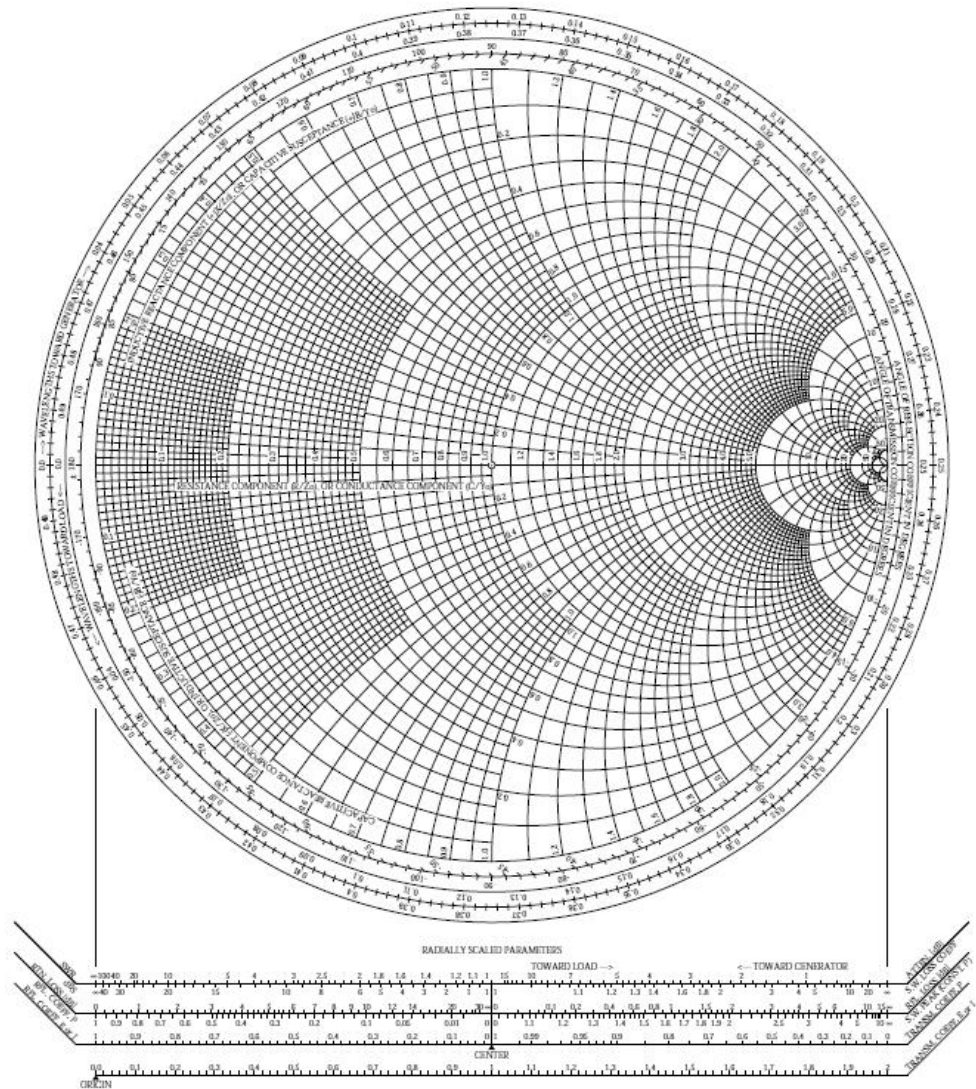
Adaptarea de impedanță

# Diagrama Smith

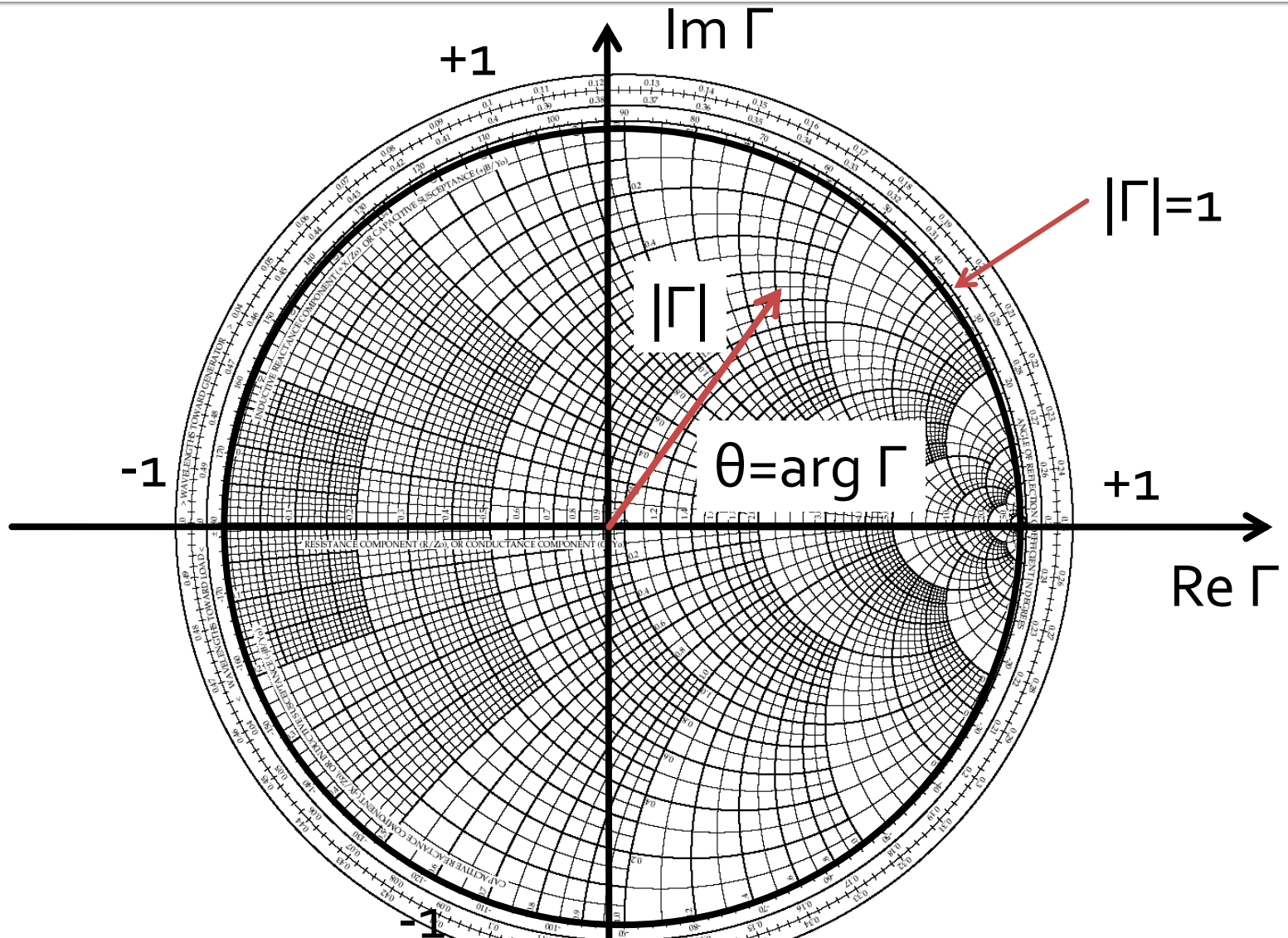
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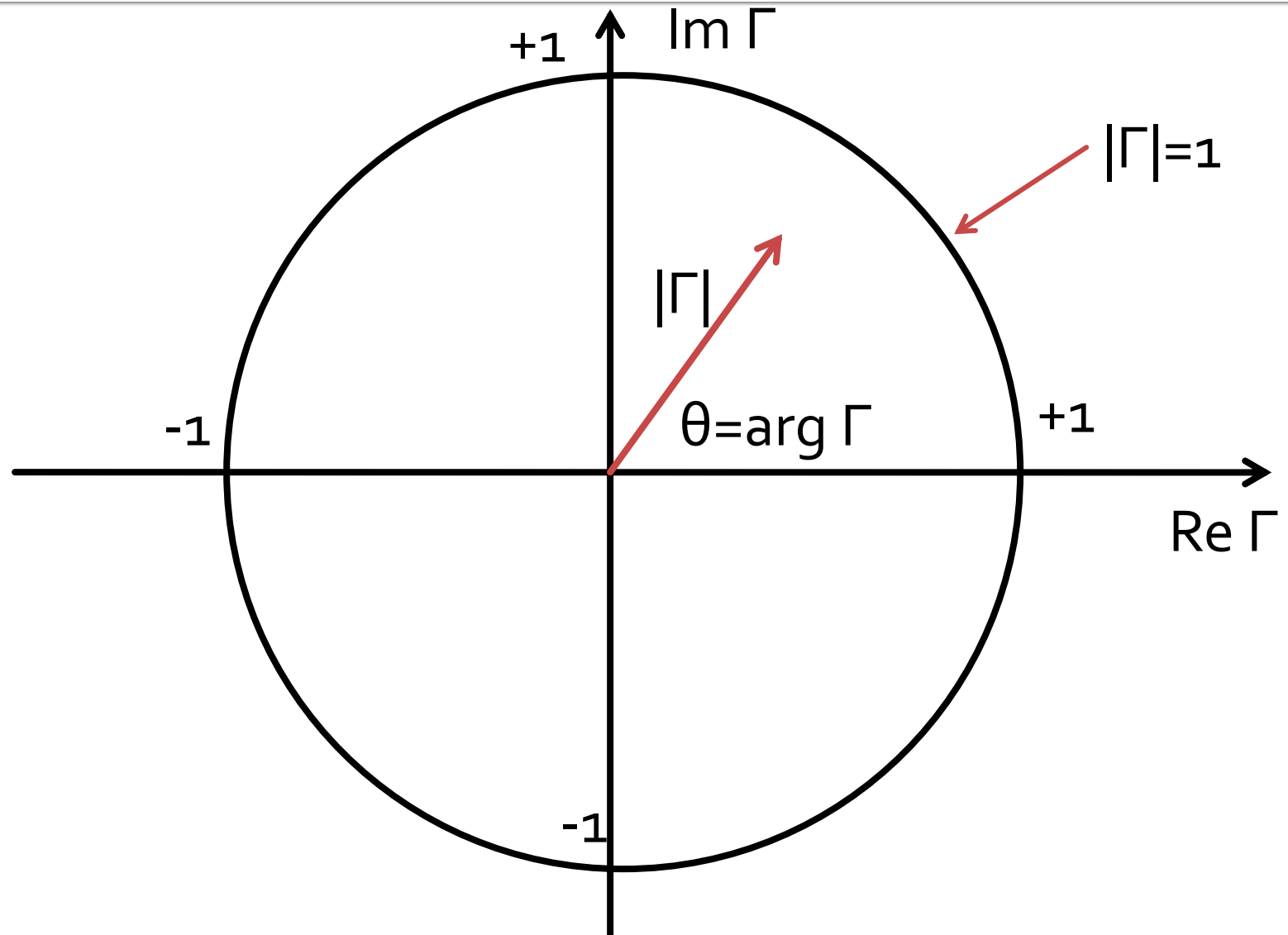
# Diagrama Smith



# Diagrama Smith



# Diagrama Smith

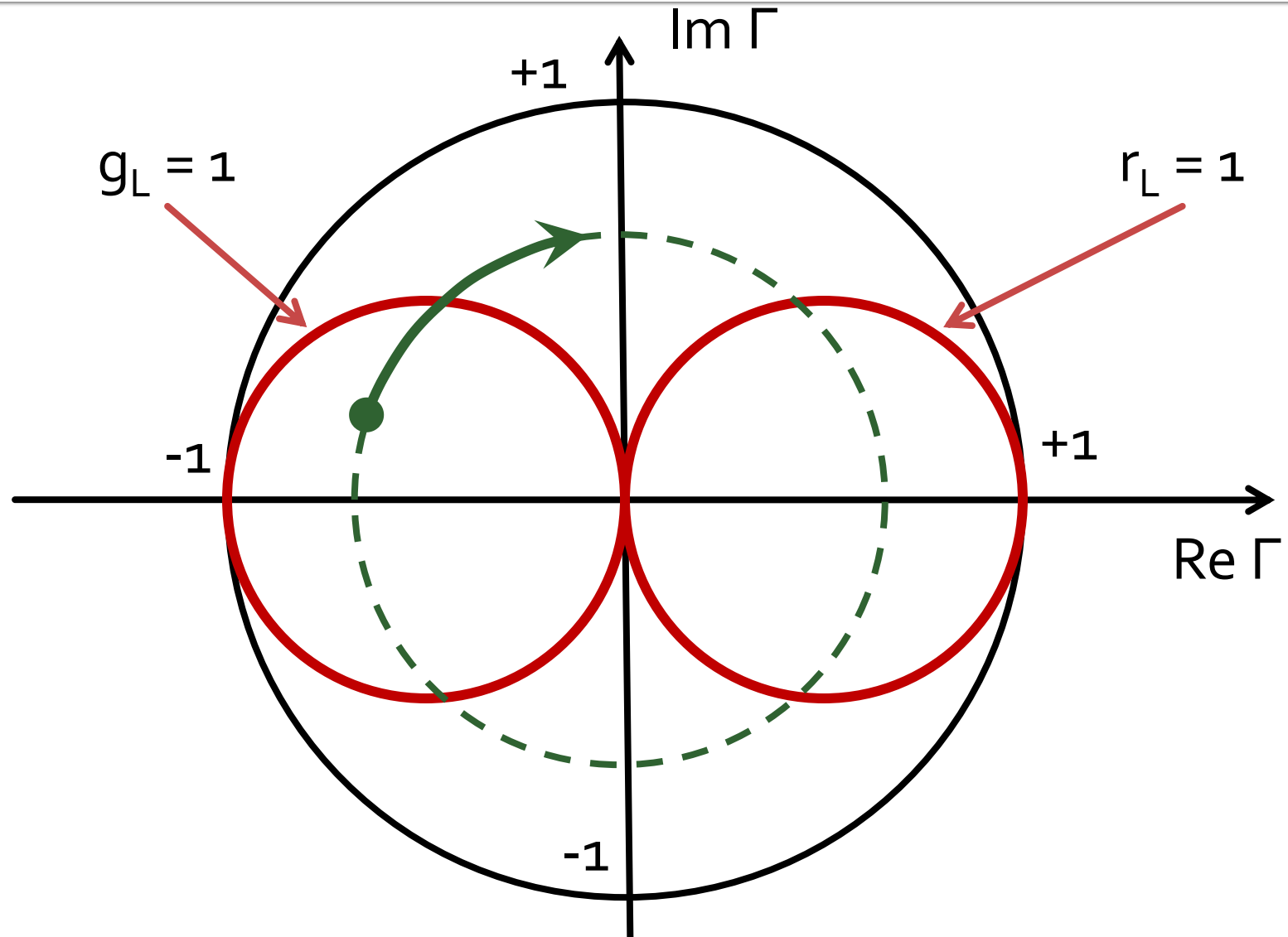


Adaptarea cu sectiuni de linii (stub)

# Adaptarea de impedanță

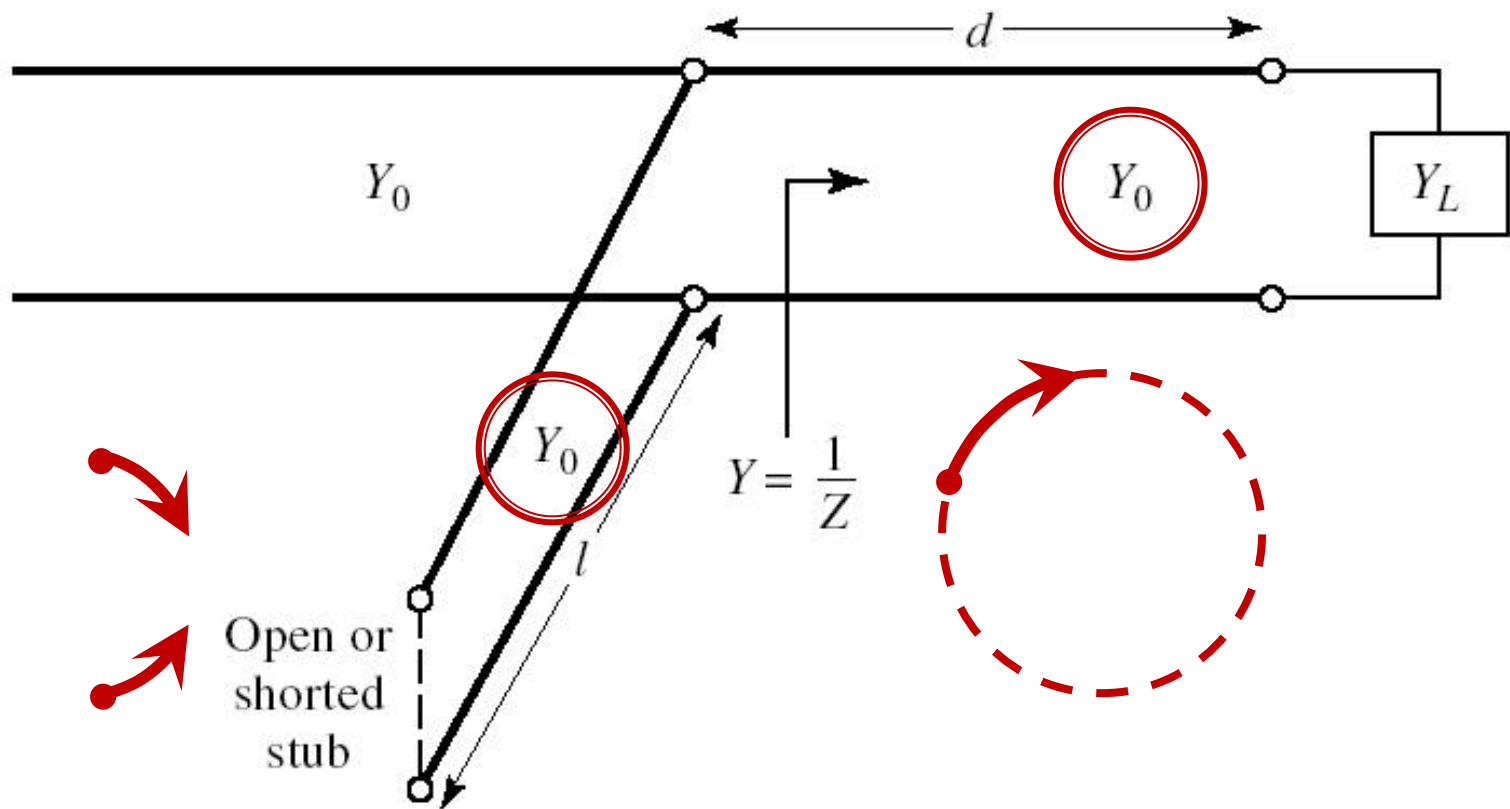


# Diagrama Smith, $r=1$ si $g=1$



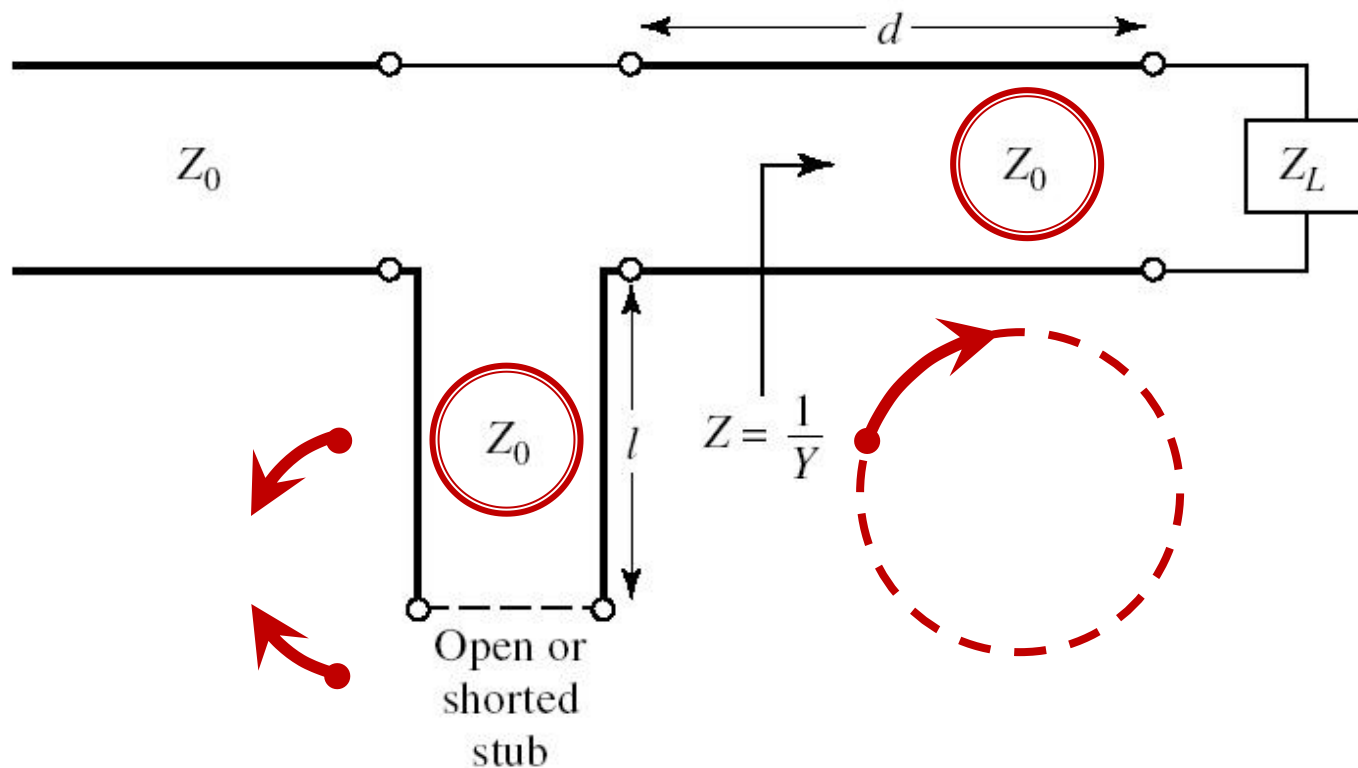
# Single stub tuning

- Shunt Stub (sectiune de linie in paralel)



# Single stub tuning

- Series Stub (secțiune de linie în serie)
- tehnologic mai dificil de realizat la liniile monofilare (microstrip)

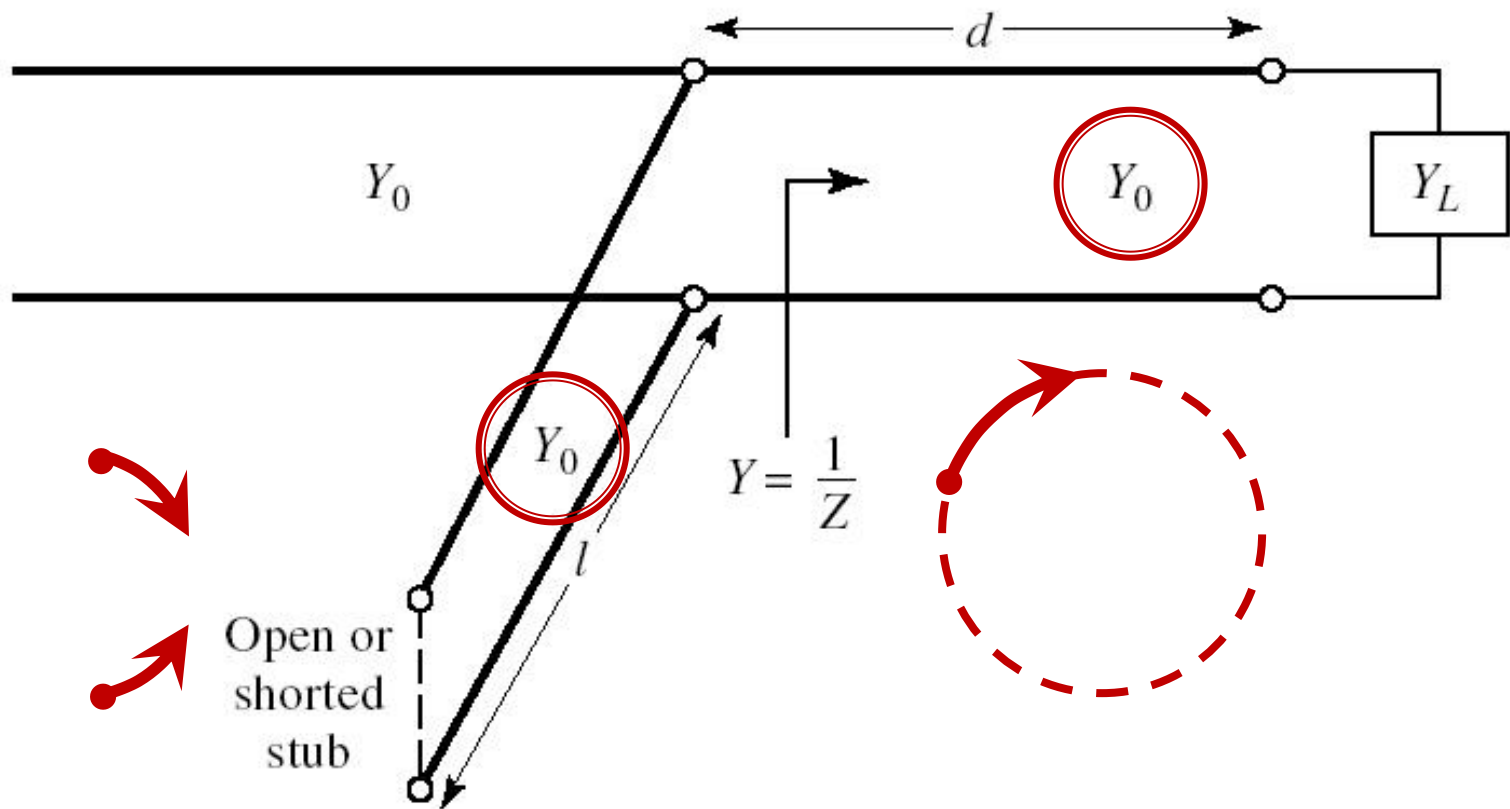


# Solutii analitice

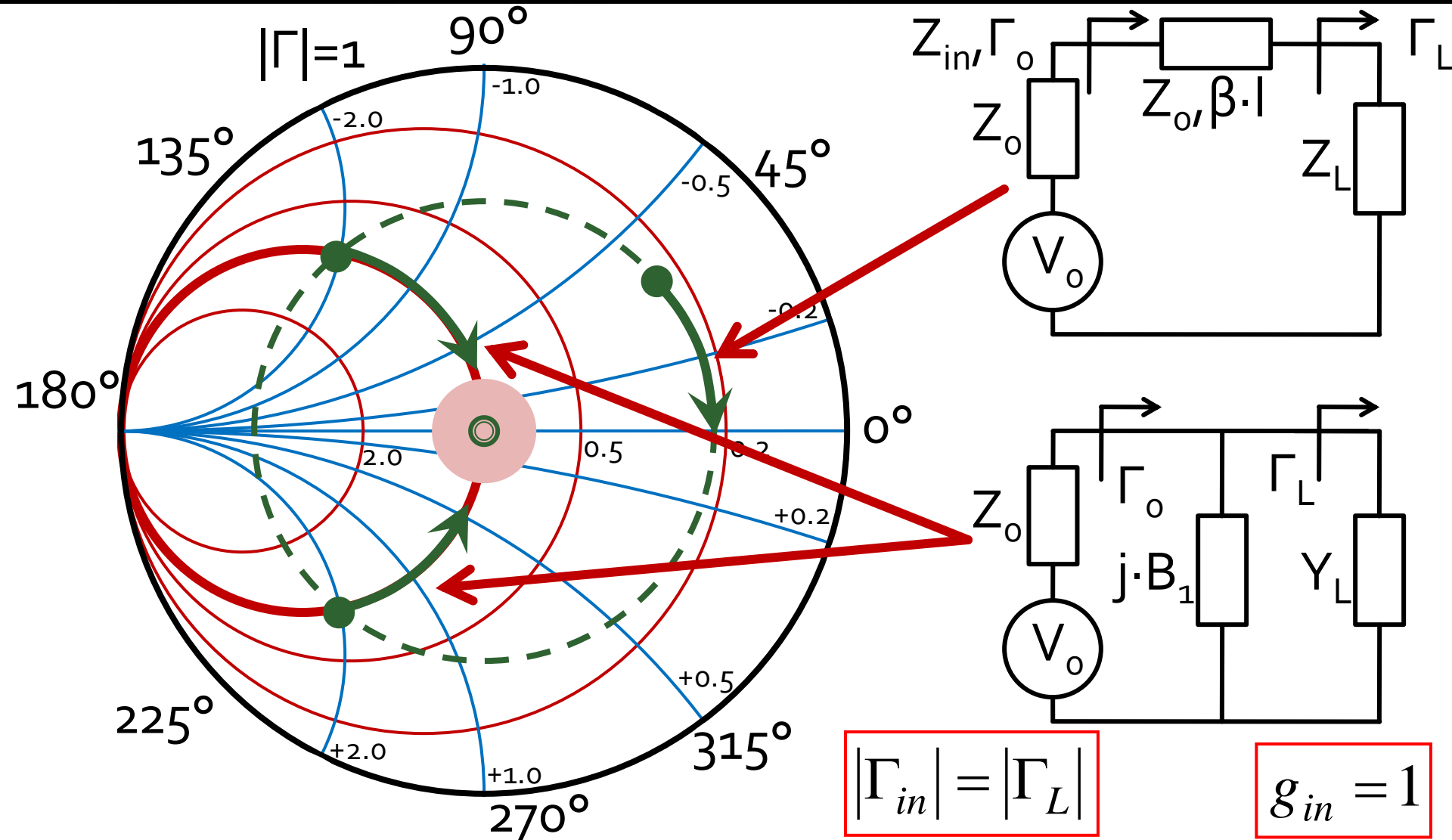
Examen / Proiect

# Caz 1, Shunt Stub

- Shunt Stub (sectiune de linie in paralel)



# Adaptare, linie serie + susceptanta in paralel



# Calcul analitic (calcul efectiv)

$$\cos(\varphi + 2\theta) = -|\Gamma_S|$$

$$\Gamma_S = 0.593 \angle 46.85^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$|\Gamma_S| = 0.593; \quad \varphi = 46.85^\circ \quad \cos(\varphi + 2\theta) = -0.593 \Rightarrow (\varphi + 2\theta) = \pm 126.35^\circ$$

- **Semnul** (+/-) solutiei alese la ecuatia **liniei serie** impune **semnul** solutiei utilizate la ecuatia **stub-ului paralel**

- **solutia "cu +"** ↓

$$(46.85^\circ + 2\theta) = +126.35^\circ \quad \theta = +39.7^\circ \quad \text{Im } y_s = \frac{-2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = -1.472$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_s) = -55.8^\circ \underline{(+180^\circ)} \rightarrow \theta_{sp} = 124.2^\circ$$

- **solutia "cu -"** ↓

$$(46.85^\circ + 2\theta) = -126.35^\circ \quad \theta = -86.6^\circ \underline{(+180^\circ)} \rightarrow \theta = 93.4^\circ$$

$$\text{Im } y_s = \frac{+2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = +1.472 \quad \theta_{sp} = \tan^{-1}(\text{Im } y_s) = 55.8^\circ$$

# Calcul analitic (calcul efectiv)

$$(\varphi + 2\theta) = \begin{cases} +126.35^\circ \\ -126.35^\circ \end{cases} \quad \theta = \begin{cases} 39.7^\circ \\ 93.4^\circ \end{cases} \quad \text{Im}[y_s(\theta)] = \begin{cases} -1.472 \\ +1.472 \end{cases} \quad \theta_{sp} = \begin{cases} -55.8^\circ + 180^\circ = 124.2^\circ \\ +55.8^\circ \end{cases}$$

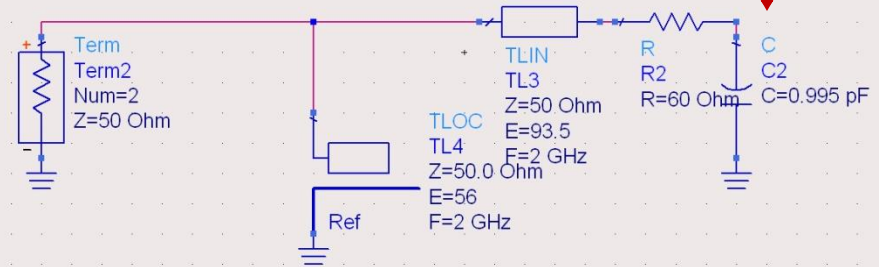
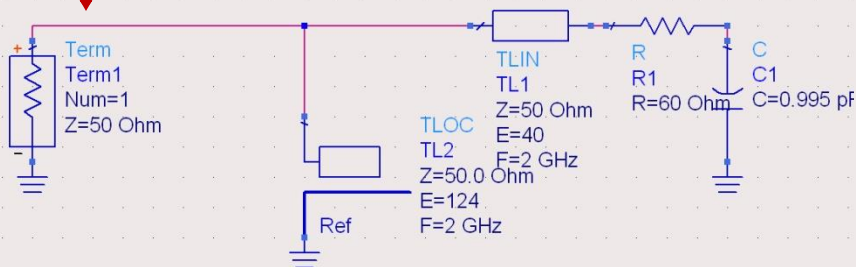
- Se alege **una** din cele doua solutii posibile
- **Semnul** (+/-) solutiei alese la **prima** ecuatie impune **semnul** solutiei utilizate la a **doua** ecuatie

$$l_1 = \frac{39.7^\circ}{360^\circ} \cdot \lambda = 0.110 \cdot \lambda$$

$$l_2 = \frac{124.2^\circ}{360^\circ} \cdot \lambda = 0.345 \cdot \lambda$$

$$l_1 = \frac{93.4^\circ}{360^\circ} \cdot \lambda = 0.259 \cdot \lambda$$

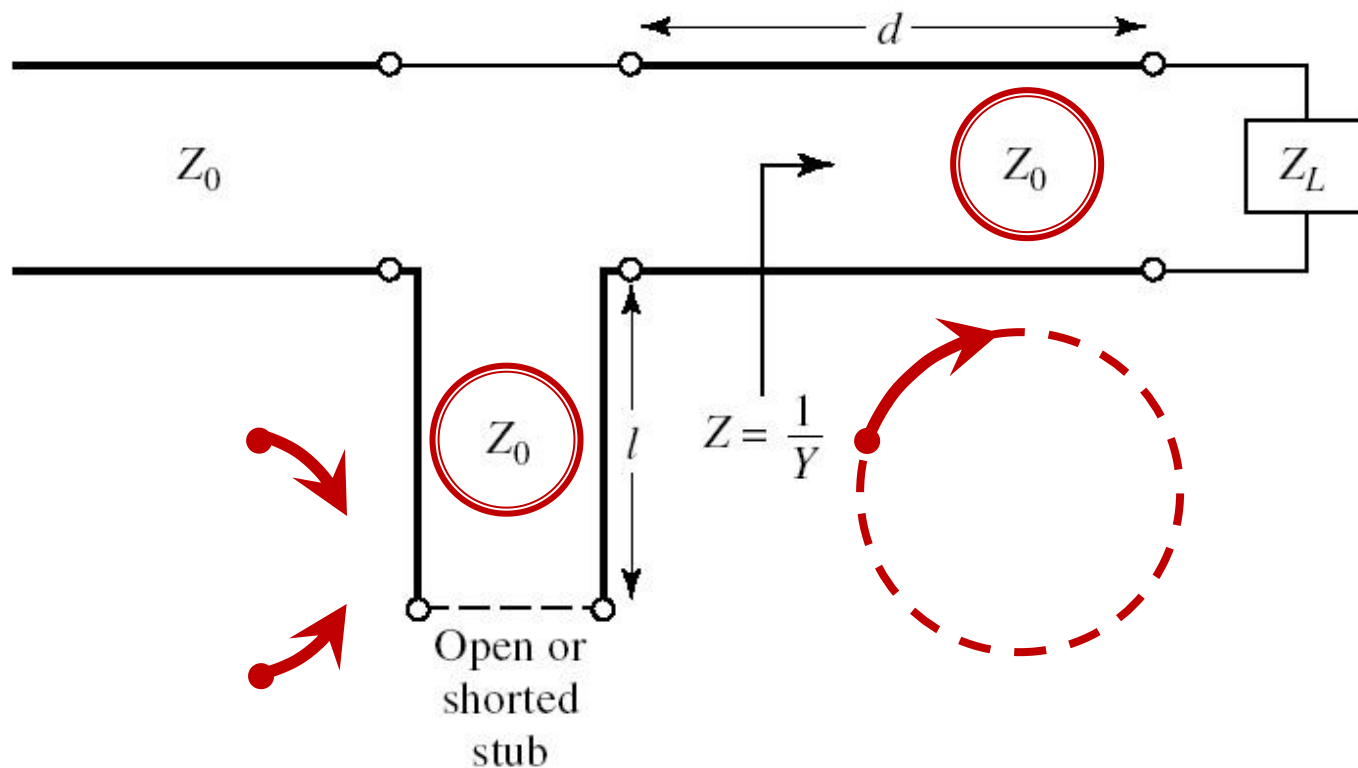
$$l_2 = \frac{55.8^\circ}{360^\circ} \cdot \lambda = 0.155 \cdot \lambda$$



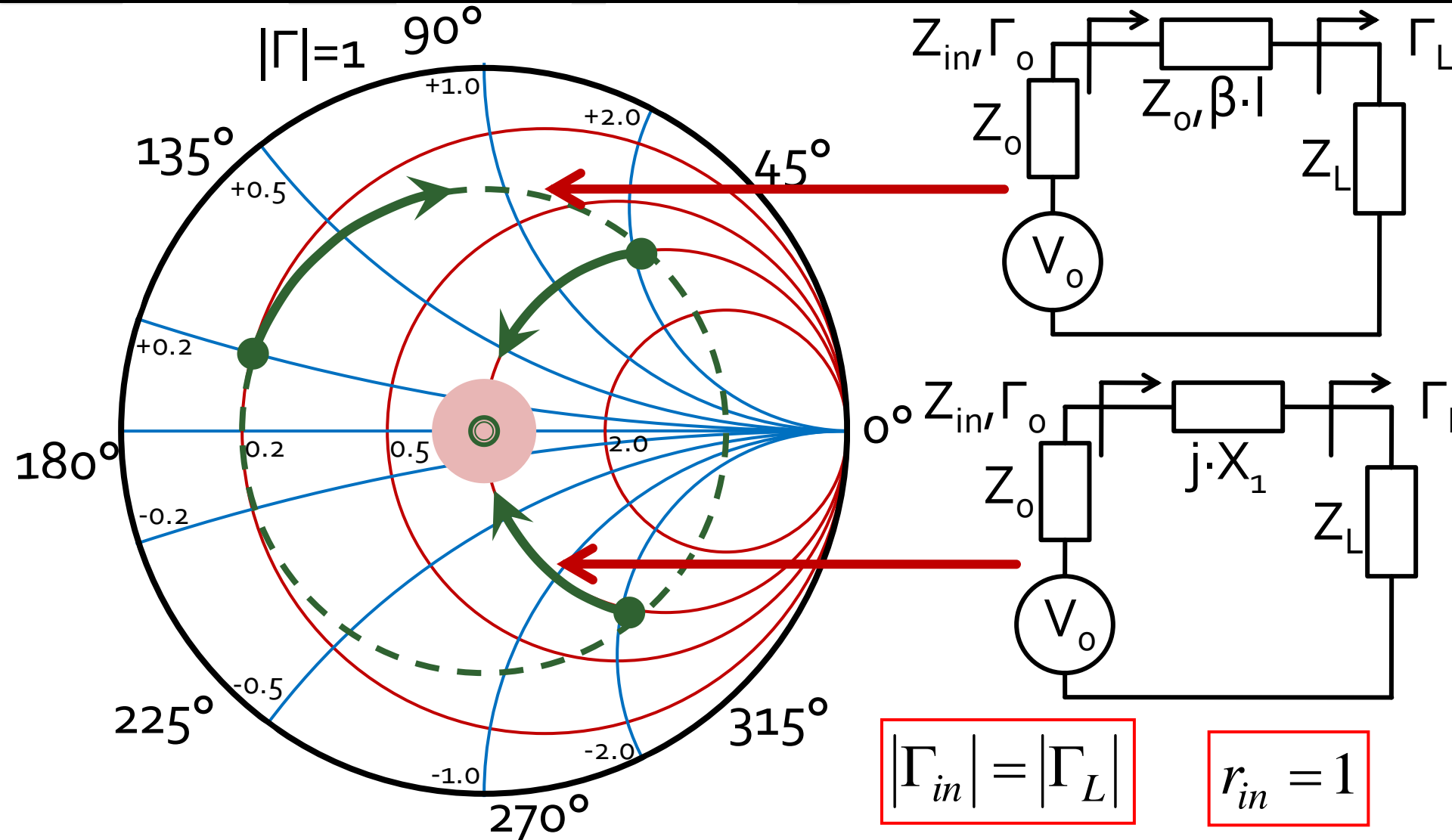


# Caz 2, Series Stub

- Series Stub (sectiune de linie in serie)
- tehnologic mai dificil de realizat la liniile monofilare (microstrip)



# Adaptare, linie serie + reactanta in serie



# Calcul analitic (calcul efectiv)

$$\cos(\varphi + 2\theta) = |\Gamma_s|$$

$$\theta_{ss} = \beta \cdot l = \cot^{-1} \frac{\mp 2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}}$$

$$\Gamma_s = 0.555 \angle -29.92^\circ$$

$$|\Gamma_s| = 0.555; \quad \varphi = -29.92^\circ \quad \cos(\varphi + 2\theta) = 0.555 \Rightarrow (\varphi + 2\theta) = \pm 56.28^\circ$$

- **Semnul** (+/-) solutiei alese la ecuatia **liniei serie** impune **semnul** solutiei utilizate la ecuatia **stub-ului serie**

- **solutia "cu +"** ↓

$$(-29.92^\circ + 2\theta) = +56.28^\circ \quad \theta = 43.1^\circ \quad \text{Im } z_s = \frac{+2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = +1.335$$

$$\theta_{ss} = -\cot^{-1}(\text{Im } z_s) = -36.8^\circ (+180^\circ) \rightarrow \theta_{ss} = 143.2^\circ$$

- **solutia "cu -"** ↓

$$(-29.92^\circ + 2\theta) = -56.28^\circ \quad \theta = -13.2^\circ (+180^\circ) \rightarrow \theta = 166.8^\circ$$

$$\text{Im } z_s = \frac{-2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = -1.335 \quad \theta_{ss} = -\cot^{-1}(\text{Im } z_s) = 36.8^\circ$$

# Calcul analitic (calcul efectiv)

$$(\varphi + 2\theta) = \begin{cases} +56.28^\circ \\ -56.28^\circ \end{cases} \quad \theta = \begin{cases} 43.1^\circ \\ 166.8^\circ \end{cases} \quad \text{Im}[z_s(\theta)] = \begin{cases} +1.335 \\ -1.335 \end{cases} \quad \theta_{ss} = \begin{cases} -36.8^\circ + 180^\circ = 143.2^\circ \\ +36.8^\circ \end{cases}$$

- Se alege **una** din cele doua solutii posibile
- **Semnul** (+/-) solutiei alese la **prima** ecuatie impune **semnul** solutiei utilizate la a **doua** ecuatie

$$l_1 = \frac{43.1^\circ}{360^\circ} \cdot \lambda = 0.120 \cdot \lambda$$

$$l_2 = \frac{143.2^\circ}{360^\circ} \cdot \lambda = 0.398 \cdot \lambda$$

$$l_1 = \frac{166.8^\circ}{360^\circ} \cdot \lambda = 0.463 \cdot \lambda$$

$$l_2 = \frac{36.8^\circ}{360^\circ} \cdot \lambda = 0.102 \cdot \lambda$$



# Stub, observatii

- adunarea si scadere de **180°** ( $\lambda/2$ ) nu schimba rezultatul (rotatie completa in jurul diagramei)

$$E = \beta \cdot l = \pi = 180^\circ \quad l = k \cdot \frac{\lambda}{2}, \forall k \in \mathbf{N}$$

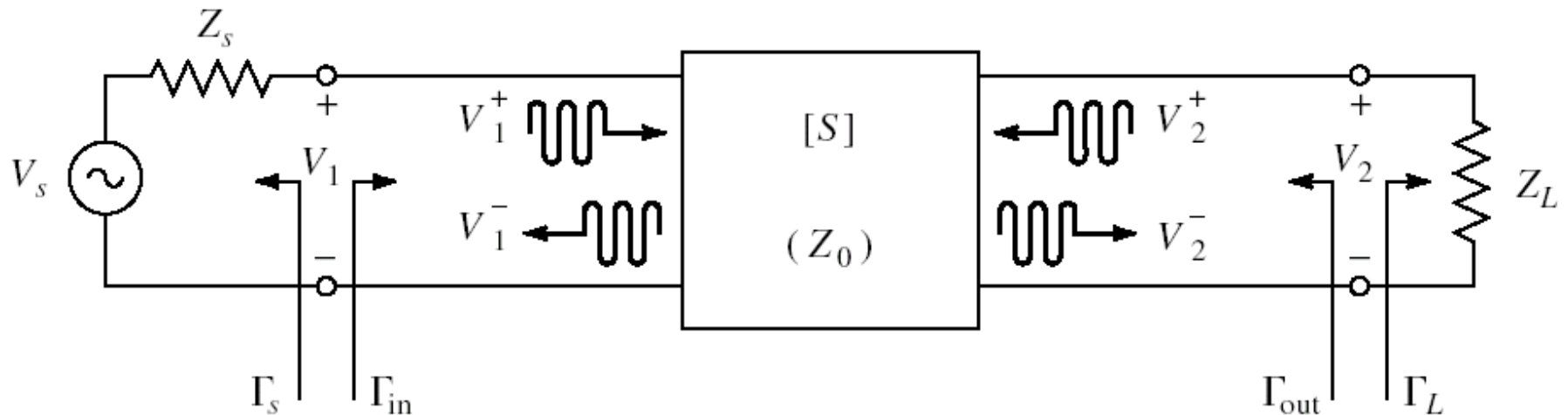
- pentru linii de “lungime” / “lungime electrica” **negative** se adauga  $\lambda/2$  /  $180^\circ$  pentru a avea valoare pozitiva (realizabila fizic)
- o adaugare sau scadere de **90°** ( $\lambda/4$ ) transforma impedanta stub-ului:

$$Z_{in,sc} = j \cdot Z_0 \cdot \tan \beta \cdot l \quad \Leftrightarrow \quad Z_{in,g} = -j \cdot Z_0 \cdot \cot \beta \cdot l$$

- pentru stub se poate adauga/scadea  $90^\circ$  ( $\lambda/4$ ) simultan cu schimbare **gol**  $\Leftrightarrow$  **scurtcircuit**

# Amplificatoare de microunde

# Cuadripol Amplificator (diport)



- Caracterizare cu parametri S
- Normalizati la  $Z_0$  (implicit  $50\Omega$ )
- Cataloage: parametri S pentru anumite polarizari

# Catalogue

## NE46100

VCE = 5 V, Ic = 50 mA

FREQUENCY (MHz)	S11		S21		S12		S22		K	MAG <sup>2</sup> (dB)
	MAG	ANG	MAG	ANG	MAG	ANG	MAG	ANG		
100	0.778	-137	26.776	114	0.028	30	0.555	-102	0.16	29.8
200	0.815	-159	14.407	100	0.035	29	0.434	-135	0.36	26.2
500	0.826	-177	5.855	84	0.040	38	0.400	-162	0.75	21.7
800	0.827	176	3.682	76	0.052	43	0.402	-169	0.91	18.5
1000	0.826	173	2.963	71	0.058	47	0.405	-172	1.02	16.3
1200	0.825	170	2.441	66	0.064	47	0.412	-174	1.08	14.0
1400	0.820	167	2.111	61	0.069	47	0.413	-176	1.17	12.4
1600	0.828	165	1.863	57	0.078	54	0.426	-177	1.15	11.4
1800	0.827	162	1.671	53	0.087	50	0.432	-178	1.14	10.6
2000	0.828	159	1.484	49	0.093	50	0.431	-180	1.17	9.5
2500	0.822	153	1.218	39	0.11	48	0.462	177	1.18	7.8
3000	0.818	148	1.010	30	0.135	46	0.490	174	1.16	6.3
3500	0.824	142	0.876	21	0.147	44	0.507	170	1.16	5.3
4000	0.812	137	0.762	13	0.168	38	0.535	167	1.14	4.3

VCE = 5 V, Ic = 100 mA

100	0.778	-144	27.669	111	0.027	35	0.523	-114	0.27	30.2
200	0.820	-164	14.559	97	0.029	29	0.445	-144	0.42	27.0
500	0.832	-179	5.885	84	0.035	38	0.435	-166	0.81	22.2
800	0.833	175	3.691	76	0.048	45	0.435	-173	0.95	18.8
1000	0.831	172	2.980	71	0.056	51	0.437	-176	1.05	16.0
1200	0.836	169	2.464	67	0.061	52	0.432	-178	1.11	14.0
1400	0.829	166	2.121	61	0.072	53	0.447	-180	1.12	12.6
1600	0.831	164	1.867	58	0.080	54	0.445	179	1.14	11.4

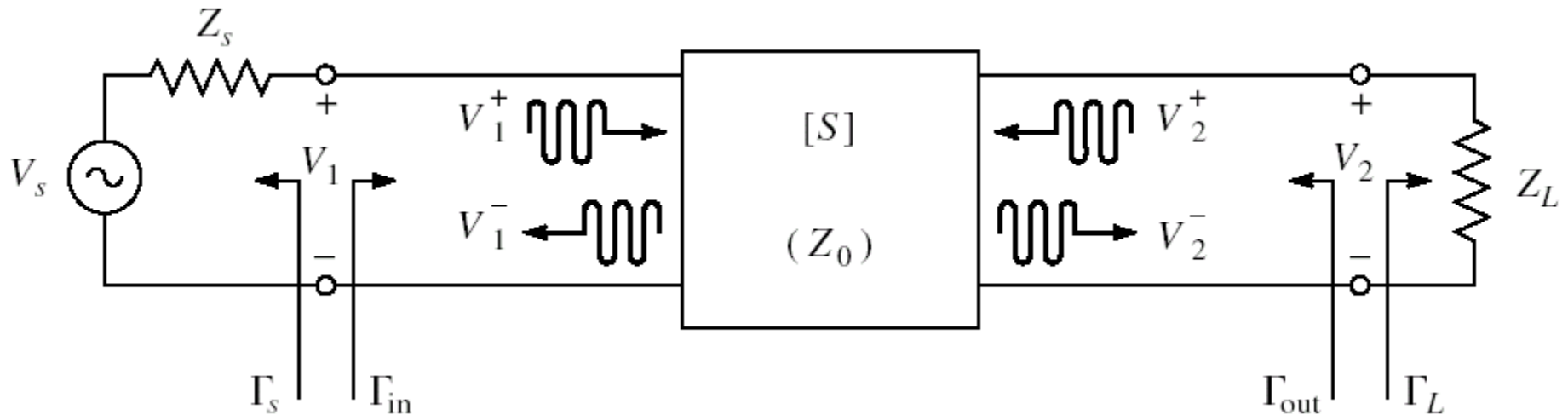


# S2P - Touchstone

- Fisiere format Touchstone (\*.s2p)

```
! SIEMENS Small Signal Semiconductors
! VDS = 3.5 V   ID = 15 mA
# GHz S MA R 50
! f      S11      S21      S12      S22
! GHz  MAG ANG  MAG ANG  MAG ANG  MAG ANG
1.000 0.9800 -18.0 2.230 157.0 0.0240 74.0 0.6900 -15.0
2.000 0.9500 -39.0 2.220 136.0 0.0450 57.0 0.6600 -30.0
3.000 0.8900 -64.0 2.210 110.0 0.0680 40.0 0.6100 -45.0
4.000 0.8200 -89.0 2.230 86.0 0.0850 23.0 0.5600 -62.0
5.000 0.7400 -115.0 2.190 61.0 0.0990 7.0 0.4900 -80.0
6.000 0.6500 -142.0 2.110 36.0 0.1070 -10.0 0.4100 -98.0
!
! f      Fmin  Gammaopt rn/50
! GHz    dB   MAG ANG  -
2.000    1.00 0.72 27 0.84
4.000    1.40 0.64 61 0.58
```

# Diport amplificador

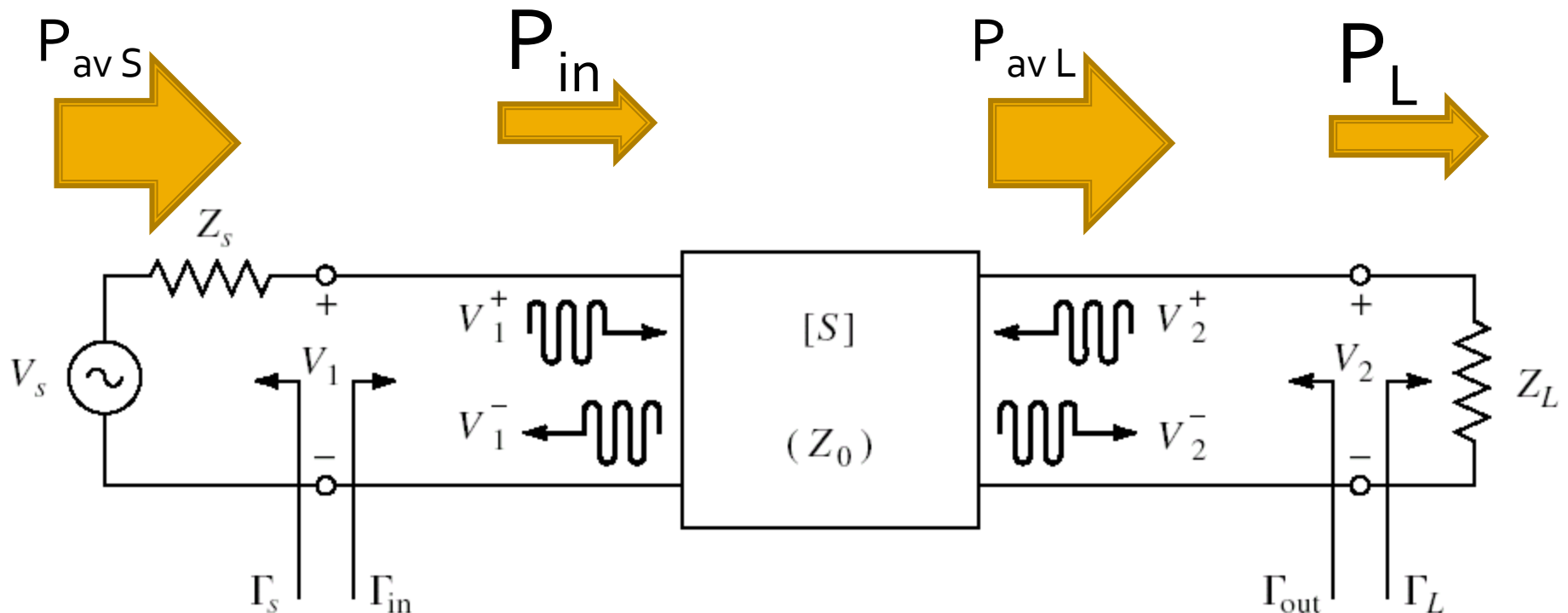


$$\Gamma_{in} = \frac{V_1^-}{V_1^+} = S_{11} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_L}{1 - S_{22} \cdot \Gamma_L}$$

$$\Gamma_{out} = \frac{V_2^-}{V_2^+} = S_{22} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_s}{1 - S_{11} \cdot \Gamma_s}$$

# Puteri / Adaptare

- Doua porturi in care adaptarea influențează transferul de putere



# Castig de putere

- Castigul de putere de **transfer** (transducer power gain)

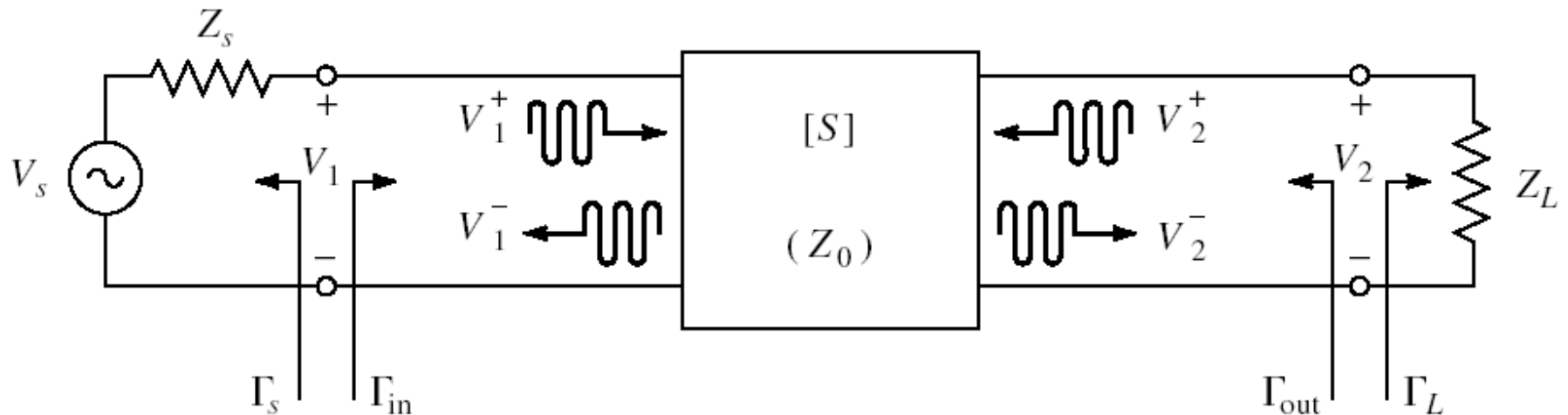
$$G_T = \frac{P_L}{P_{av S}} = \frac{|S_{21}|^2 \cdot (1 - |\Gamma_S|^2) \cdot (1 - |\Gamma_L|^2)}{|1 - \Gamma_S \cdot \Gamma_{in}|^2 \cdot |1 - S_{22} \cdot \Gamma_L|^2} \quad \Gamma_{in} = \Gamma_{in}(\Gamma_L)$$

- Castigul de putere de **transfer unilateral**

$$G_{TU} = |S_{21}|^2 \cdot \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2} \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2} \quad S_{12} \cong 0 \quad \Gamma_{in} = S_{11}$$

Permite tratarea separata  
a intrarii si iesirii

# Cuadripol Amplificator

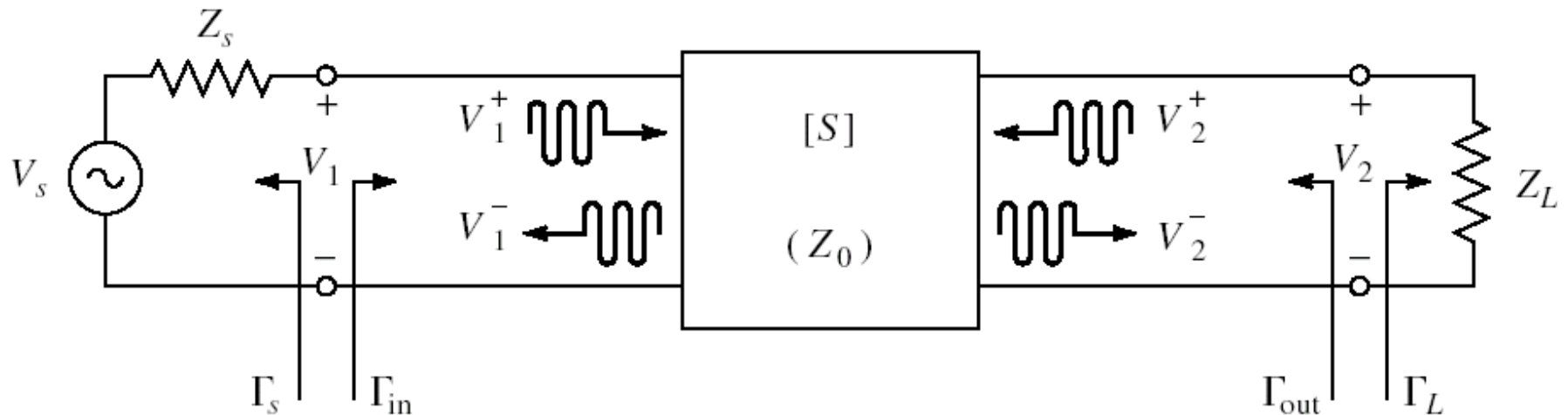


- marimi care intereseaza:
  - stabilitate
  - castig de putere
  - zgomot (uneori – semnal mic)
  - liniaritate (uneori – semnal mare)

Amplificatoare de microunde

# Stabilitate

# Cuadripol Amplificator



- marimi care intereseaza:
  - **stabilitate**
  - castig de putere
  - zgomot (uneori – semnal mic)
  - liniaritate (uneori – semnal mare)

# Stabilitate

- C7  $\Gamma = \Gamma_r + j \cdot \Gamma_i$   $r_L = \frac{1 - \Gamma_r^2 - \Gamma_i^2}{(1 - \Gamma_r)^2 + \Gamma_i^2}$   
 $Z_{in}$   $\Gamma_{in} = \Gamma_r + j \cdot \Gamma_i$

- instabilitate

$$\operatorname{Re}\{Z_{in}\} < 0 \Leftrightarrow 1 - \Gamma_r^2 - \Gamma_i^2 < 0 \quad |\Gamma_{in}| > 1$$

- stabilitate,  $Z_{in}$

- conditii ce trebuie indeplinite de  $\Gamma_L$  pentru a obtine stabilitatea (la intrare)

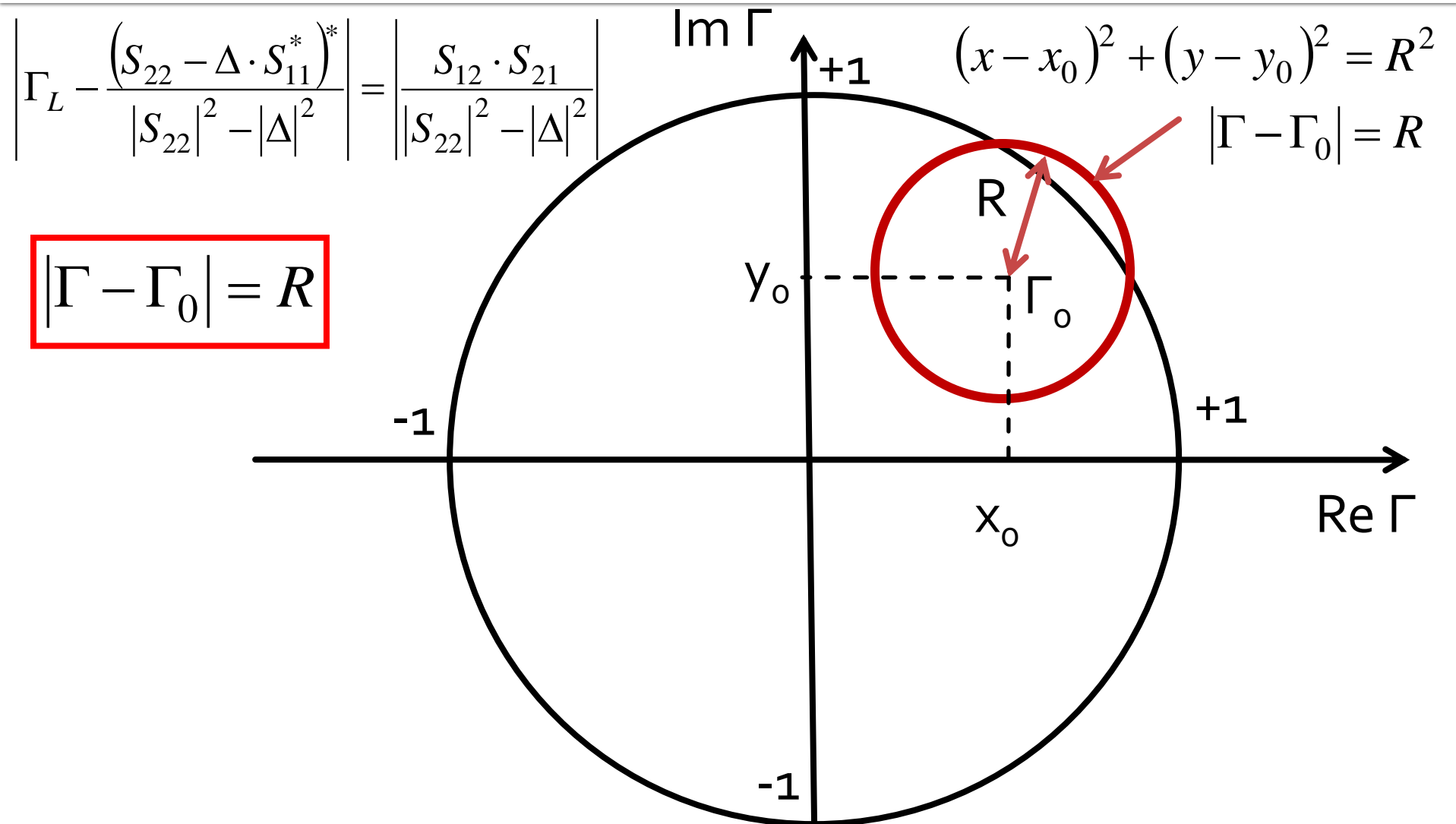
$$|\Gamma_{in}| < 1 \quad \left| S_{11} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_L}{1 - S_{22} \cdot \Gamma_L} \right| < 1$$

- similar  $Z_{out}$

- conditii ce trebuie indeplinite de  $\Gamma_S$  pentru a obtine stabilitatea (la iesire)



# Stabilitate



# Cerc de stabilitate la iesire (CSOUT)

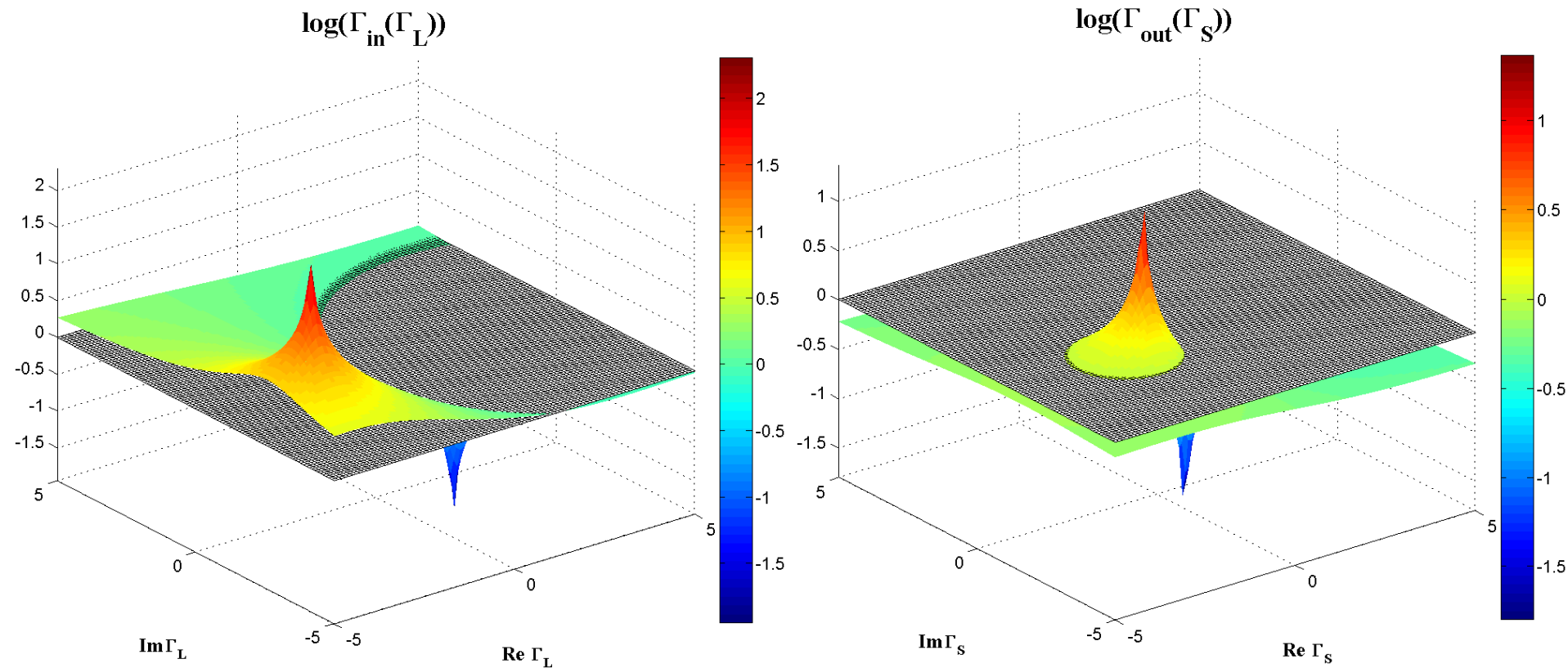
$$\left| \Gamma_L - \frac{(S_{22} - \Delta \cdot S_{11}^*)^*}{|S_{22}|^2 - |\Delta|^2} \right| = \left| \frac{S_{12} \cdot S_{21}}{|S_{22}|^2 - |\Delta|^2} \right| \quad |\Gamma_L - C_L| = R_L$$

- Ecuația unui cerc, care reprezintă locul geometric al punctelor  $\Gamma_L$  pentru **limita** de stabilitate
- Cercul se numește **cerc de stabilitate la iesire** ( $\Gamma_L$ )

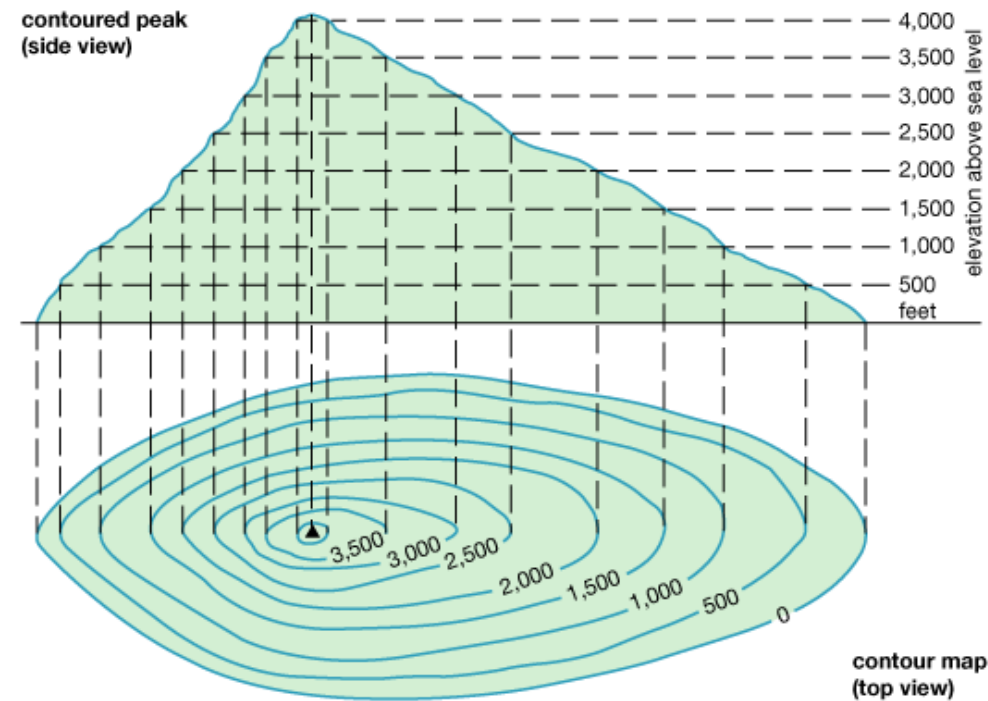
$$C_L = \frac{(S_{22} - \Delta \cdot S_{11}^*)^*}{|S_{22}|^2 - |\Delta|^2} \quad R_L = \frac{|S_{12} \cdot S_{21}|}{\left| |S_{22}|^2 - |\Delta|^2 \right|}$$

# Reprezentare 3D $|\Gamma_{in}|$ , $|\Gamma_{out}|$ , $|\Gamma|=1$

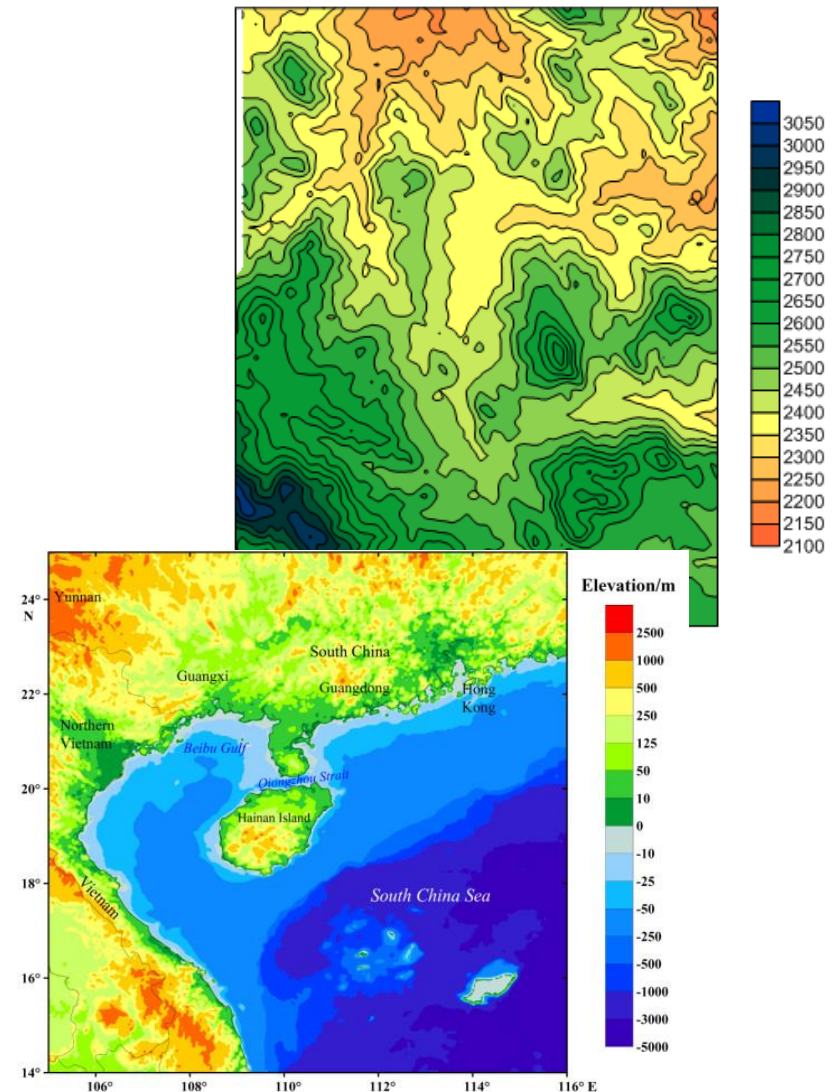
- $|\Gamma| = 1 \rightarrow \log_{10}|\Gamma| = 0$ , intersectia = cerc



# Contour map/lines

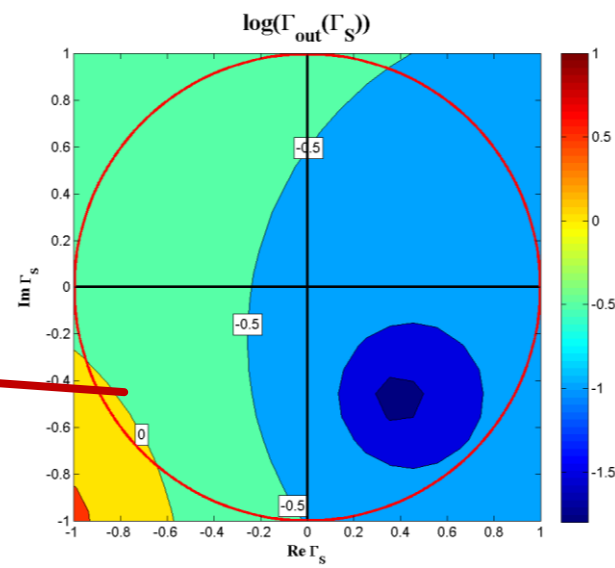
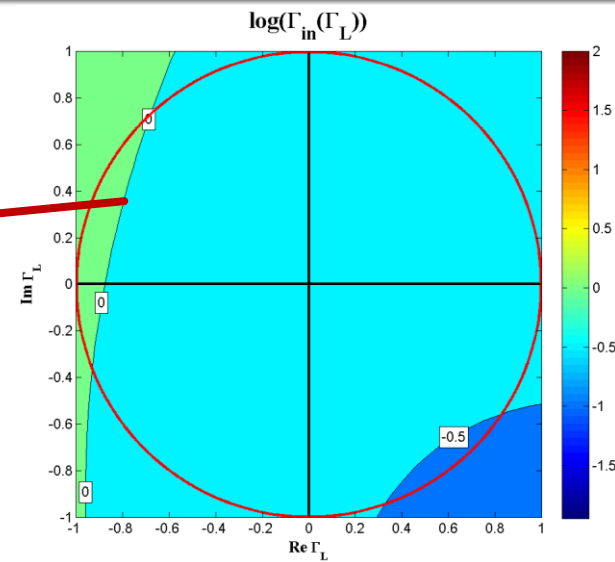
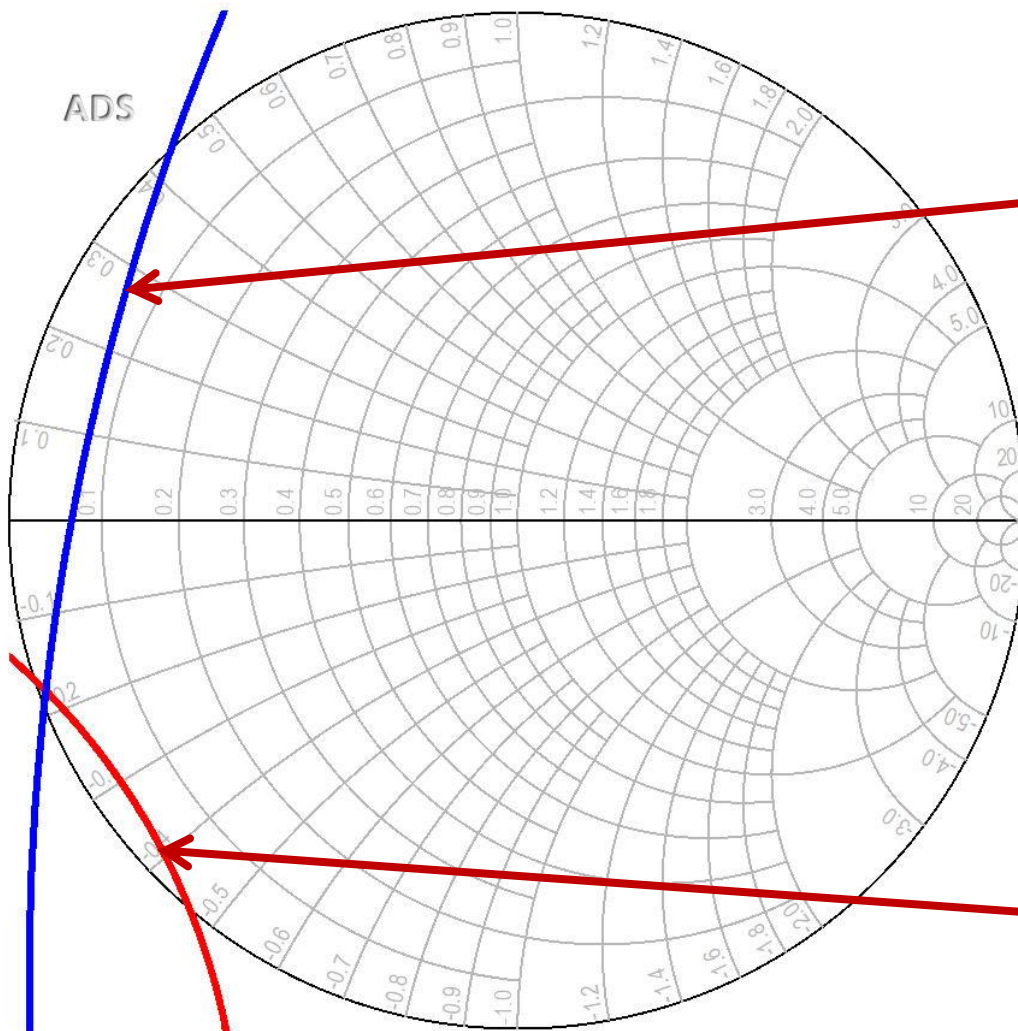


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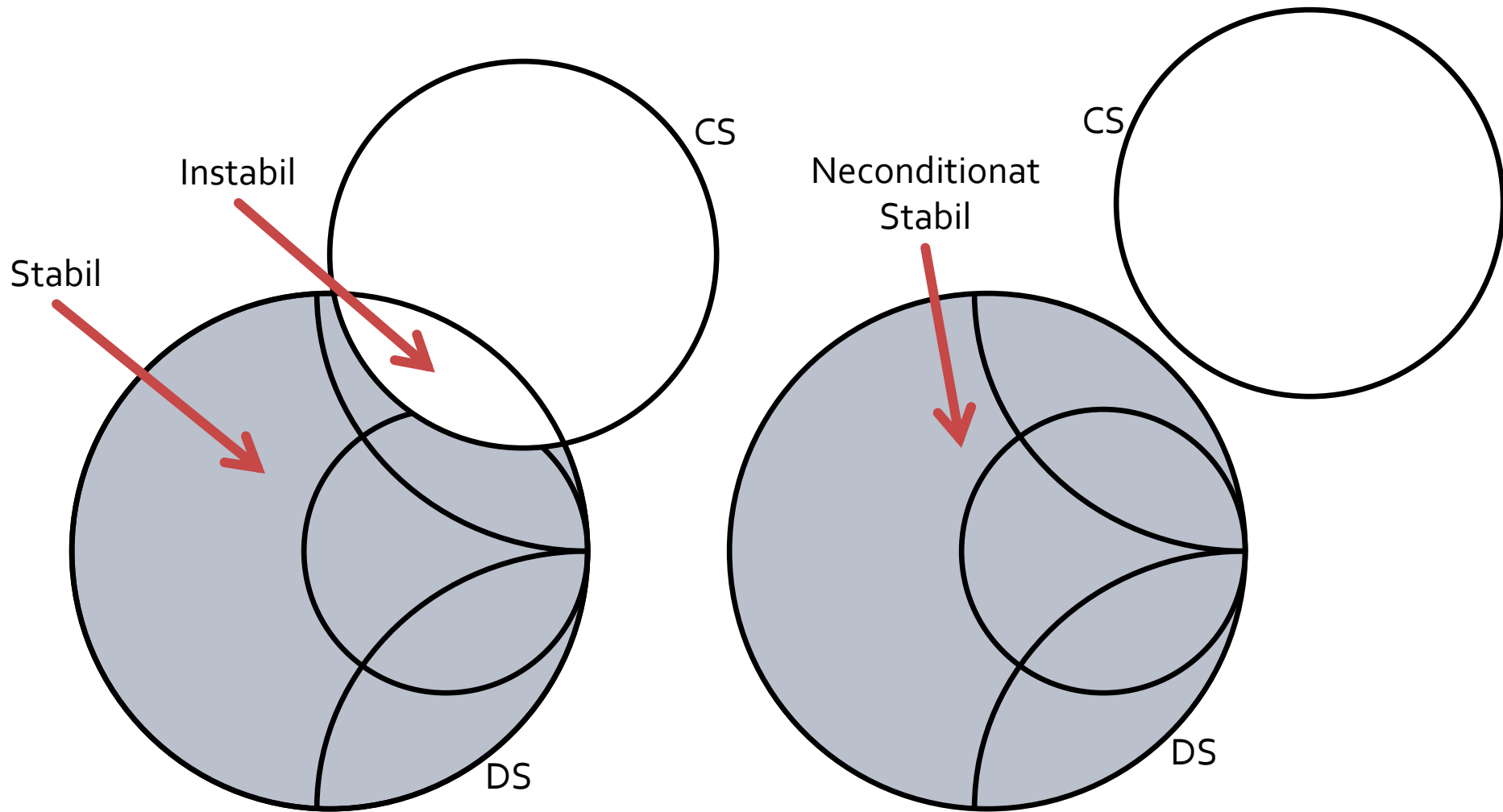


# CSIN, CSOUT

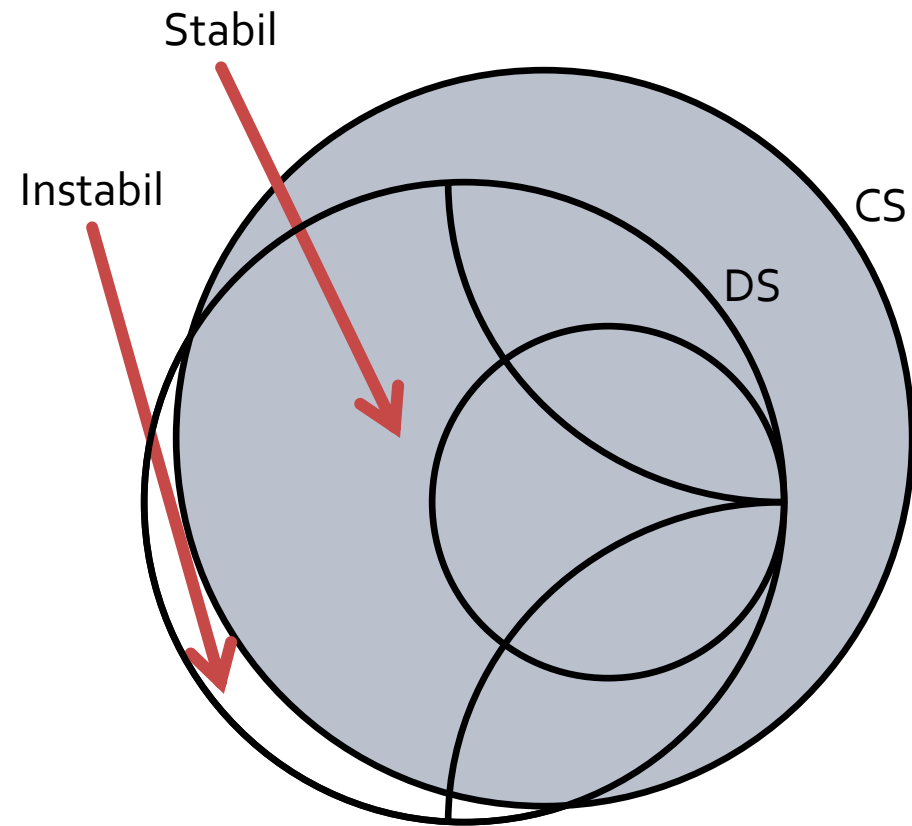
CSOUT  
CSIN



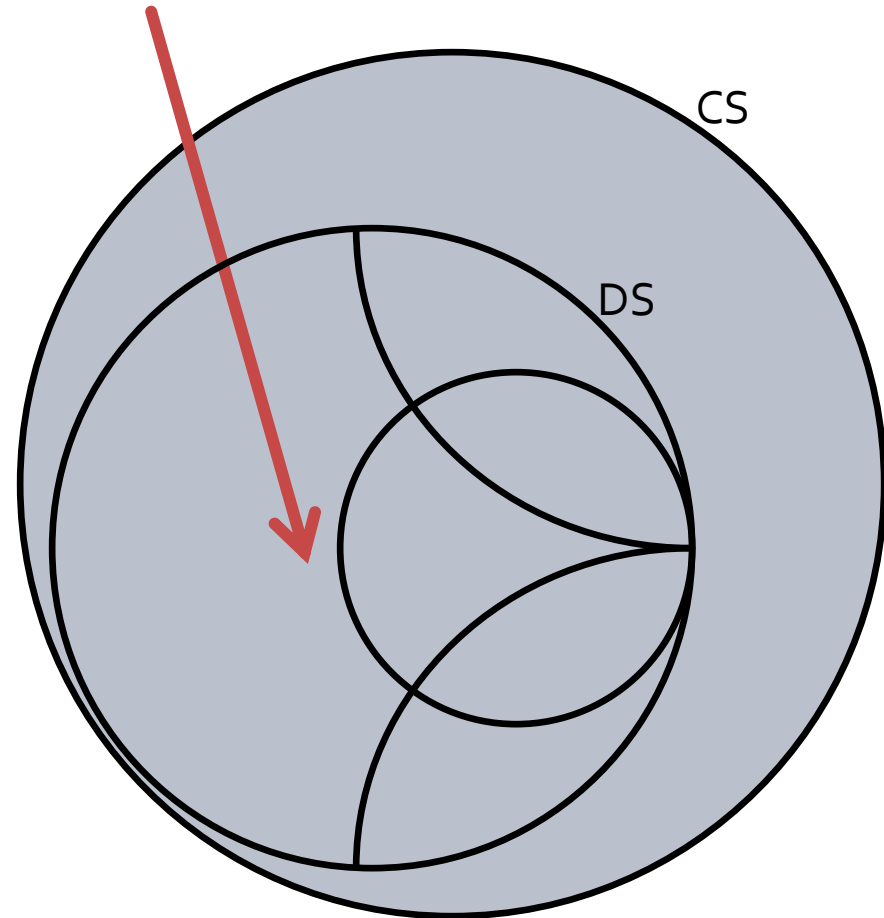
# Mai multe pozitionari posibile



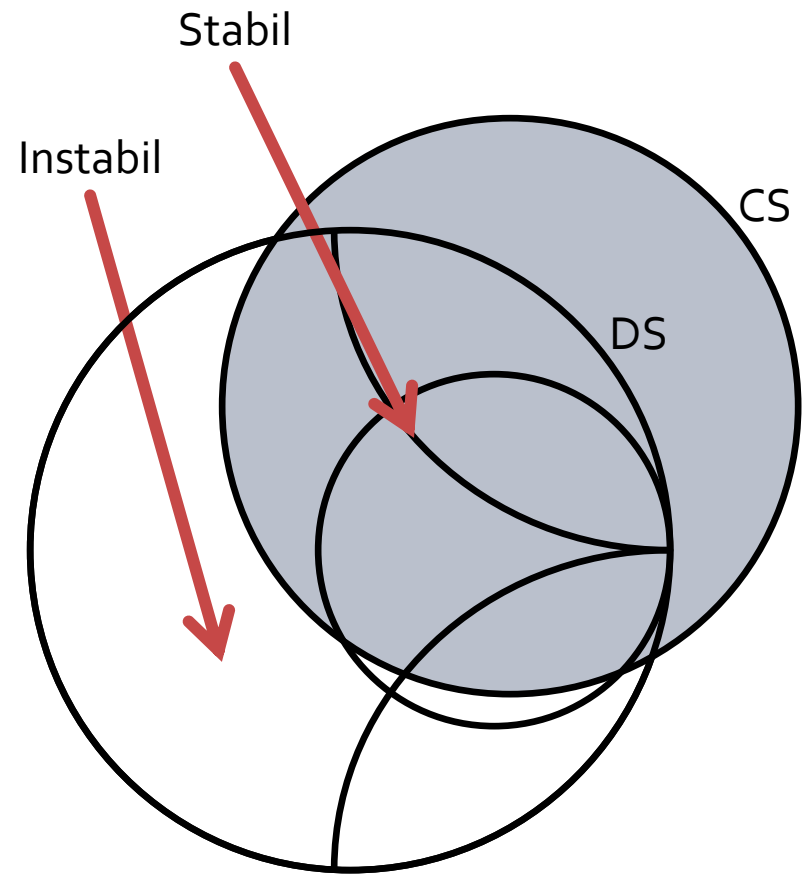
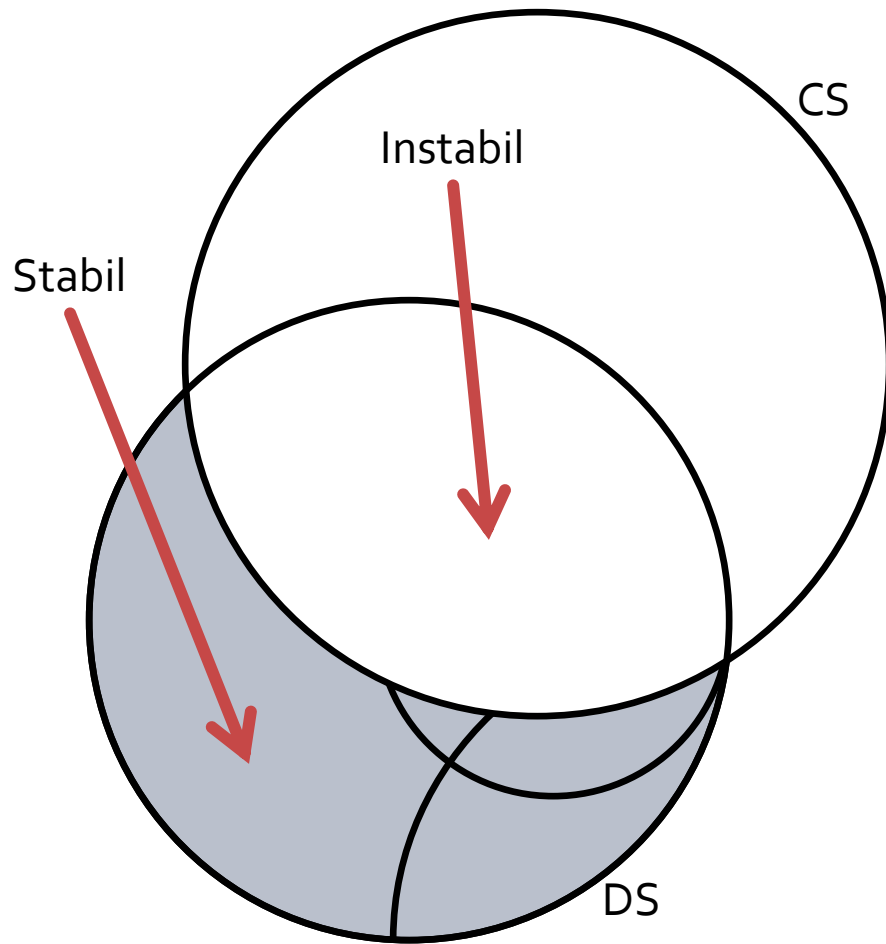
# Mai multe pozitionari posibile



Neconditionat  
Stabil



# Pozitionari mai rare





# Stabilitate

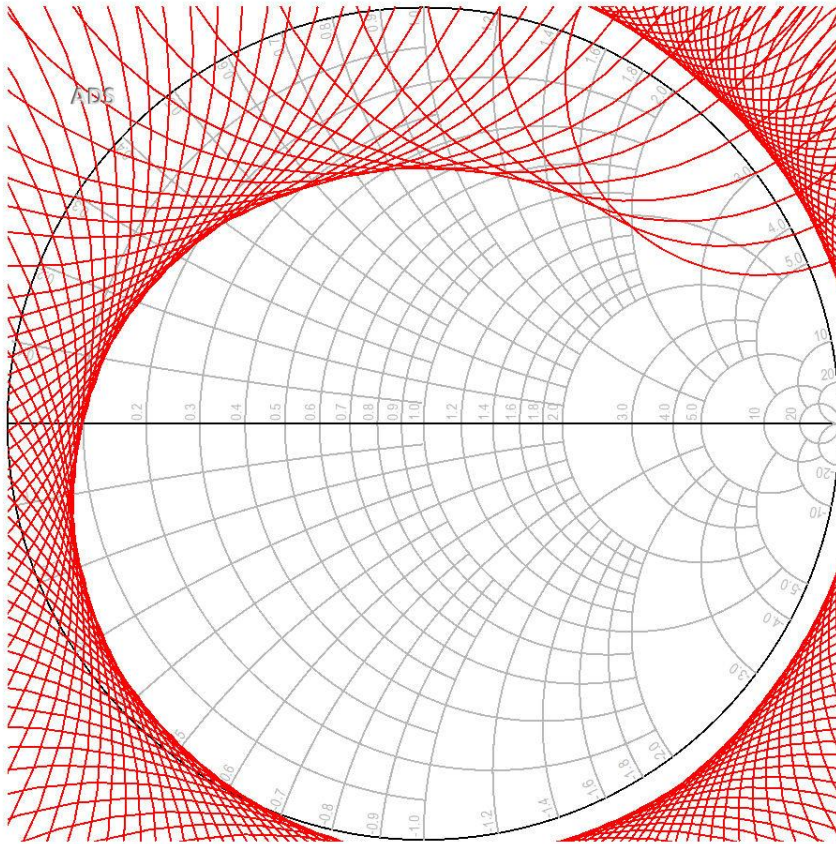
- **Stabilitatea necondiționată:** circuitul este necondiționat stabil dacă  $|\Gamma_{in}| < 1$  și  $|\Gamma_{out}| < 1$  pentru **orice** impedanță pasivă a sarcinii și sursei
- **Stabilitatea condiționată:** circuitul este condiționat stabil dacă  $|\Gamma_{in}| < 1$  și  $|\Gamma_{out}| < 1$  doar pentru un anumit interval de valori pentru impedanța pasivă a sarcinii și sursei

# Conditii analitice de stabilitate neconditionata

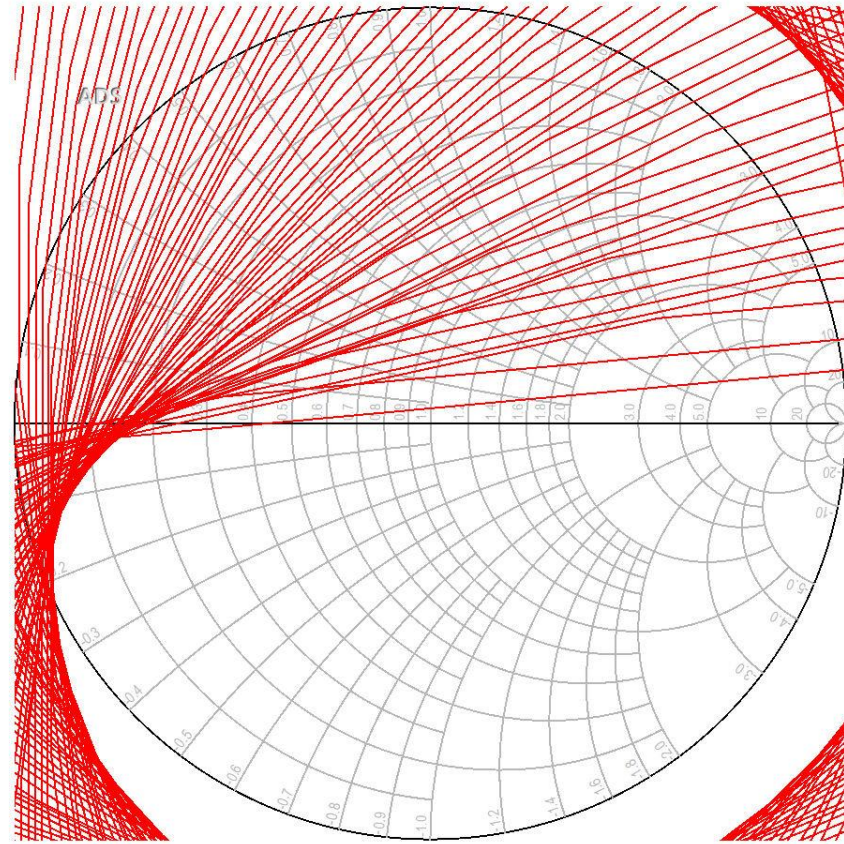
- Utile pentru analiza de banda larga
- Stabilitatea nu e suficient sa fie apreciata doar la frecventele de lucru
  - e necesar sa avem stabilitate pentru  $\Gamma_L$  si  $\Gamma_S$  alese la **orice** frecventa

# Cercuri in banda larga

CSIN



CSOUT



# Conditia Rollet

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2 \cdot |S_{12} \cdot S_{21}|}$$

$$\Delta = S_{11} \cdot S_{22} - S_{12} \cdot S_{21}$$

- Diportul este **neconditionat stabil** daca:
- Sunt indeplinite simultan conditiile
  - $K > 1$
  - $|\Delta| < 1$
- Sunt valabile si conditiile implicite
  - $|S_{11}| < 1$
  - $|S_{22}| < 1$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2 \cdot |S_{12} \cdot S_{21}|} > 1$$

$$|\Delta| = |S_{11} \cdot S_{22} - S_{12} \cdot S_{21}| < 1$$

# Criteriul $\mu$

- Conditia Rollet depinde de doi parametri,  $K$  si  $\Delta$ , si nu poate fi utilizata pentru compararea stabilitatii a doua scheme

$$\mu = \frac{1 - |S_{11}|^2}{|S_{22} - \Delta \cdot S_{11}^*| + |S_{12} \cdot S_{21}|} > 1$$

- Diportul este **neconditionat stabil** daca:
  - $\mu > 1$
- Sunt valabile si conditiile implicite
  - $|S_{11}| < 1$
  - $|S_{22}| < 1$
- In plus se poate spune ca daca  $\mu$  creste se obtine stabilitate mai buna
  - $\mu$  este distanta de la centrul diagramei Smith la cercul de stabilitate la iesire

# Criteriul $\mu'$

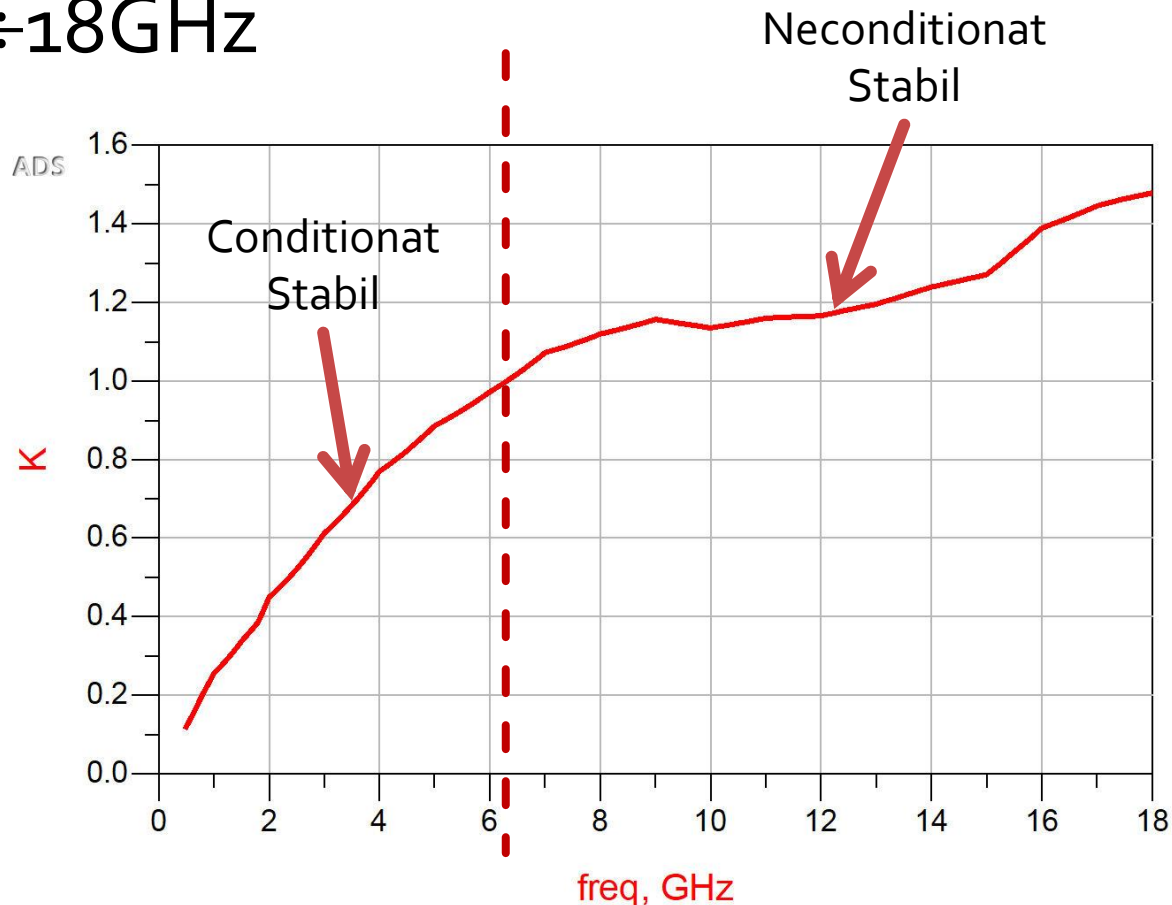
- Parametru dual pentru  $\mu$ , determinat relativ la cercul de stabilitate la intrare

$$\mu' = \frac{1 - |S_{22}|^2}{|S_{11} - \Delta \cdot S_{22}^*| + |S_{12} \cdot S_{21}|} > 1$$

- Diportul este **neconditionat stabil** daca:
  - $\mu' > 1$
- Sunt valabile si conditiile implicite
  - $|S_{11}| < 1$
  - $|S_{22}| < 1$
- In plus se poate spune ca daca  $\mu'$  creste se obtine stabilitate mai buna
  - $\mu'$  este distanta de la centrul diagramei Smith la cercul de stabilitate la intrare

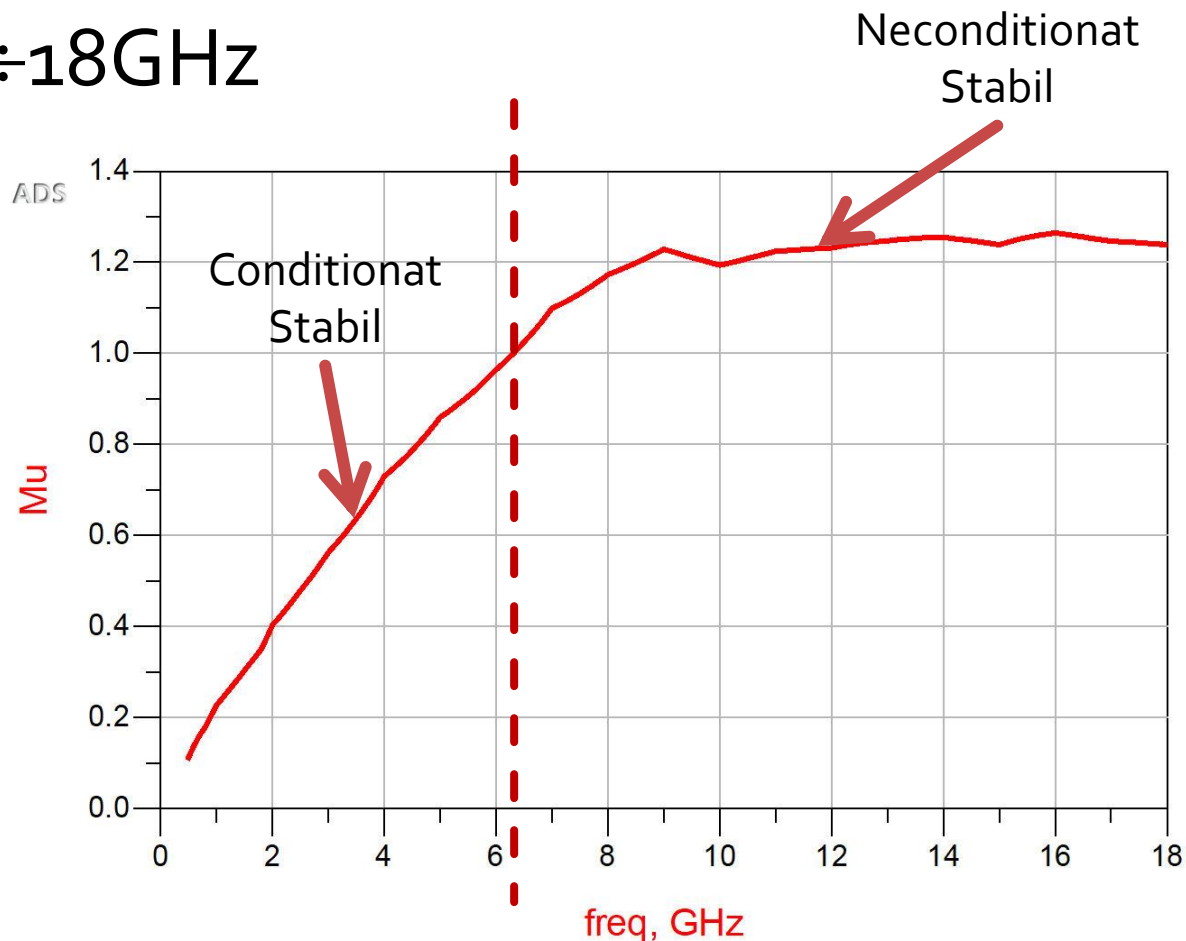
# Conditia Rollet

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @0.5÷18GHz



# Criteriul $\mu$

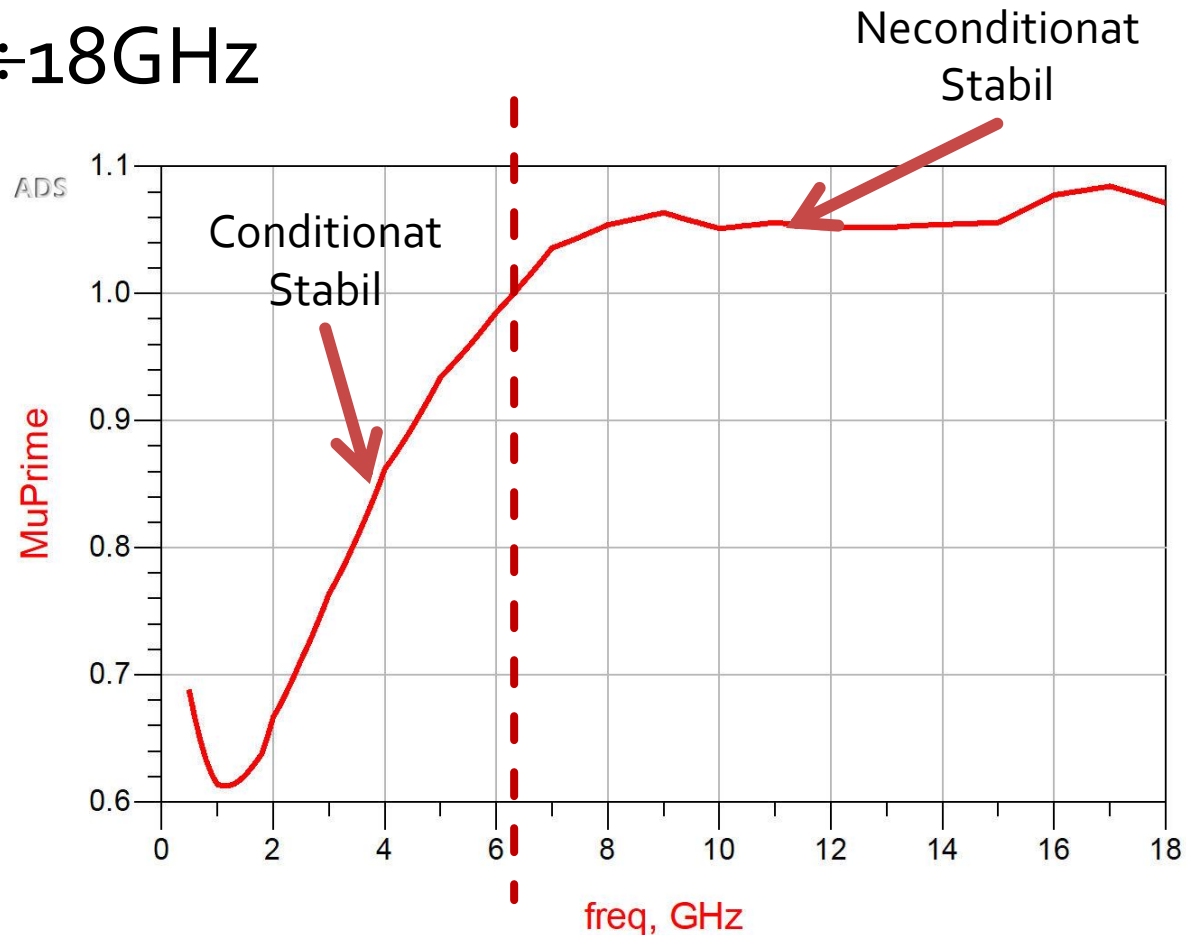
- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @0.5÷18GHz





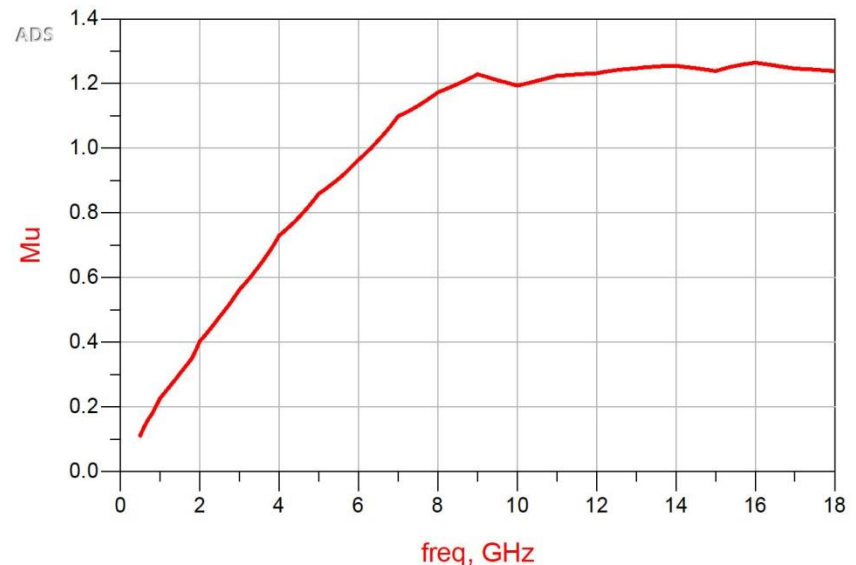
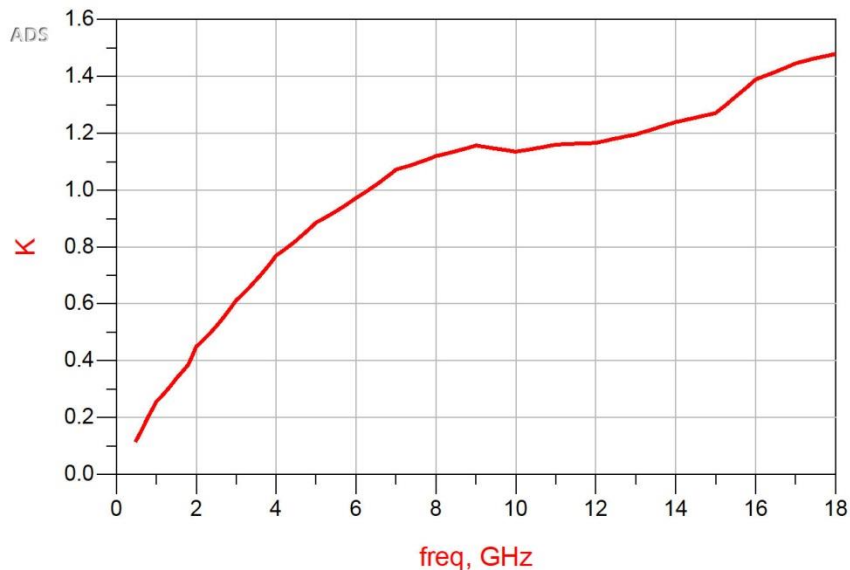
# Criteriul $\mu'$

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @0.5÷18GHz



# Stabilitate

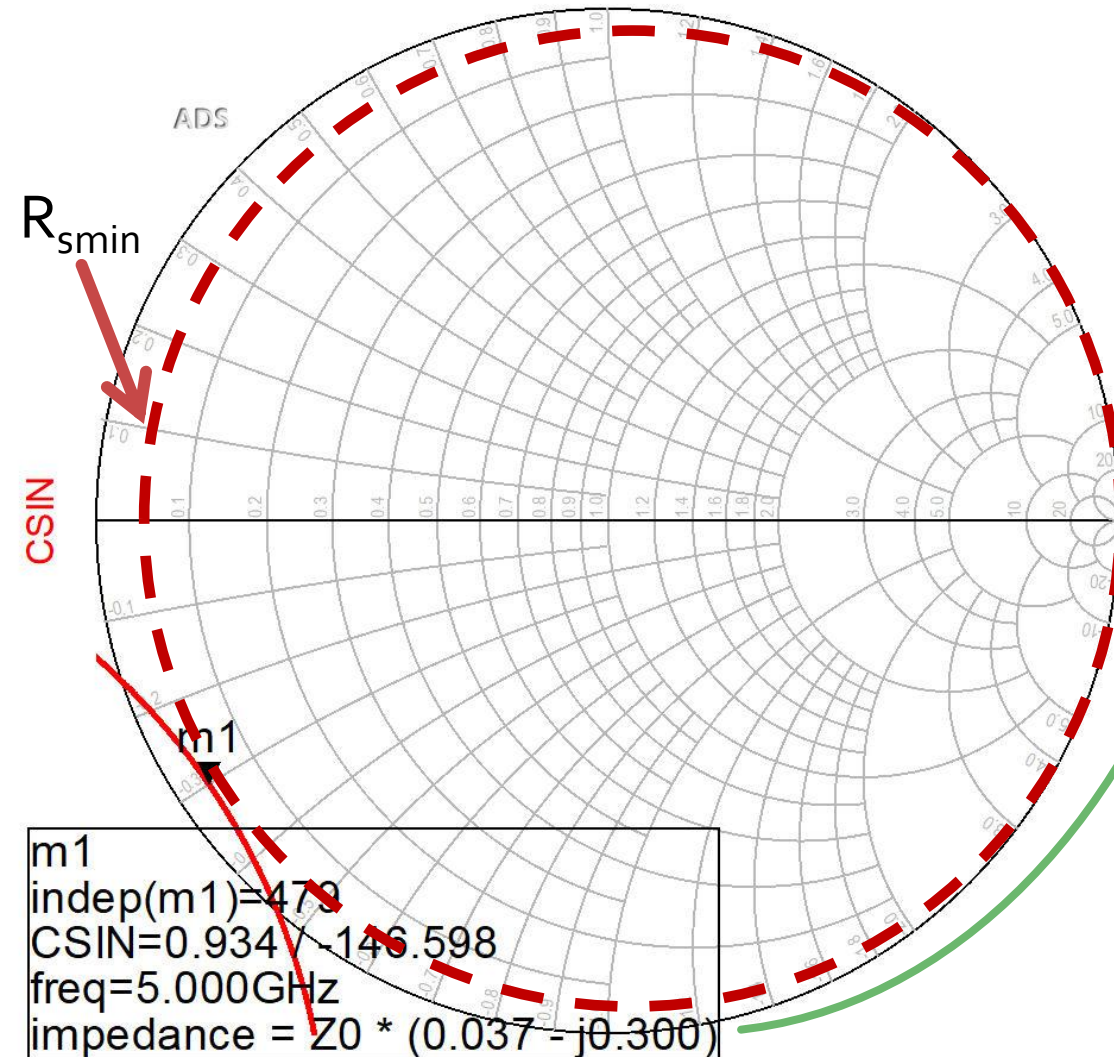
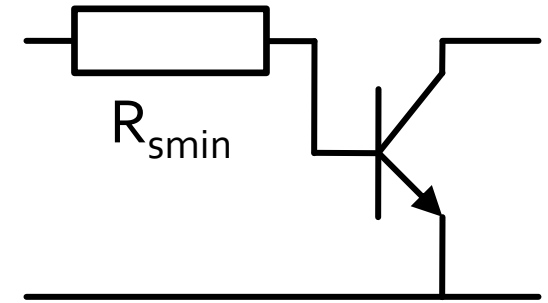
- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @0.5÷18GHz
- Neconditionat stabil pentru  $f > 6.31GHz$



# Stabilizarea unui diport

- Stabilitatea neconditionata pentru un interval larg de frecvente are avantaje importante
  - Ex: pot proiecta cu ATF 34143 un amplificator stabil (conditionat) la 5GHz, dar acest lucru este inutil daca apar oscilatii la 500MHz ( $\mu \approx 0.1$ )
  - **Minimul necesar** in conditii de lucru cu stabilitate conditionata este **sa se verifice stabilitatea** la frecvente inafara benzii
- Stabilitatea neconditionata poate fi fortata prin introducerea de elemente rezistive in serie/paralel la intrare si/sau iesire

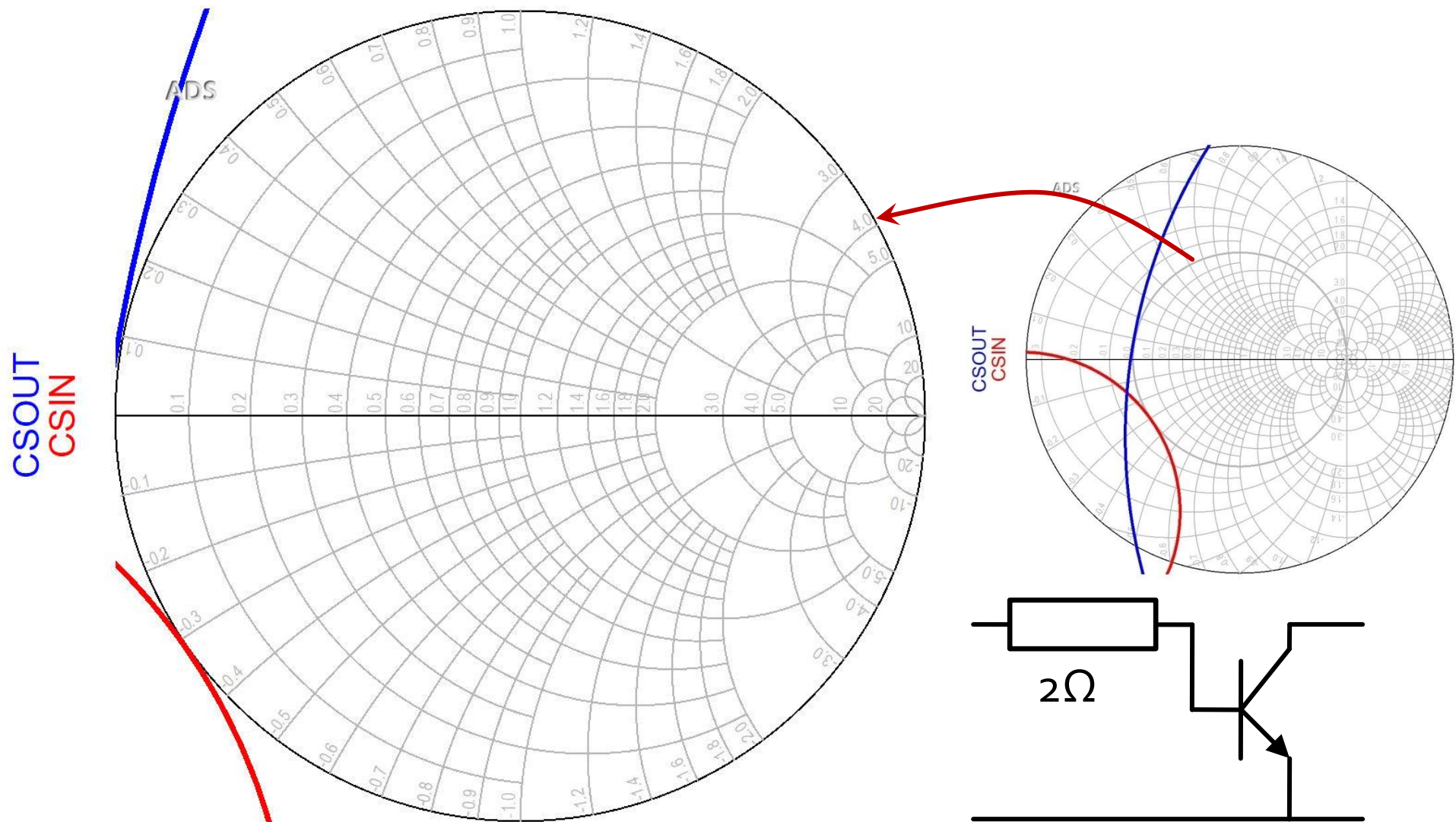
# Rezistentă serie la intrare



$$z = 0.037 - j \cdot 0.3$$

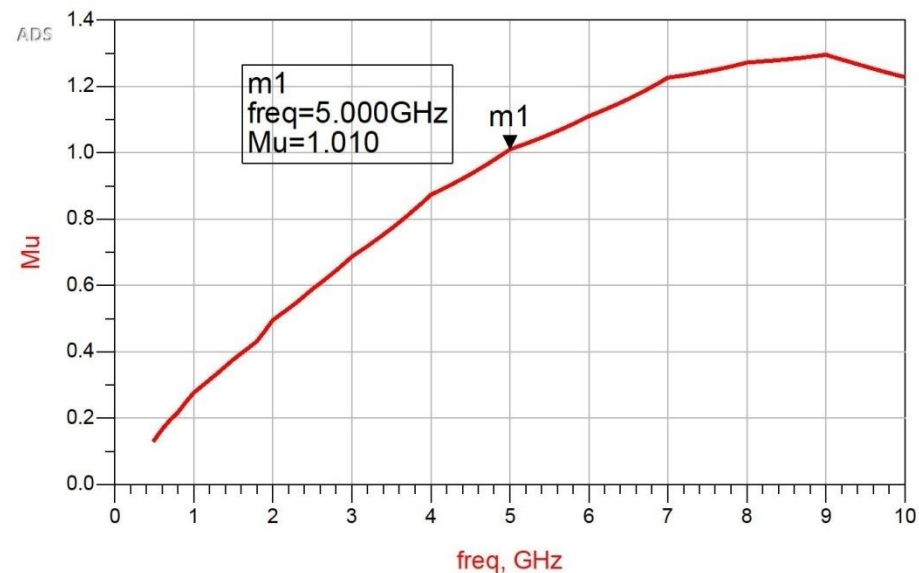
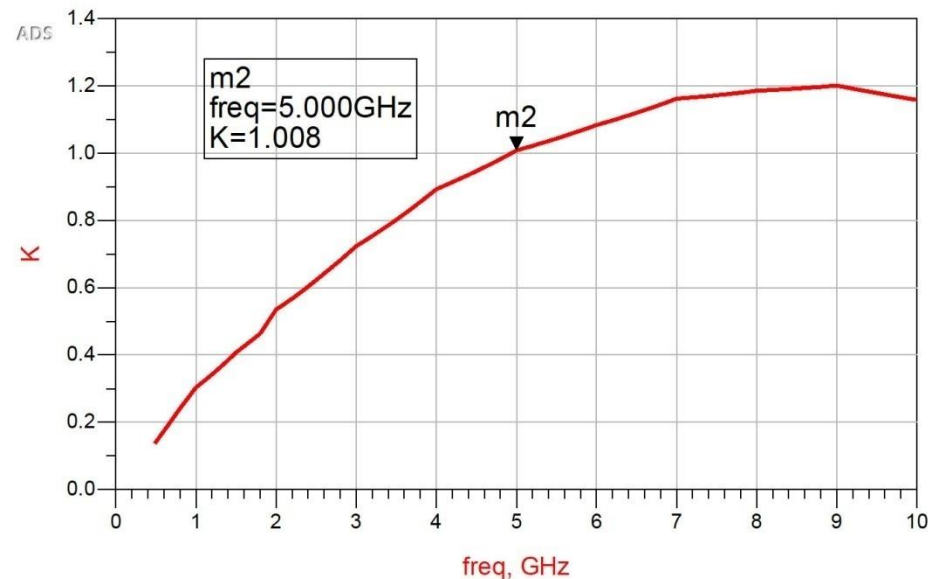
$$R_{smin} = 0.037 \cdot 50\Omega = 1.85\Omega$$

# ADS, $R_s = 2\Omega$



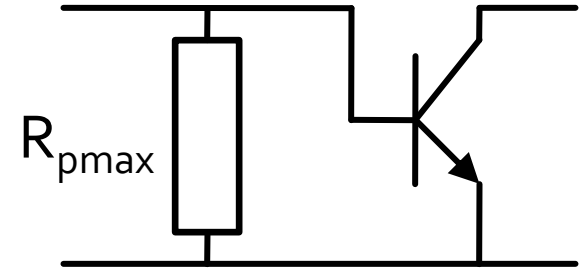
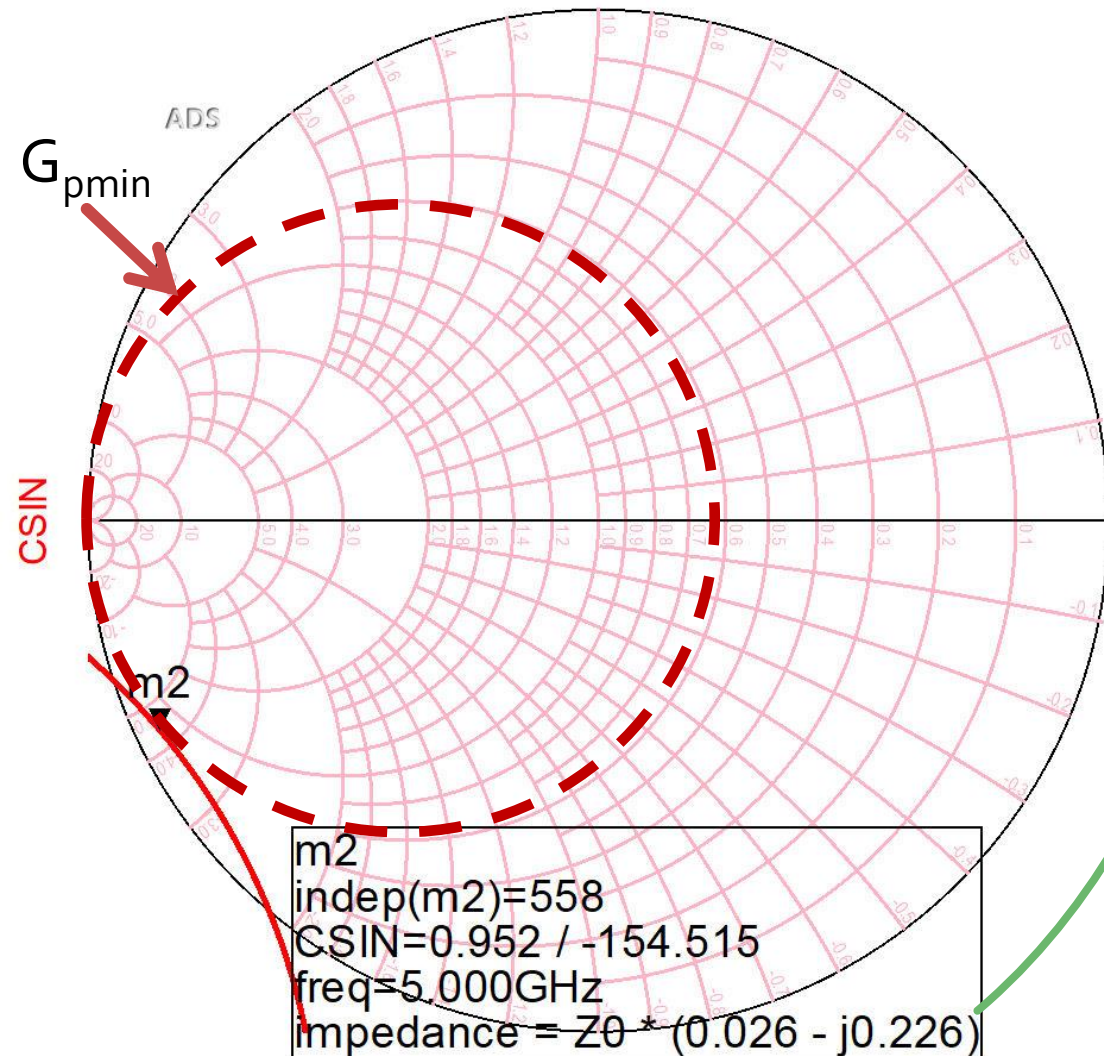
# Rezistentă serie la intrare

- $R_s = 2\Omega$
- $K = 1.008$ ,  $MAG = 13.694\text{dB}$  @ 5GHz
  - fara stabilizare,  $K = 0.886$ ,  $MAG = 14.248\text{dB}$  @ 5GHz





# Rezistentă paralel la intrare



$$R_{pmax} = \frac{1}{G_{pmin}}$$

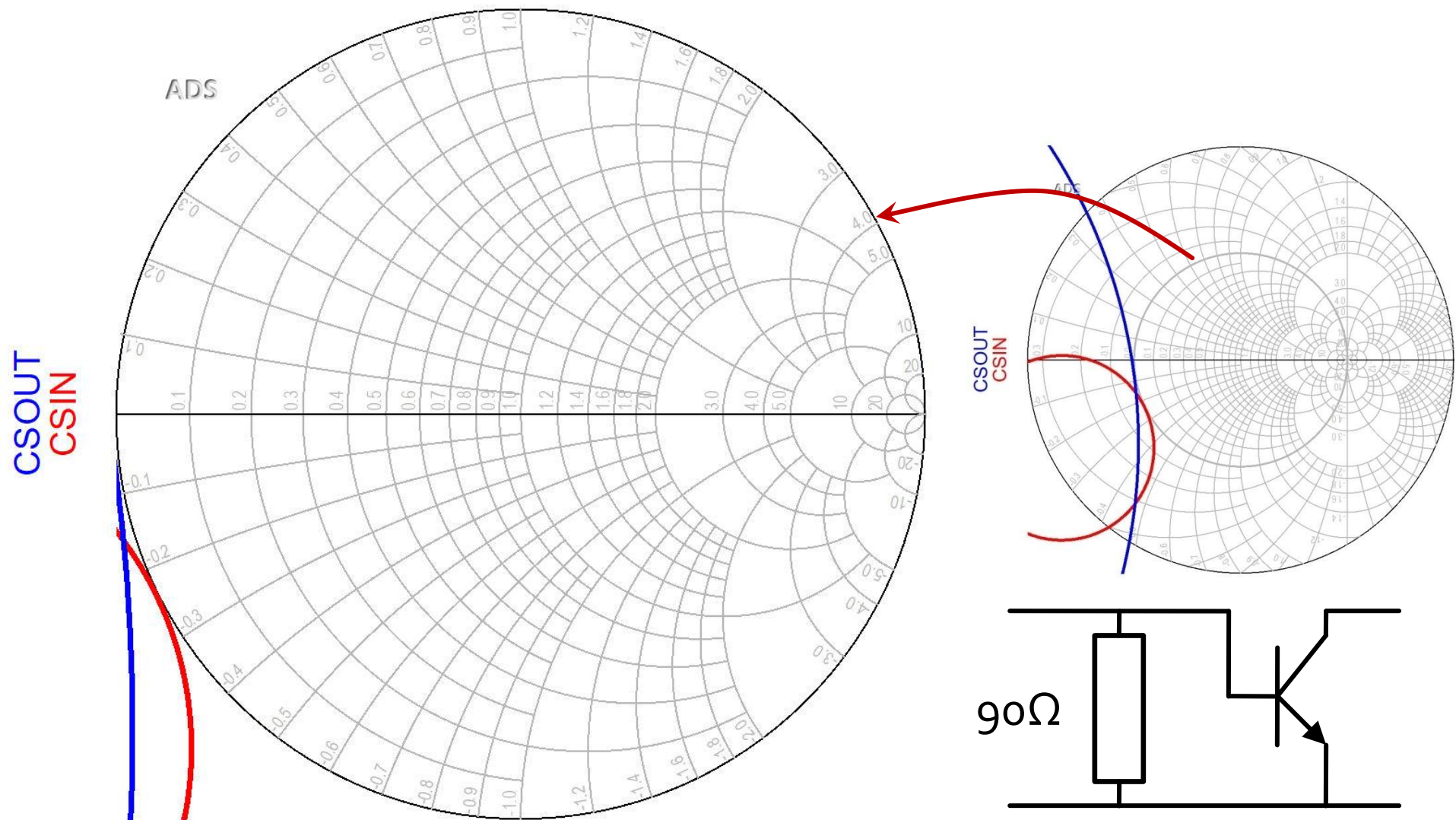
$$z = 0.026 - j \cdot 0.226$$

$$y = \frac{1}{z} = \frac{1}{0.026 - j \cdot 0.226}$$

$$y = 0.502 + j \cdot 4.367$$

$$R_{pmax} = \frac{50\Omega}{0.502} = 99.6\Omega$$

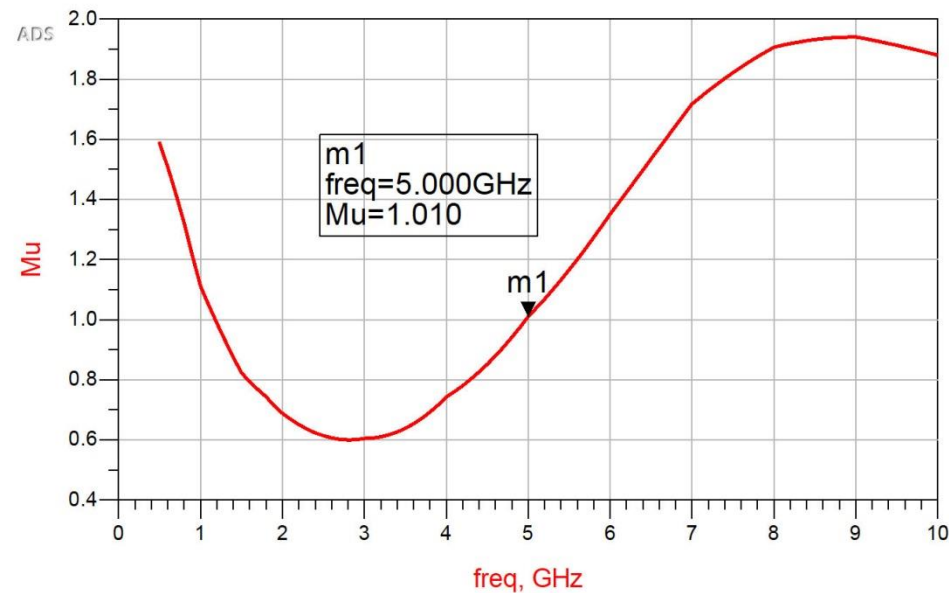
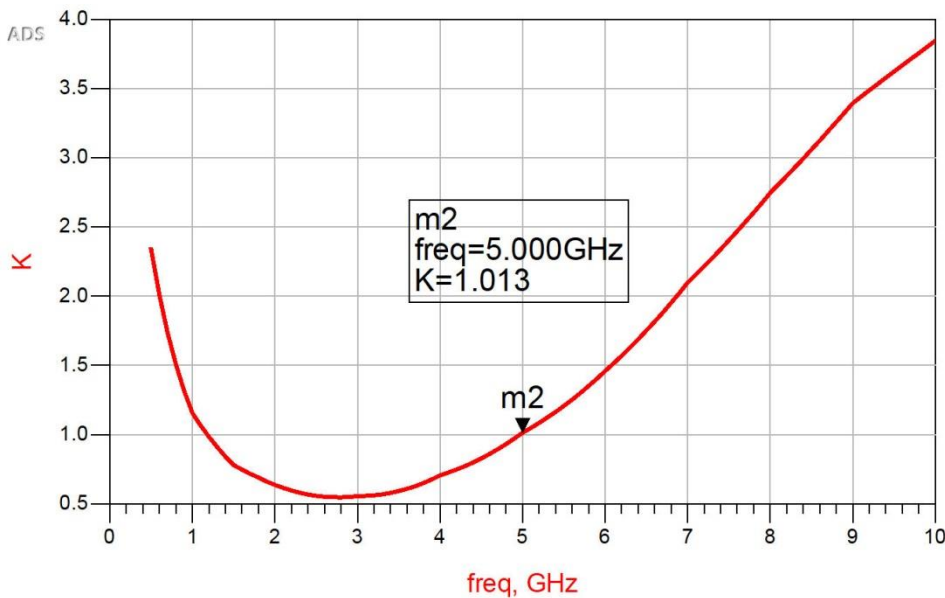
# ADS, $R_p = 90\Omega$





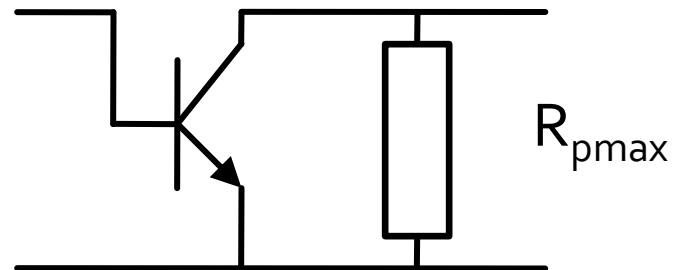
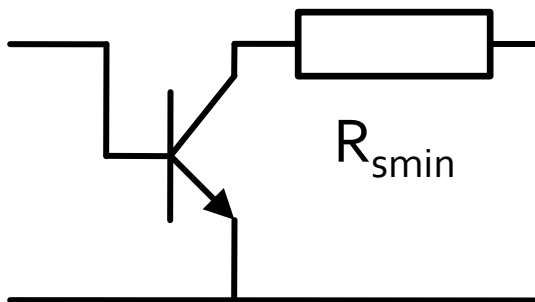
# Rezistentă paralel la intrare

- $R_p = 90\Omega$
- $K = 1.013$ ,  $MAG = 13.561\text{dB}$  @ 5GHz
  - fara stabilizare,  $K = 0.886$ ,  $MAG = 14.248\text{dB}$  @ 5GHz



# Rezistenta serie/paralel la iesire

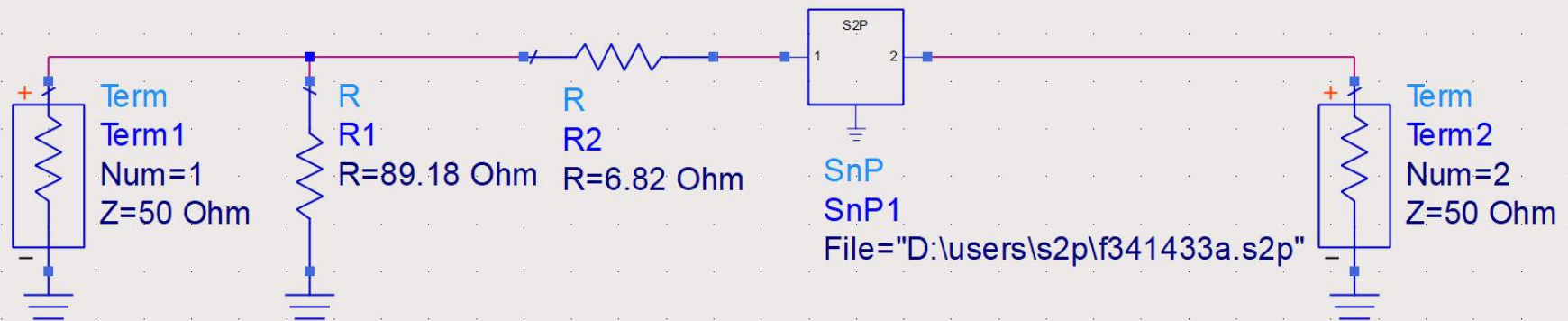
- Procedura se poate aplica similar la iesire (plecand de la CSOUT)
- Din exemplele anterioare, incarcarea rezistiva la intrare are efect pozitiv si asupra stabilitatii la iesire si viceversa (incarcare la iesire efect asupra stabilitatii la intrare)



# Stabilizarea unui diport

- Efect negativ asupra castigului
  - trebuie urmarit MAG/MSG in timpul proiectarii
- Efect negativ asupra zgomotului (va urma)
- Se poate alege una din cele 4 variante care ofera performante mai bune (in functie de aplicatie)
- Se pot realiza cu elemente de pasivizare selective in frecventa
  - Ex: Circuite RL, RC sacrifica performanta doar unde este necesar sa se imbunatateasca stabilitatea fara afectarea frecventelor la care dispozitivul e deja stabil
- E posibil ca aceste efecte sa apara automat ca urmare a elementelor parazite ale circuitelor de polarizare (capacitati de decuplare, socuri de radiofrecventa)

# Stabilizarea unui diport



S-PARAMETERS

S\_Param

SP1

Start=0.5 GHz

Stop=10.0 GHz

Step=0.1 GHz

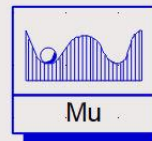


MaxGain

MaxGain

MAG

MAG=max\_gain(S)

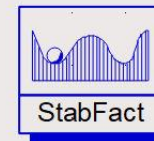


Mu

Mu

Mu1

Mu=mu(S)



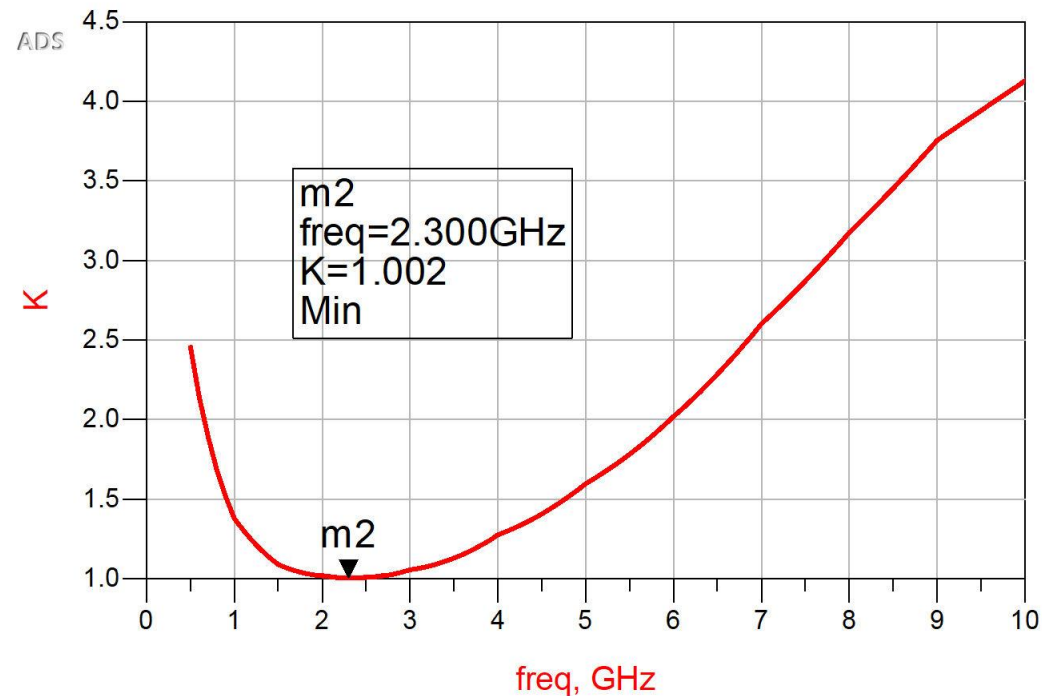
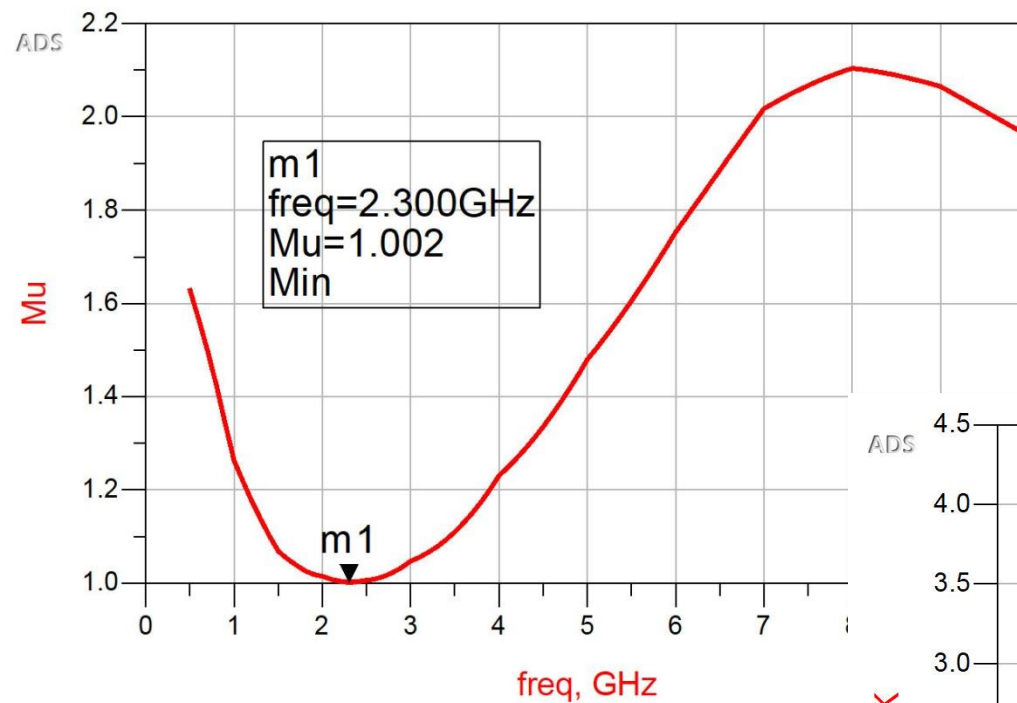
StabFact

StabFact

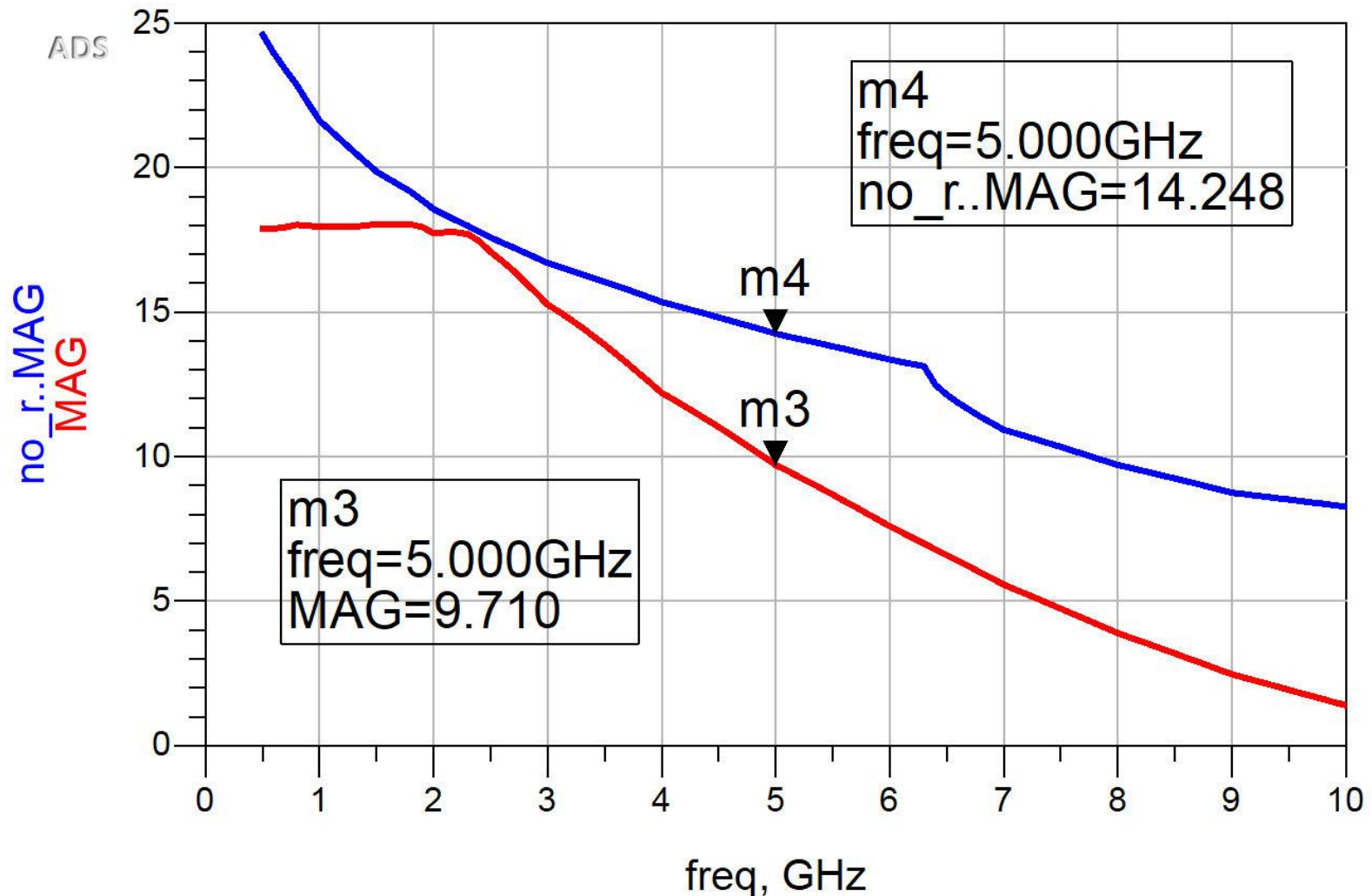
K

K=stab\_fact(S)

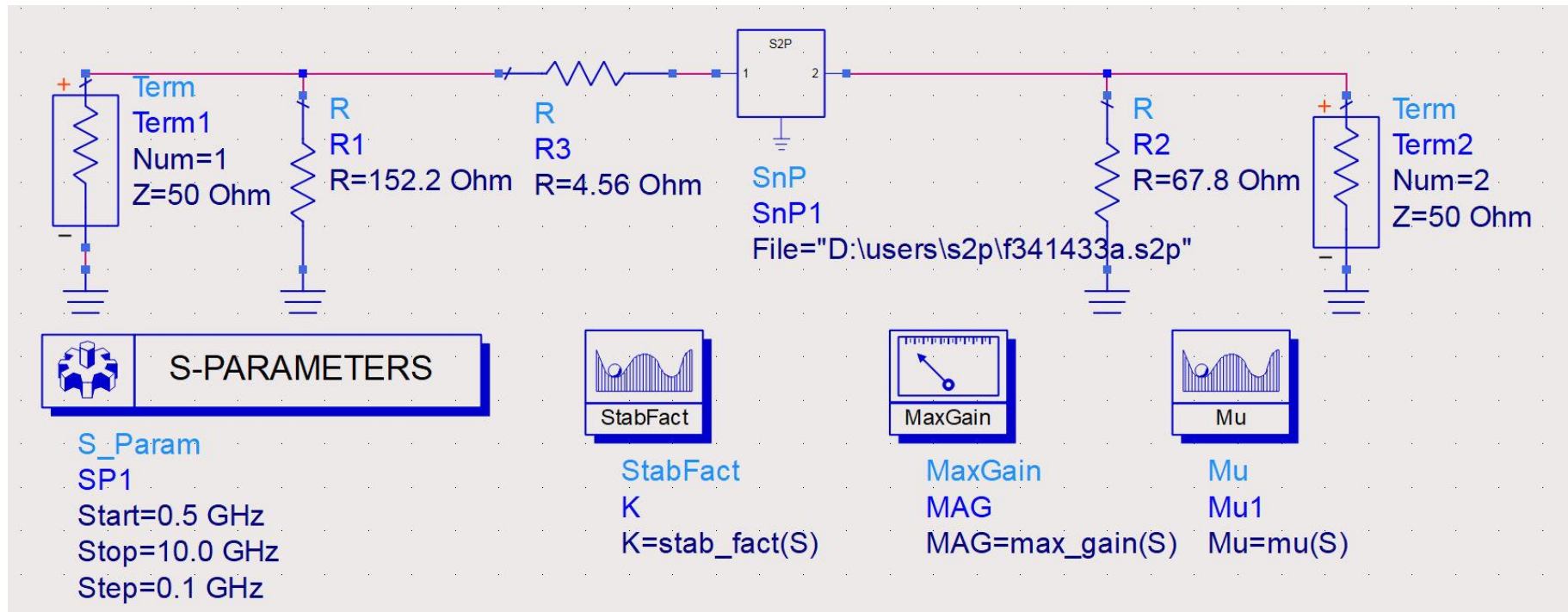
# Stabilizarea unui diport



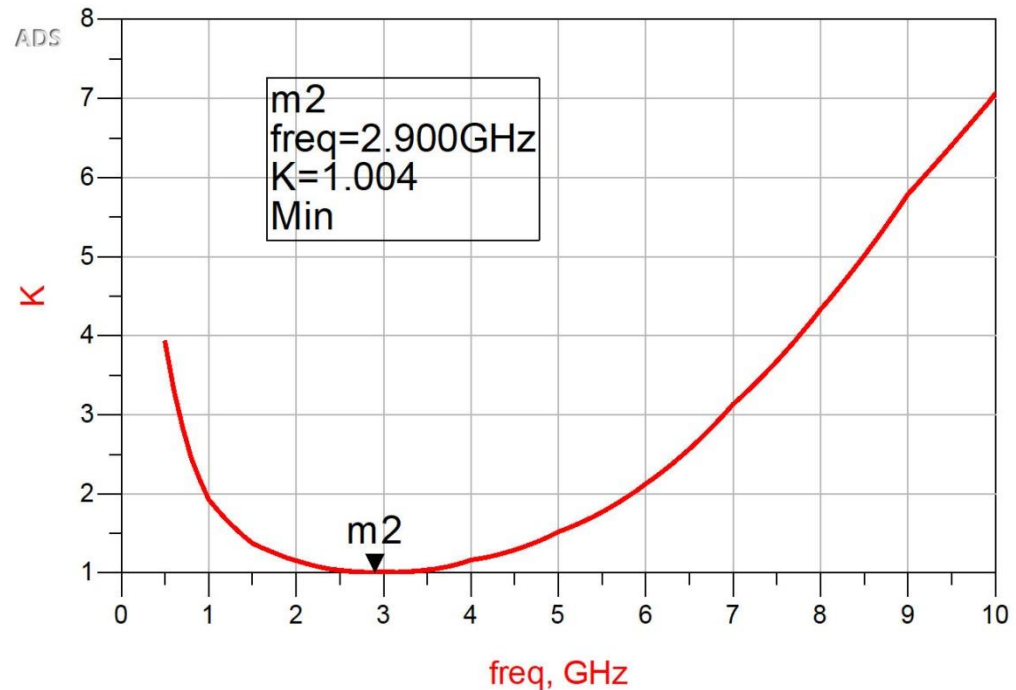
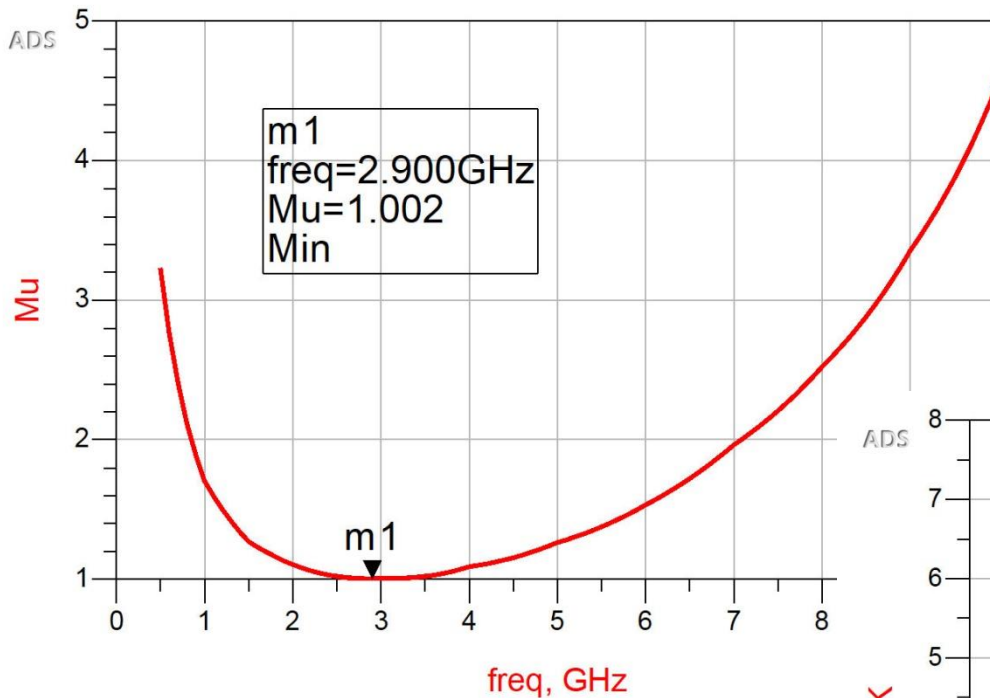
# Stabilizarea unui diport



# Stabilizarea unui diport

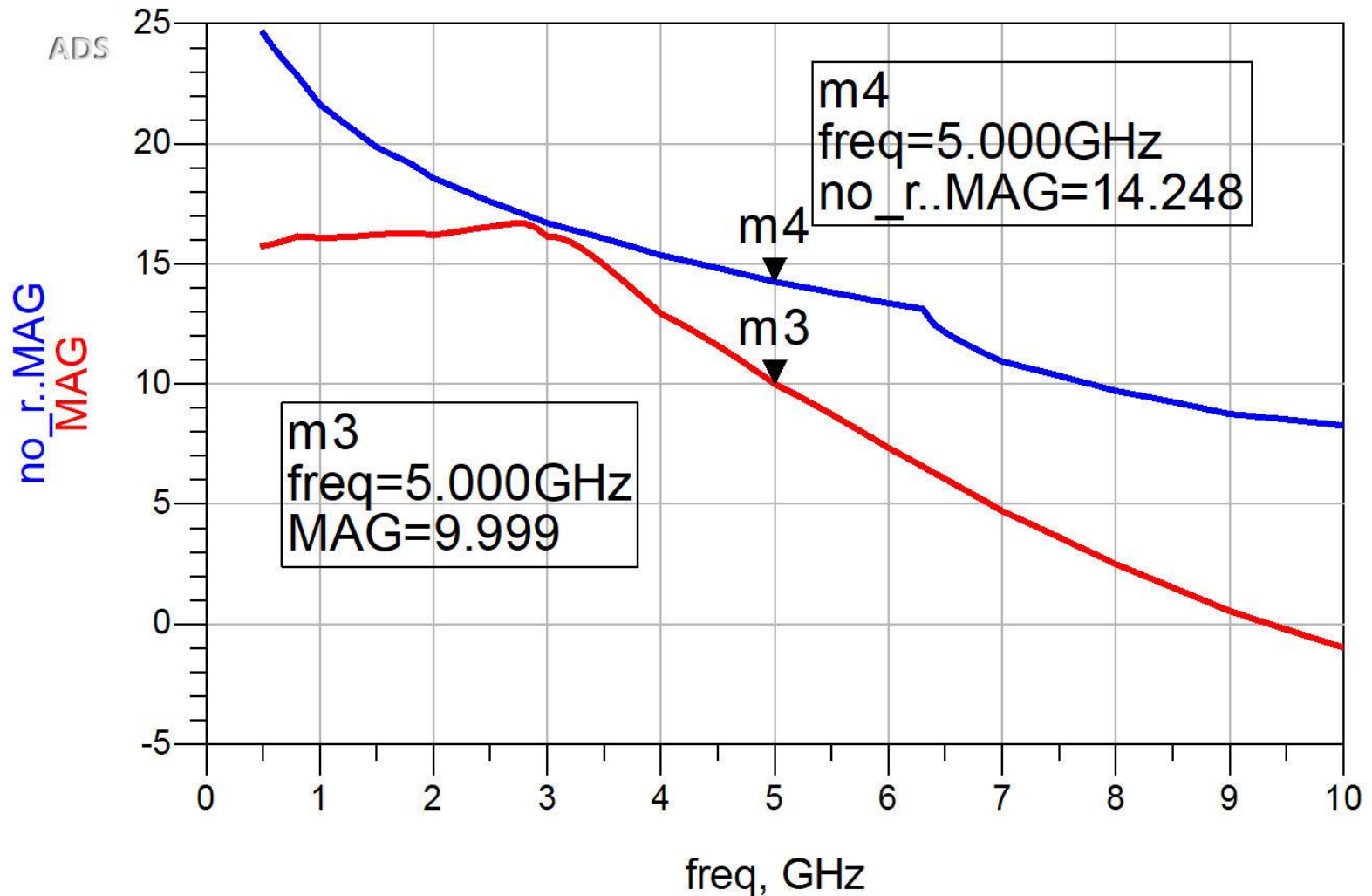


# Stabilizarea unui diport





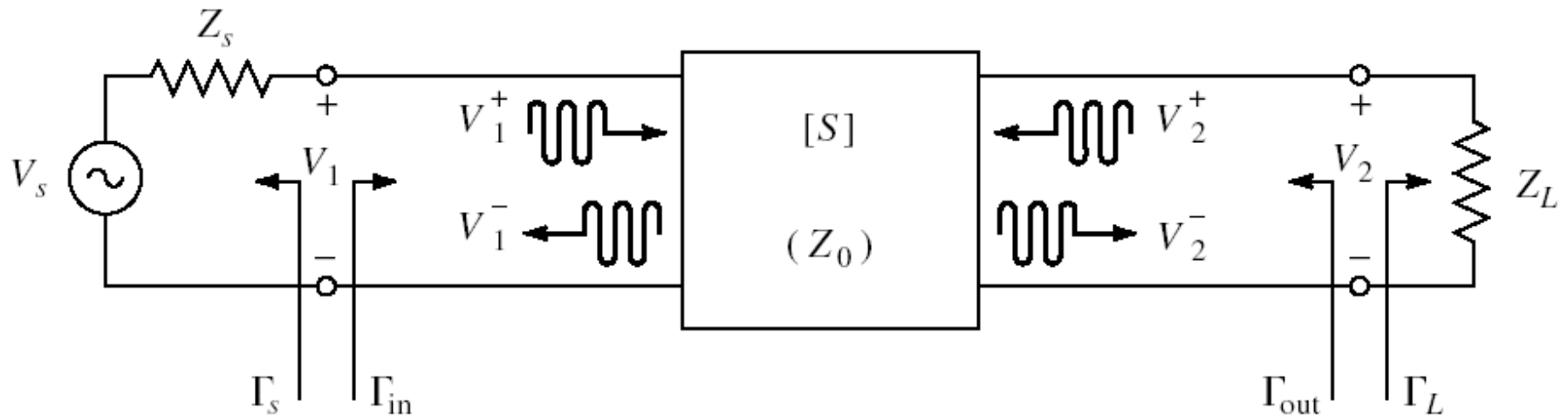
# Stabilizarea unui diport



Amplificatoare de microunde

# Castigul amplificatoarelor de microunde

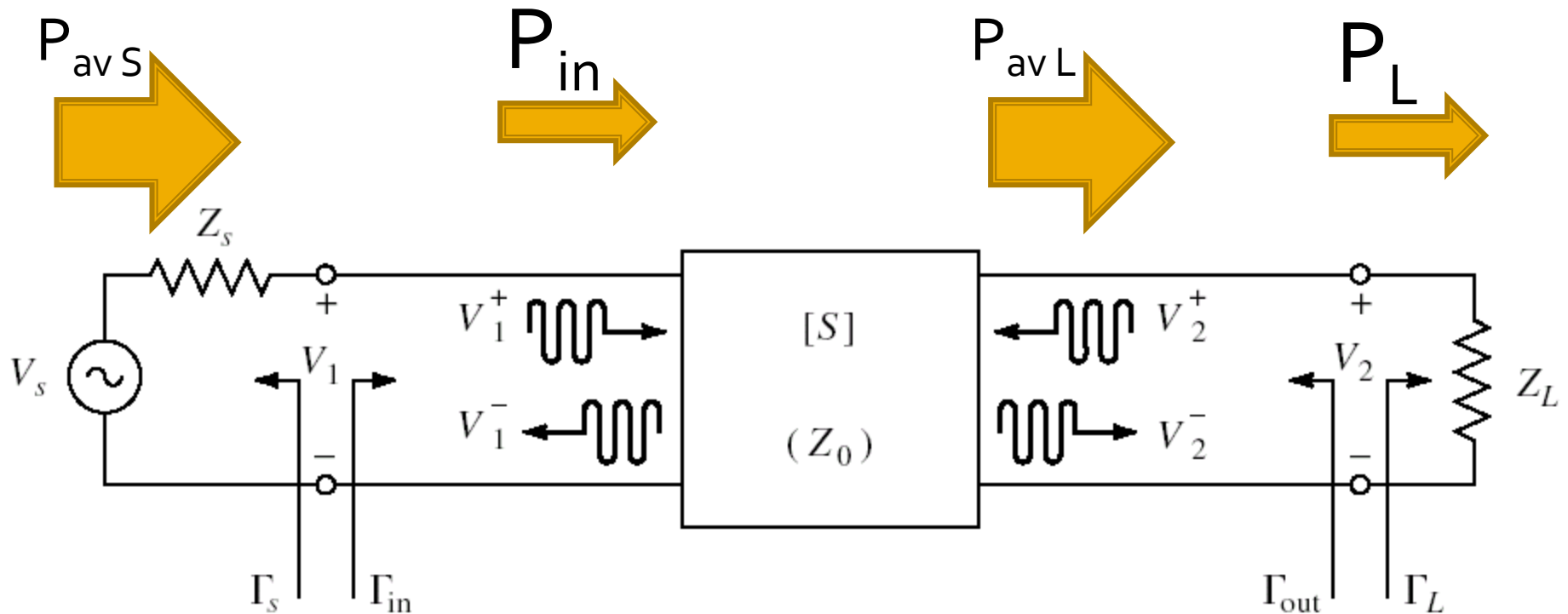
# Cuadripol Amplificator



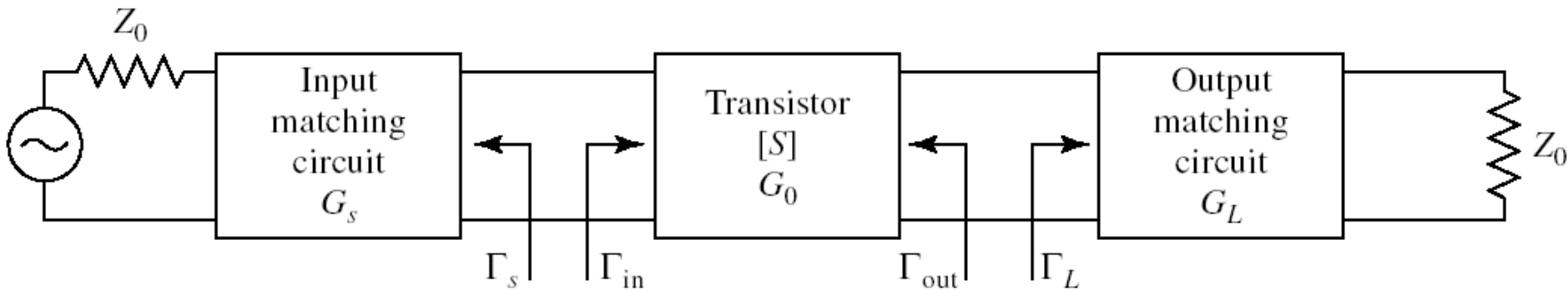
- marimi care intereseaza:
  - stabilitate
  - **castig de putere**
  - zgomot (uneori – semnal mic)
  - liniaritate (uneori – semnal mare)

# Puteri / Adaptare

- Doua porturi in care adaptarea influenteaza transferul de putere



# Proiectare pentru castig maxim



- Castig maxim de putere se obtine cand

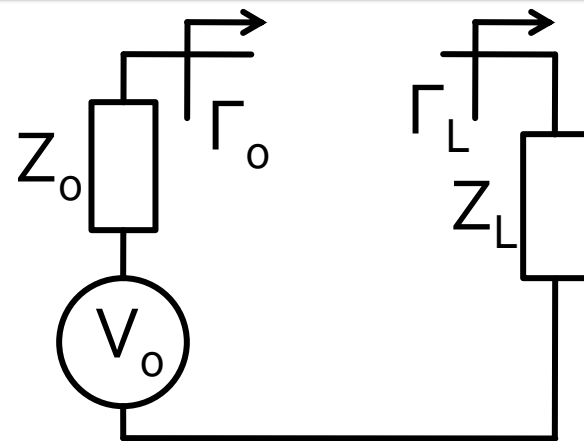
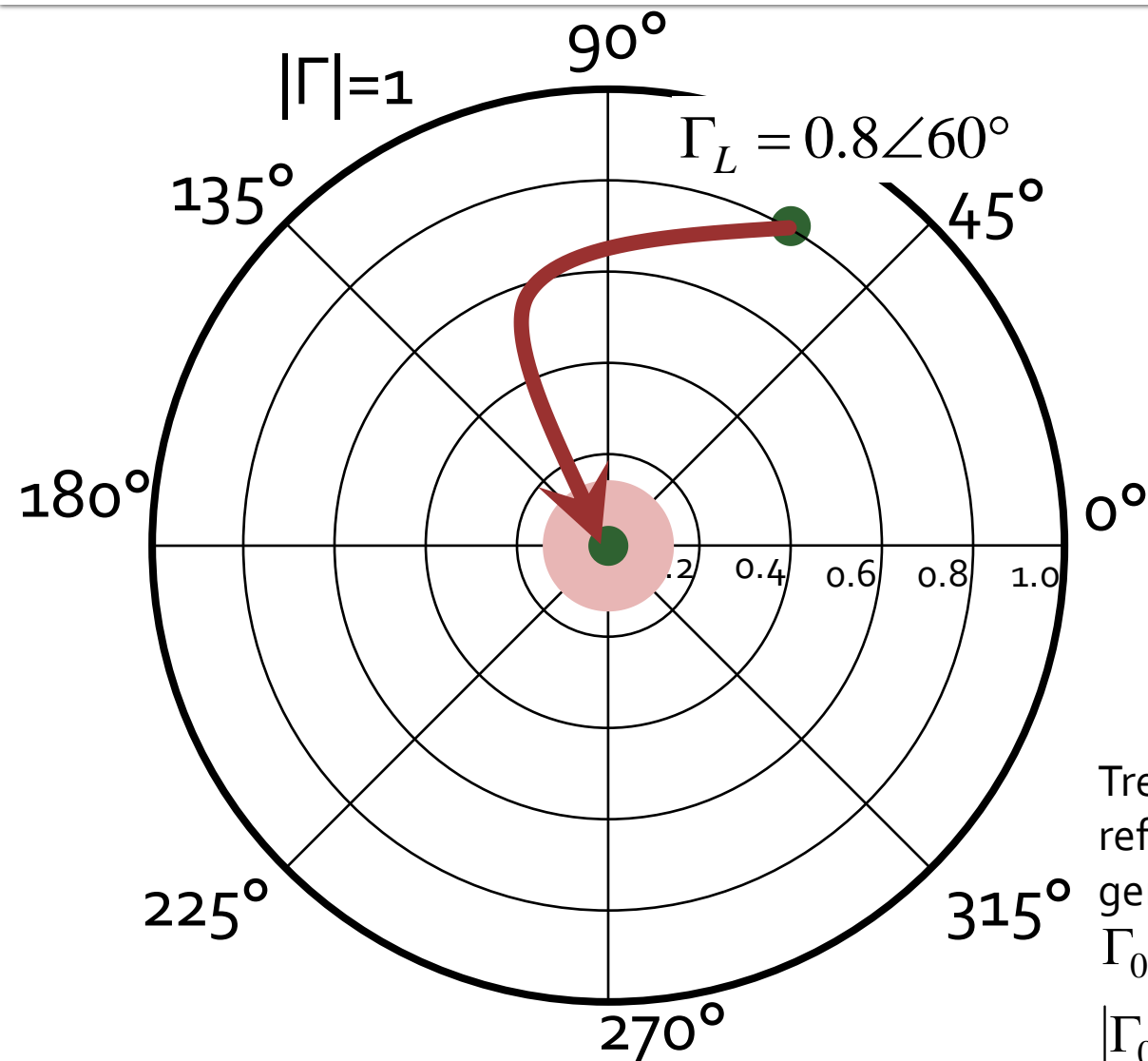
$$\rightarrow \Gamma_{in} = \Gamma_s^* \quad \Gamma_{out} = \Gamma_L^*$$

- Pentru retele de adaptare fara pierderi

$$G_{T \max} = \frac{|S_{21}|^2 \cdot (1 - |\Gamma_s|^2) \cdot (1 - |\Gamma_L|^2)}{|1 - \Gamma_s \cdot \Gamma_{in}|^2 \cdot |1 - S_{22} \cdot \Gamma_L|^2} \quad G_{T \max} = \frac{1}{1 - |\Gamma_s|^2} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

- Pentru tranzistor bilateral ( $S_{12} \neq 0$ )  $\Gamma_{in}$  si  $\Gamma_{out}$  se influenteaza reciproc deci adaptarea trebuie sa fie simultana

# Diagrama Smith, adaptare, $Z_L \neq Z_o$



Adaptare  $Z_L$  la  $Z_o$ . Se raporteaza  $Z_L$  la  $Z_o$

$$Z_L = 21.429\Omega + j \cdot 82.479\Omega$$

$$z_L = 0.429 + j \cdot 1.65$$

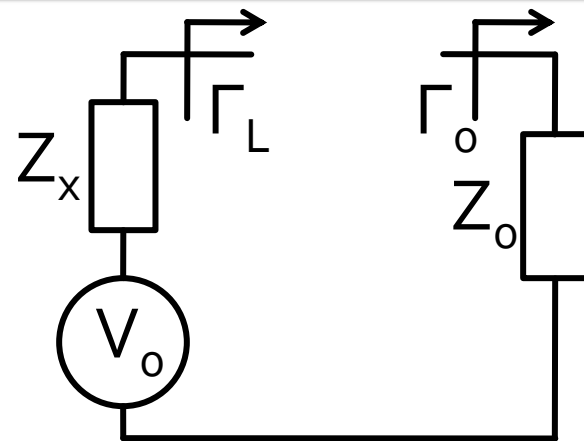
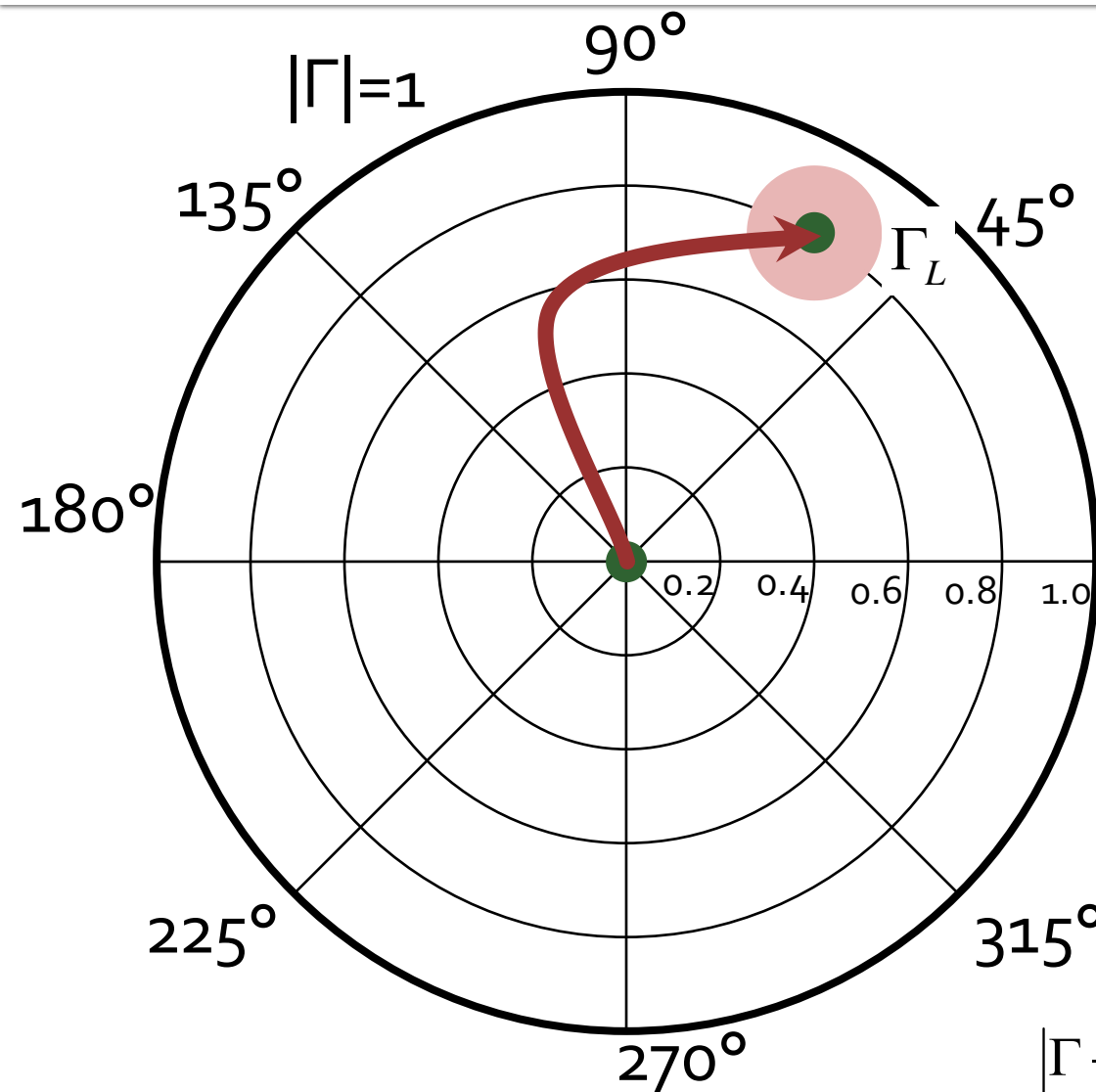
$$\Gamma_L = 0.8 \angle 60^\circ$$

Trebuie sa deplasez coeficientul de reflexie in zona in care pentru generator cu  $Z_o$  am:

$\Gamma_0 = 0$  adaptare perfecta ●

$|\Gamma_0| \leq \Gamma_m$  adaptare "suficienta" ●

# Diagrama Smith, adaptare, $Z_L = Z_o$



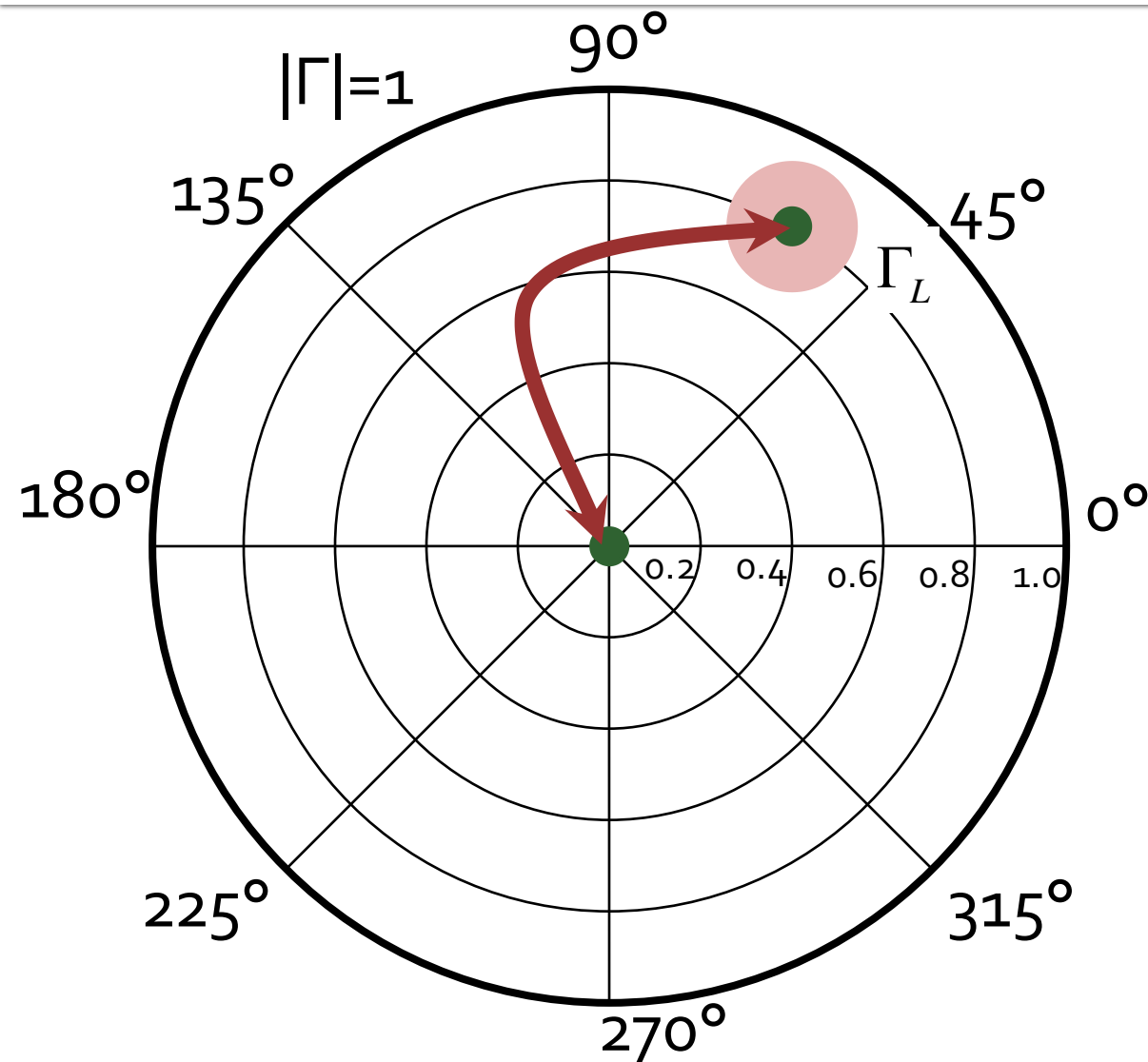
0° Sursa (de ex. tranzistorul) cu  $Z_x$  are nevoie de un anumit coeficient de reflexie  $\Gamma_L$  pentru a funcționa corect

Circuitul de adaptare trebuie să deplaseze coeficientul de reflexie văzut spre sarcină în zona în care pentru sarcină  $Z_o$  ( $\Gamma_o=0$ ) am:

$\Gamma = \Gamma_L$  adaptare perfectă ●

$|\Gamma - \Gamma_L| \leq \Gamma_m$  adaptare "suficientă" ●

# Diagrama Smith, adaptare, $Z_L = Z_o$



- Circuitele de adaptare care muta
  - $\Gamma_L$  in  $\Gamma_o$
  - $\Gamma_o$  in  $\Gamma_L$
- sunt **identice** ca realizare. Diferă doar prin **ordine** în care se introduc elementele în circuitul de adaptare
- Ca urmare se pot folosi în proiectarea circuitelor de adaptare aceleași:
  - **metode**
  - **relatii**



# Adaptare simultana

$$\rightarrow \Gamma_{in} = \Gamma_S^*$$

$$\Gamma_{in} = S_{11} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_L}{1 - S_{22} \cdot \Gamma_L}$$

$$\Gamma_S^* = S_{11} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_L}{1 - S_{22} \cdot \Gamma_L}$$

$$\rightarrow \Gamma_{out} = \Gamma_L^*$$

$$\Gamma_{out} = S_{22} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_S}{1 - S_{11} \cdot \Gamma_S}$$

$$\Gamma_L^* = S_{22} + \frac{S_{12} \cdot S_{21} \cdot \Gamma_S}{1 - S_{11} \cdot \Gamma_S}$$

## ■ Aflam $\Gamma_S$

$$\Gamma_S = S_{11}^* + \frac{S_{12}^* \cdot S_{21}^*}{1/\Gamma_L^* - S_{22}^*}$$

$$\Gamma_L^* = \frac{S_{22} - \Delta \cdot \Gamma_S}{1 - S_{11} \cdot \Gamma_S}$$

$$\Gamma_S \cdot (1 - |S_{22}|^2) + \Gamma_S^2 \cdot (\Delta \cdot S_{22}^* - S_{11}) = \Gamma_S \cdot (\Delta \cdot S_{11}^* \cdot S_{22}^* - |S_{22}|^2 - \Delta \cdot S_{12}^* \cdot S_{21}^*) + S_{11}^* \cdot (1 - |S_{22}|^2) + S_{12}^* \cdot S_{21}^* \cdot S_{22}$$

# Adaptare simultana

$$\Delta \cdot (S_{11}^* \cdot S_{22}^* - S_{12}^* \cdot S_{21}^*) = |\Delta|^2$$

$$\Gamma_S^2 \cdot \underbrace{(S_{11} - \Delta \cdot S_{22}^*)}_C + \Gamma_S \cdot \underbrace{(|\Delta|^2 - |S_{11}|^2 + |S_{22}|^2 - 1)}_{-B} + \underbrace{(S_{11}^* - \Delta^* \cdot S_{22})}_{C^*} = 0$$

- Ecuatie de gradul 2

$$\Gamma_S = \frac{B_1 \pm \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

- Similar

$$\Gamma_L = \frac{B_2 \pm \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

- Cu variabilele

$$\begin{cases} B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2 \\ C_1 = S_{11} - \Delta \cdot S_{22}^* \end{cases} \quad \begin{cases} B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 \\ C_2 = S_{22} - \Delta \cdot S_{11}^* \end{cases}$$

# Adaptare simultana

- Este posibila daca

$$B_1^2 - 4 \cdot |C_1|^2 > 0 \quad B_2^2 - 4 \cdot |C_2|^2 > 0$$

$$\Delta \cdot (S_{11}^* \cdot S_{22}^* - S_{12}^* \cdot S_{21}^*) = |\Delta|^2$$

$$|C_1|^2 = |S_{11} - \Delta \cdot S_{22}^*|^2 = |S_{12}|^2 \cdot |S_{21}|^2 + (1 - |S_{22}|^2) \cdot (|S_{11}|^2 - |\Delta|^2)$$

$$B_1^2 - 4 \cdot |C_1|^2 = (1 + |S_{11}|^2)^2 + (|S_{22}|^2 + |\Delta|^2)^2 - \\ - 2 \cdot (1 + |S_{11}|^2) \cdot (|S_{22}|^2 + |\Delta|^2) - 4 \cdot |S_{12} \cdot S_{21}|^2 - 4 \cdot (1 - |S_{22}|^2) \cdot (|S_{22}|^2 - |\Delta|^2)$$

$$B_1^2 - 4 \cdot |C_1|^2 = (1 + |S_{11}|^2)^2 + (|S_{22}|^2 + |\Delta|^2)^2 - \\ - 4 \cdot |S_{11}|^2 - 4 \cdot |S_{22}|^2 \cdot |\Delta|^2 - 2 \cdot (1 - |S_{11}|^2) \cdot (|S_{22}|^2 - |\Delta|^2) - 4 \cdot |S_{12} \cdot S_{21}|^2$$

# Adaptare simultana

$$B_1^2 - 4 \cdot |C_1|^2 = \left(1 + |S_{11}|^2\right)^2 + \left(|S_{22}|^2 + |\Delta|^2\right)^2 - 4 \cdot |S_{11}|^2 - 4 \cdot |S_{22}|^2 \cdot |\Delta|^2 - 2 \cdot \left(1 - |S_{11}|^2\right) \cdot \left(|S_{22}|^2 - |\Delta|^2\right) - 4 \cdot |S_{12} \cdot S_{21}|^2$$

$$B_1^2 - 4 \cdot |C_1|^2 = \left(1 - |S_{11}|^2\right)^2 + \left(|S_{22}|^2 - |\Delta|^2\right)^2 - 2 \cdot \left(1 - |S_{11}|^2\right) \cdot \left(|S_{22}|^2 - |\Delta|^2\right) - 4 \cdot |S_{12} \cdot S_{21}|^2$$

$$B_1^2 - 4 \cdot |C_1|^2 = \left(1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2\right)^2 - 4 \cdot |S_{12} \cdot S_{21}|^2$$

$$B_1^2 - 4 \cdot |C_1|^2 = \left(K \cdot 2 \cdot |S_{12} \cdot S_{21}|\right)^2 - 4 \cdot |S_{12} \cdot S_{21}|^2$$

$$B_1^2 - 4 \cdot |C_1|^2 = 4 \cdot |S_{12}|^2 \cdot |S_{21}|^2 \cdot (K^2 - 1)$$

■ Similar

$$B_2^2 - 4 \cdot |C_2|^2 = 4 \cdot |S_{12}|^2 \cdot |S_{21}|^2 \cdot (K^2 - 1)$$

# Adaptare simultana

$$\Gamma_S = \frac{B_1 \pm \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

$$\Gamma_L = \frac{B_2 \pm \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

## ■ Necesari pentru solutii

$$|\Gamma_S| < 1 \qquad |\Gamma_L| < 1$$

$$|\Delta| = |S_{11} \cdot S_{22} - S_{12} \cdot S_{21}| < 1$$

$$\begin{cases} B_1 > 0 \\ B_2 > 0 \end{cases}$$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2 \cdot |S_{12} \cdot S_{21}|} > 1$$

$$\begin{cases} B_1^2 - 4 \cdot |C_1|^2 = 4 \cdot |S_{12}|^2 \cdot |S_{21}|^2 \cdot (K^2 - 1) > 0 \\ B_2^2 - 4 \cdot |C_2|^2 = 4 \cdot |S_{12}|^2 \cdot |S_{21}|^2 \cdot (K^2 - 1) > 0 \end{cases}$$

# Adaptare simultana

- Adaptarea simultana se poate realiza **numai** pentru amplificatoarele **neconditionat stabile** la frecventa de lucru, si solutia cu  $|\Gamma| < 1$  se obtine cu semnul “-”

$$\Gamma_S = \frac{B_1 - \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

$$\begin{cases} B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2 \\ C_1 = S_{11} - \Delta \cdot S_{22}^* \end{cases}$$

$$\Gamma_L = \frac{B_2 - \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

$$\begin{cases} B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 \\ C_2 = S_{22} - \Delta \cdot S_{11}^* \end{cases}$$

# Adaptare simultana

- In conditiile adaptarii simultane se obtine castigul de transfer maxim pentru tranzistorul bilateral

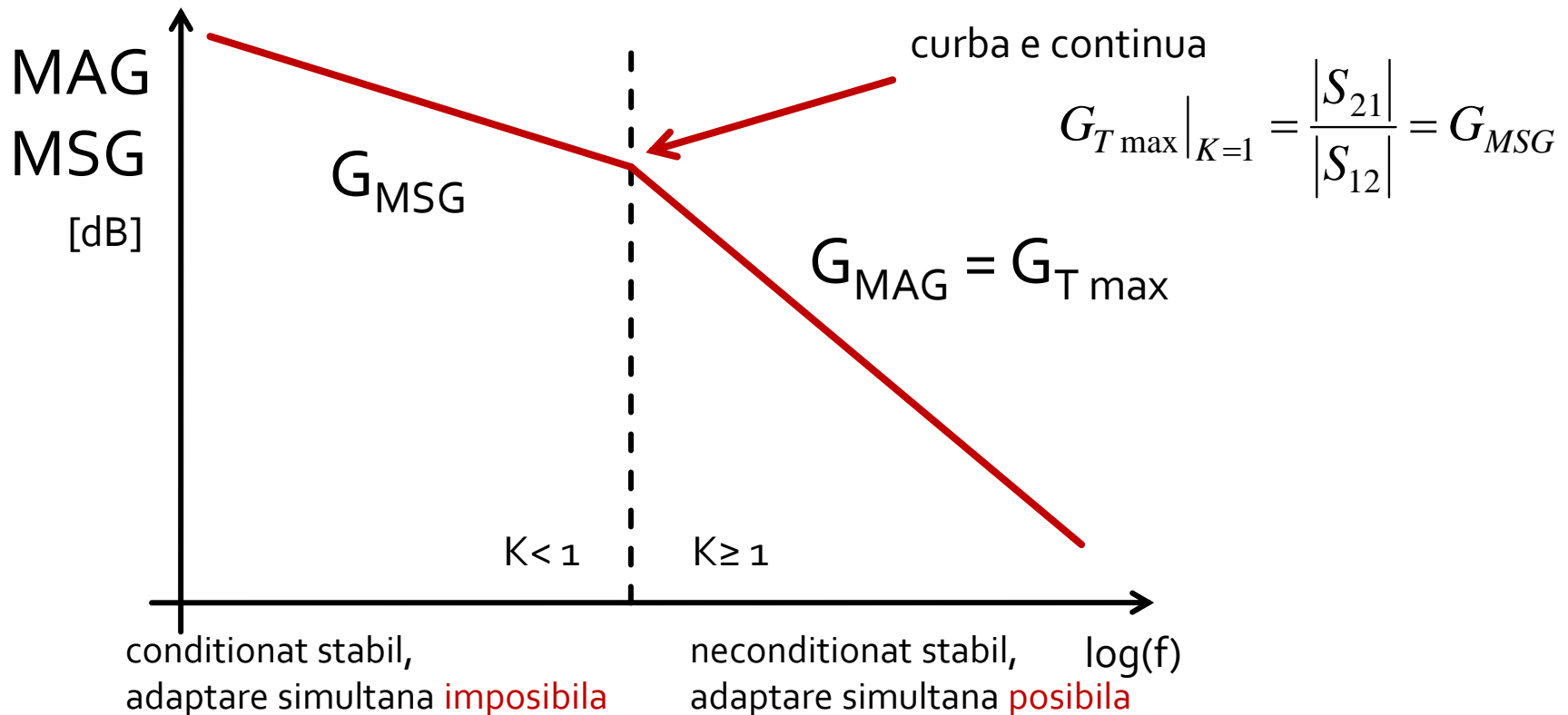
$$G_{T \max} = \frac{|S_{21}|}{|S_{12}|} \cdot (K - \sqrt{K^2 - 1})$$

- Daca dispozitivul **nu** este **neconditionat stabil** se poate folosi ca o indicatie a capacitatii de amplificare castigul maxim stabil (Maximum Stable Gain)

$$G_{MSG} = \frac{|S_{21}|}{|S_{12}|}$$

# Maximum Available Gain

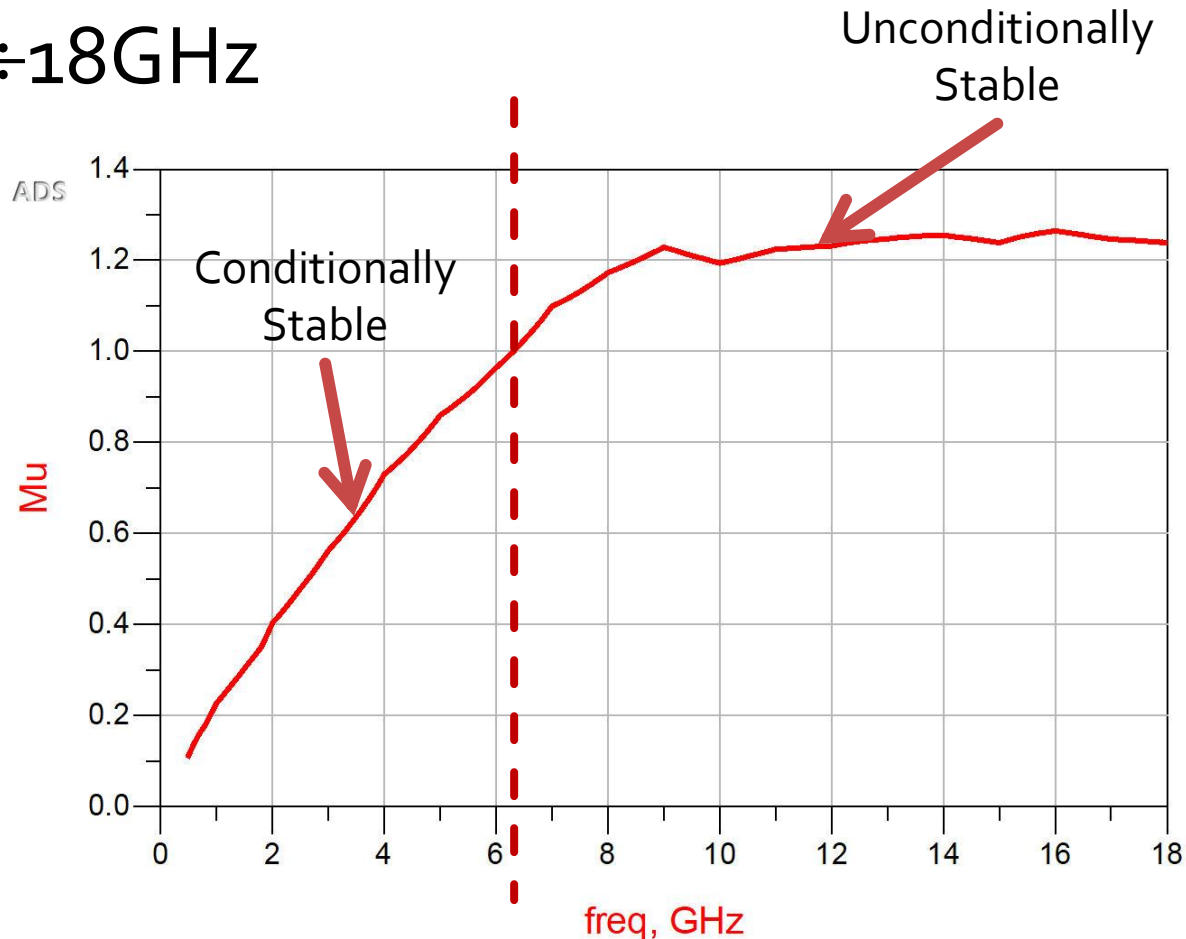
- Indicator in the entire frequency range of the ability to obtain gain





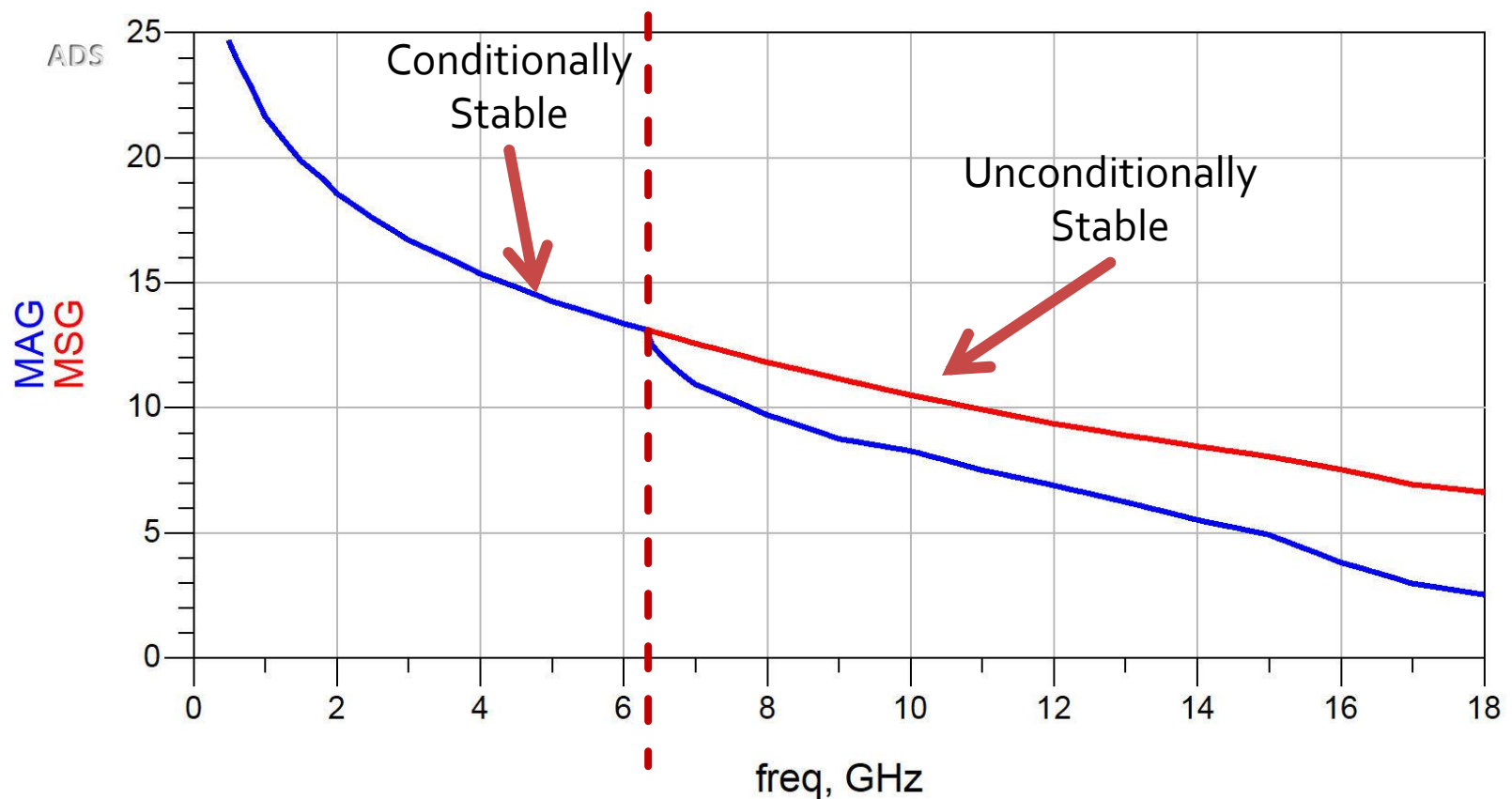
# Stabilitate

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @0.5÷18GHz



# Castig

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @0.5÷18GHz



# Adaptare simultana, tranzistor unilateral

- Daca amplificatorul/tranzistorul este **unilateral** ( $S_{12} = 0$ ) adaptarea simultana implica:

$$\Gamma_{in} = S_{11}$$

$$\Gamma_{out} = S_{22}$$

$$\Gamma_S = S_{11}^*$$

$$\Gamma_L = S_{22}^*$$

$$G_{T \max} = \frac{1}{1 - |\Gamma_S|^2} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

$$G_{TU \max} = \frac{1}{1 - |S_{11}|^2} \cdot |S_{21}|^2 \cdot \frac{1}{1 - |S_{22}|^2}$$

# Exemplu

- ATF-34143 **at  $V_{ds}=3V$   $I_d=20mA$ .**
  - fara stabilizare  $K = 0.886$ ,  $MAG = 14.248dB$  @ 5GHz
  - nu poate fi folosit in aceasta polarizare
- ATF-34143 **at  $V_{ds}=4V$   $I_d=40mA$** 
  - fara stabilizare  $K = 1.031$ ,  $MAG = 12.9dB$  @ 5GHz
  - utilizam aceasta polarizare pentru a implementa un amplificator

# Exemplu

- ATF-34143 at  $V_{ds}=4V$   $I_d=40mA$ .
  - @5GHz
    - $S_{11} = 0.64 \angle 111^\circ$
    - $S_{12} = 0.117 \angle -27^\circ$
    - $S_{21} = 2.923 \angle -6^\circ$
    - $S_{22} = 0.21 \angle 111^\circ$
- $$\begin{cases} S_{11} = 0.64 \angle 111^\circ \\ S_{11} = 0.64 \cdot \cos 111^\circ + j \cdot 0.64 \cdot \sin 111^\circ \end{cases}$$

# Calcul

## ■ Parametri S

- $S_{11} = -0.229 + 0.597 \cdot j$
  - $S_{12} = 0.104 - 0.053 \cdot j$
  - $S_{21} = 2.907 - 0.306 \cdot j$
  - $S_{22} = -0.075 + 0.196 \cdot j$
- $$\begin{cases} S_{11} = 0.64 \angle 111^\circ \\ S_{11} = 0.64 \cdot \cos 111^\circ + j \cdot 0.64 \cdot \sin 111^\circ \end{cases}$$

$$G_{T \max} = \frac{|S_{21}|}{|S_{12}|} \cdot (K - \sqrt{K^2 - 1}) = 19.497 = 12.9 \text{ dB}$$

$$G_{TU \max} = \frac{1}{1 - |S_{11}|^2} \cdot |S_{21}|^2 \cdot \frac{1}{1 - |S_{22}|^2} = 15.139 = 11.8 \text{ dB}$$

# Calcul

$$\begin{cases} B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2 \\ C_1 = S_{11} - \Delta \cdot S_{22}^* \end{cases}$$

$$\begin{cases} B_1 = ? \\ C_1 = ? \end{cases}$$

$$\Gamma_S = \frac{B_1 - \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

$$\Gamma_S = ?$$

$$\begin{cases} B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 \\ C_2 = S_{22} - \Delta \cdot S_{11}^* \end{cases}$$

$$\begin{cases} B_2 = ? \\ C_2 = ? \end{cases}$$

$$\Gamma_L = \frac{B_2 - \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

$$\Gamma_L = ?$$

# Calcul

$$\begin{cases} B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2 \\ C_1 = S_{11} - \Delta \cdot S_{22}^* \end{cases}$$

$$\begin{cases} B_1 = 1.207 \\ C_1 = -0.277 + j \cdot 0.529 \end{cases}$$

$$\Gamma_S = \frac{B_1 - \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

$$\Gamma_S = -0.403 - j \cdot 0.768$$

$$|\Gamma_S| = 0.867 < 1$$

$$\Gamma_S = 0.867 \angle -117.7^\circ$$

$$\begin{cases} B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 \\ C_2 = S_{22} - \Delta \cdot S_{11}^* \end{cases}$$

$$\begin{cases} B_2 = 0.476 \\ C_2 = -0.222 - j \cdot 0.013 \end{cases}$$

$$\Gamma_L = \frac{B_2 - \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

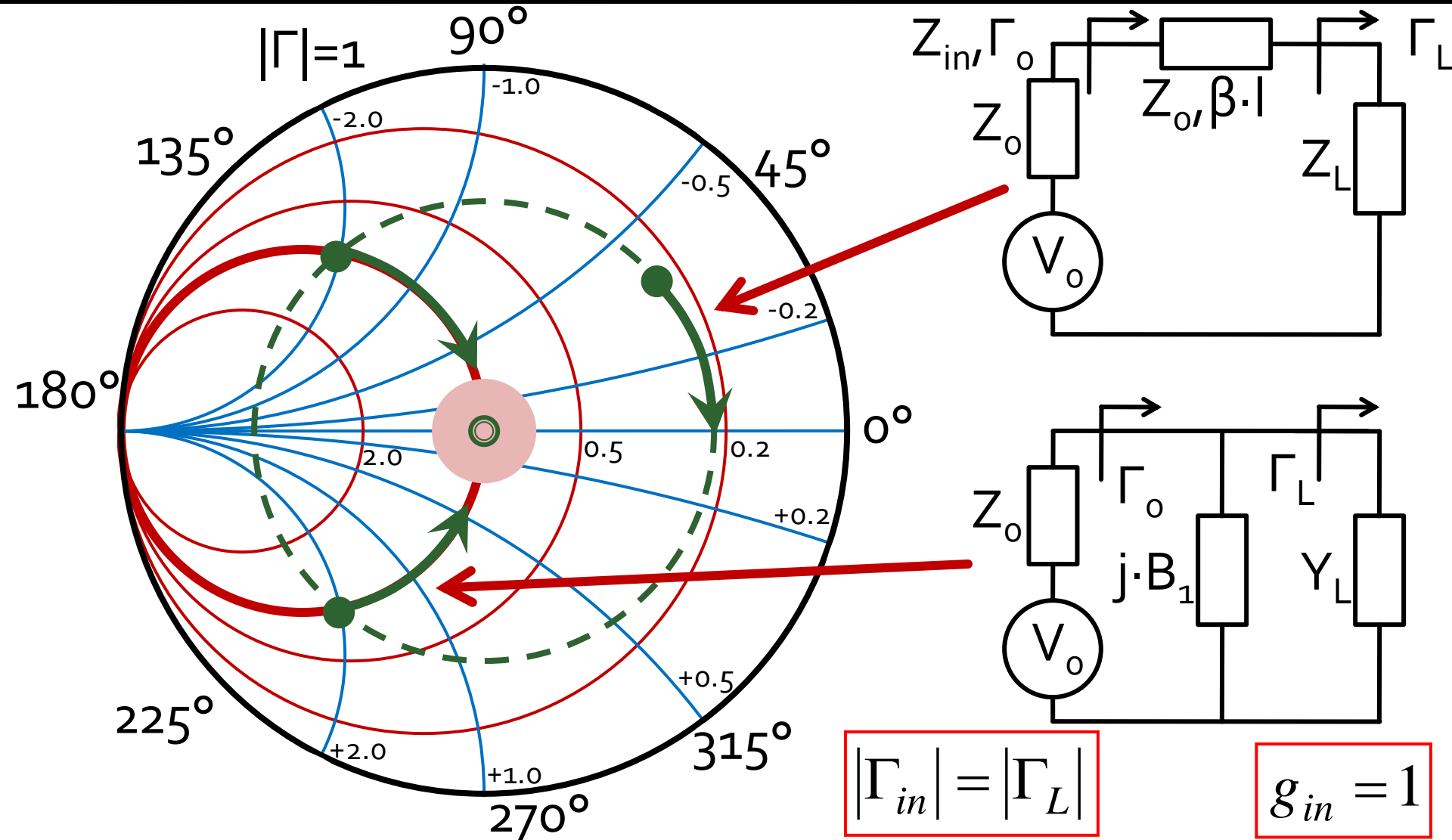
$$\Gamma_L = -0.685 + j \cdot 0.04$$

$$|\Gamma_L| = 0.686 < 1$$

$$\Gamma_L = 0.686 \angle 176.7^\circ$$



# Adaptare cu stub-uri, C8



# Calcul analitic ( $\Gamma_s$ )

$$\cos(\varphi + 2\theta) = -|\Gamma_s|$$

$$\Gamma_s = 0.867 \angle -117.7^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}}$$

$$|\Gamma_s| = 0.867; \quad \varphi = -117.7^\circ \quad \cos(\varphi + 2\theta) = -0.867 \Rightarrow (\varphi + 2\theta) = \pm 150.1^\circ$$

- **Semnul** (+/-) solutiei alese la ecuatia **liniei serie** impune **semnul** solutiei utilizate la ecuatia **stub-ului paralel**

- **solutia "cu +"** 

$$(-117.7^\circ + 2\theta) = +150.1^\circ$$

$$\theta = 133.9^\circ$$

$$\text{Im } y_s = \frac{-2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = -3.477$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_s) = -74^\circ (+180^\circ) \rightarrow \theta_{sp} = 106^\circ$$

- **solutia "cu -"** 

$$(-117.7^\circ + 2\theta) = -150.1^\circ$$

$$\theta = -16.2^\circ (+180^\circ) \rightarrow \theta = 163.8^\circ$$

$$\text{Im } y_s = \frac{+2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = +3.477$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_s) = 74^\circ$$

# Calcul analitic ( $\Gamma_L$ )

$$\cos(\varphi + 2\theta) = -|\Gamma_L|$$

$$\Gamma_L = 0.686 \angle 176.7^\circ$$

$$|\Gamma_L| = 0.686; \quad \varphi = 176.7^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}}$$

- **Semnul** (+/-) solutiei alese la ecuatia **liniei serie** impune **semnul** solutiei utilizate la ecuatia **stub-ului paralel**
  - solutia "cu +"
  - solutia "cu -"

# Calcul analitic ( $\Gamma_L$ )

$$\cos(\varphi + 2\theta) = -|\Gamma_L|$$

$$\Gamma_L = 0.686 \angle 176.7^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}}$$

$$|\Gamma_L| = 0.686; \quad \varphi = 176.7^\circ \quad \cos(\varphi + 2\theta) = -0.686 \Rightarrow (\varphi + 2\theta) = \pm 133.3^\circ$$

- **Semnul** (+/-) solutiei alese la ecuatia **liniei serie** impune **semnul** solutiei utilizate la ecuatia **stub-ului paralel**

- **solutia "cu +"** 

$$(176.7^\circ + 2\theta) = +133.3^\circ \quad \theta = -21.7^\circ (+180^\circ) \rightarrow \theta = 158.3^\circ$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_L) = -62.1^\circ (+180^\circ) \rightarrow \theta_{sp} = 117.9^\circ \quad \text{Im } y_L = \frac{-2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = -1.885$$

- **solutia "cu -"** 

$$(176.7^\circ + 2\theta) = -133.3^\circ \quad \theta = -155^\circ (+180^\circ) \rightarrow \theta = 25^\circ$$

$$\text{Im } y_L = \frac{+2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = +1.885 \quad \theta_{sp} = \tan^{-1}(\text{Im } y_L) = 62.1^\circ$$

# Calcul analitic

- Se alege **una** din cele doua solutii posibile la intrare

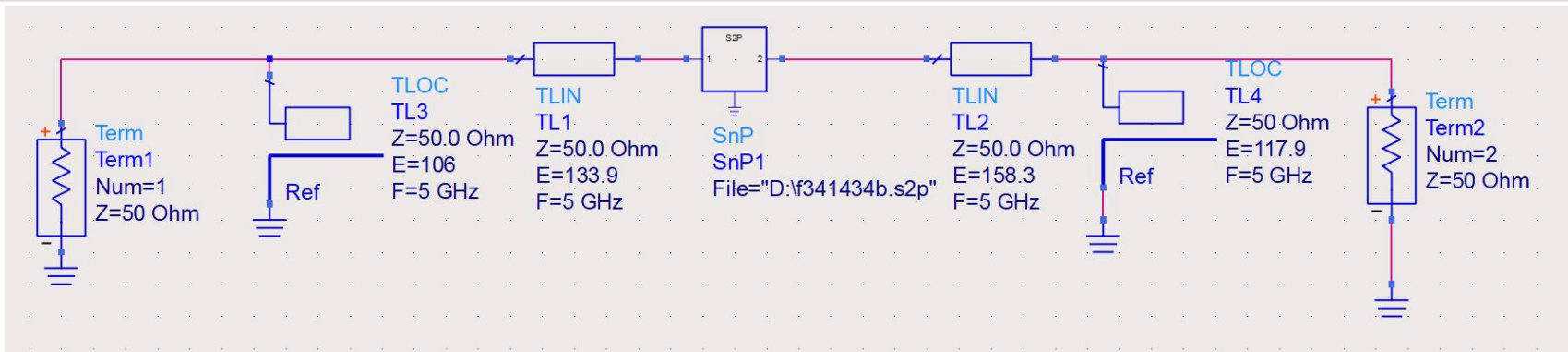
$$(\varphi + 2\theta) = \begin{cases} +150.1^\circ \\ -150.1^\circ \end{cases} \quad \theta = \begin{cases} 133.9^\circ \\ 163.8^\circ \end{cases} \quad \text{Im}[y_s(\theta)] = \begin{cases} -3.477 \\ +3.477 \end{cases} \quad \theta_{sp} = \begin{cases} -74^\circ + 180^\circ = 106^\circ \\ +74^\circ \end{cases}$$

- Similar pentru adaptarea la iesire

$$(\varphi + 2\theta) = \begin{cases} +133.3^\circ \\ -133.3^\circ \end{cases} \quad \theta = \begin{cases} 158.3^\circ \\ 25.0^\circ \end{cases} \quad \text{Im}[y_s(\theta)] = \begin{cases} -1.885 \\ +1.885 \end{cases} \quad \theta_{sp} = \begin{cases} 117.9^\circ \\ 62.1^\circ \end{cases}$$

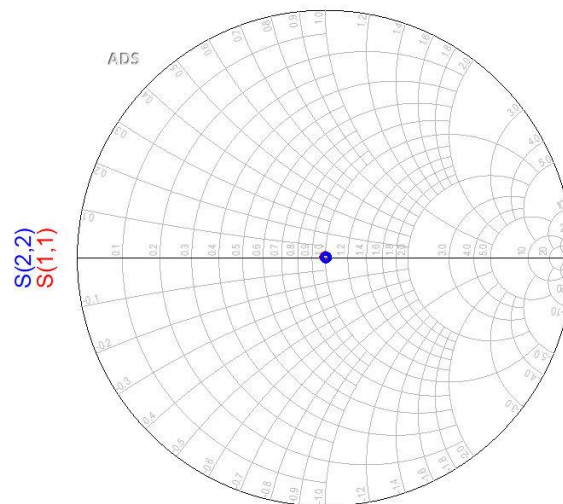
- In total exista **4** posibilitati de adaptare intrare/iesire

# ADS



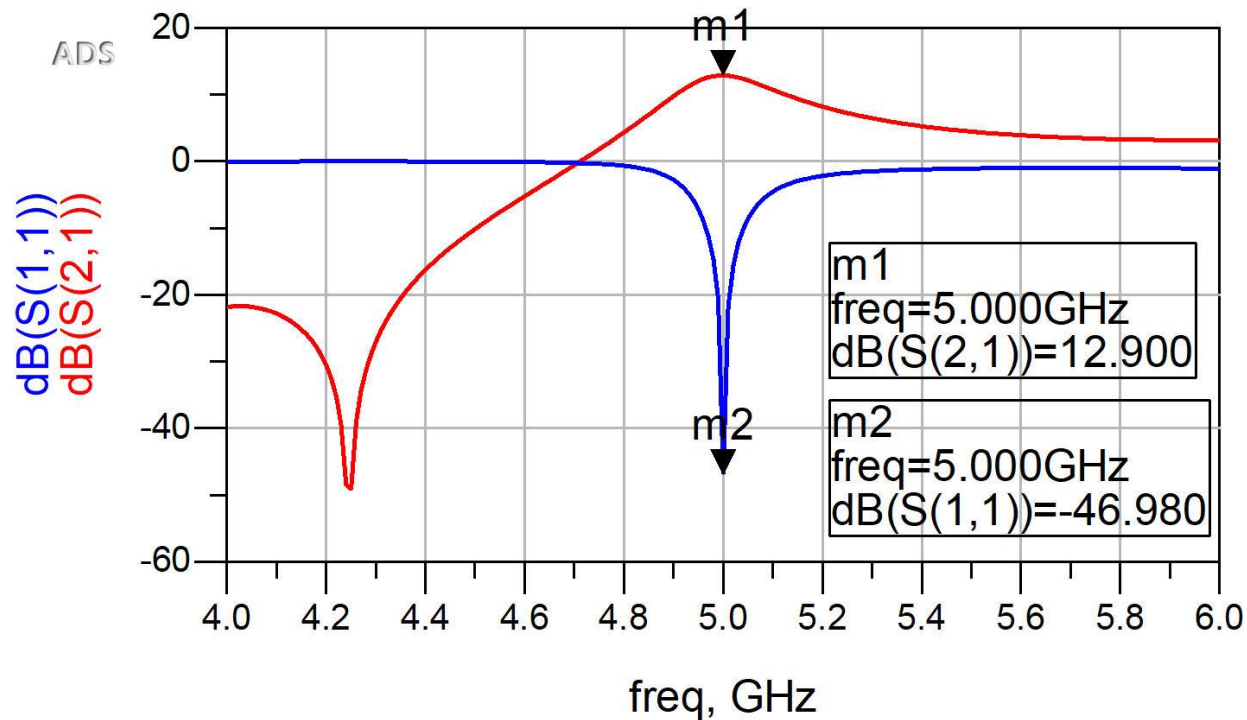
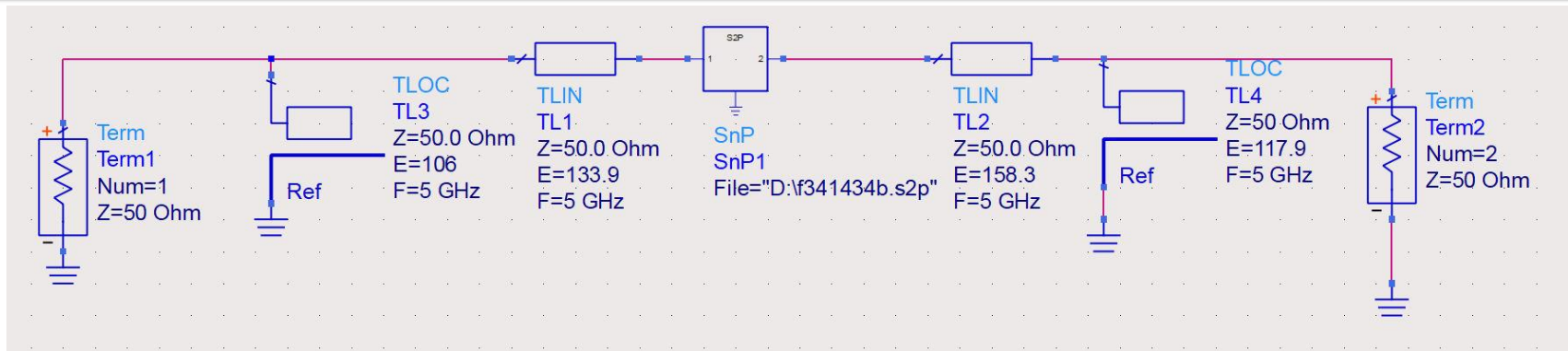
$$EqnGT=10*\log(\text{mag}(S(2,1))^*2)$$

freq	S(2,1)	GT	S(1,1)	S(2,2)
5.000 GHz	4.415 / 157.353	12.900	0.004 / 86.088	0.004 / 37.766



freq (5.000GHz to 5.000GHz)

# ADS

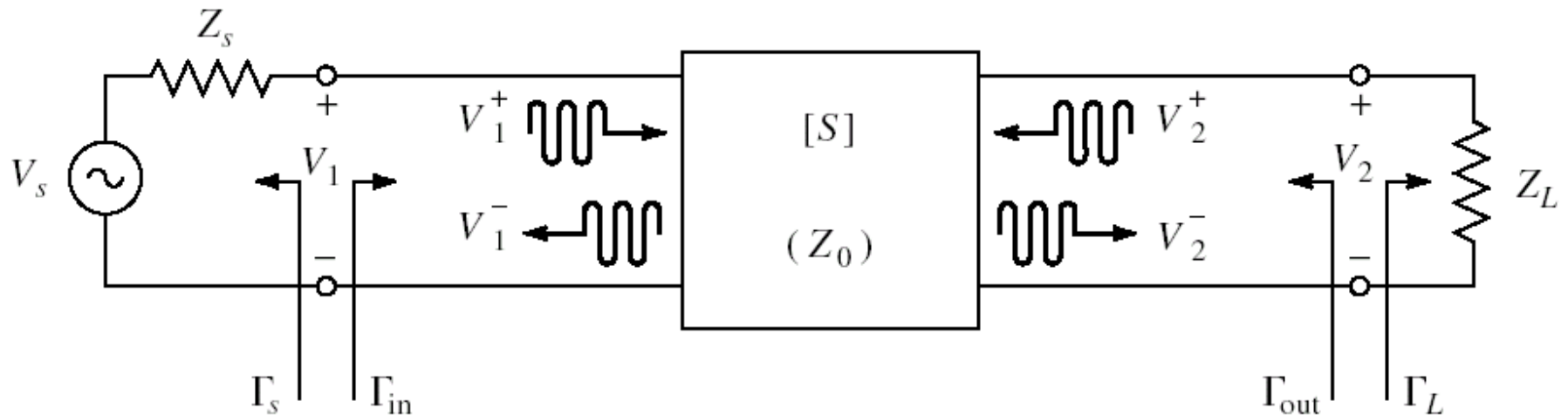


Amplificatoare de microunde

# Proiectare pentru castig impus



# Cuadripol Amplificator



- marimi care intereseaza:
  - stabilitate
  - **castig de putere**
  - zgomot (uneori – semnal mic)
  - liniaritate (uneori – semnal mare)

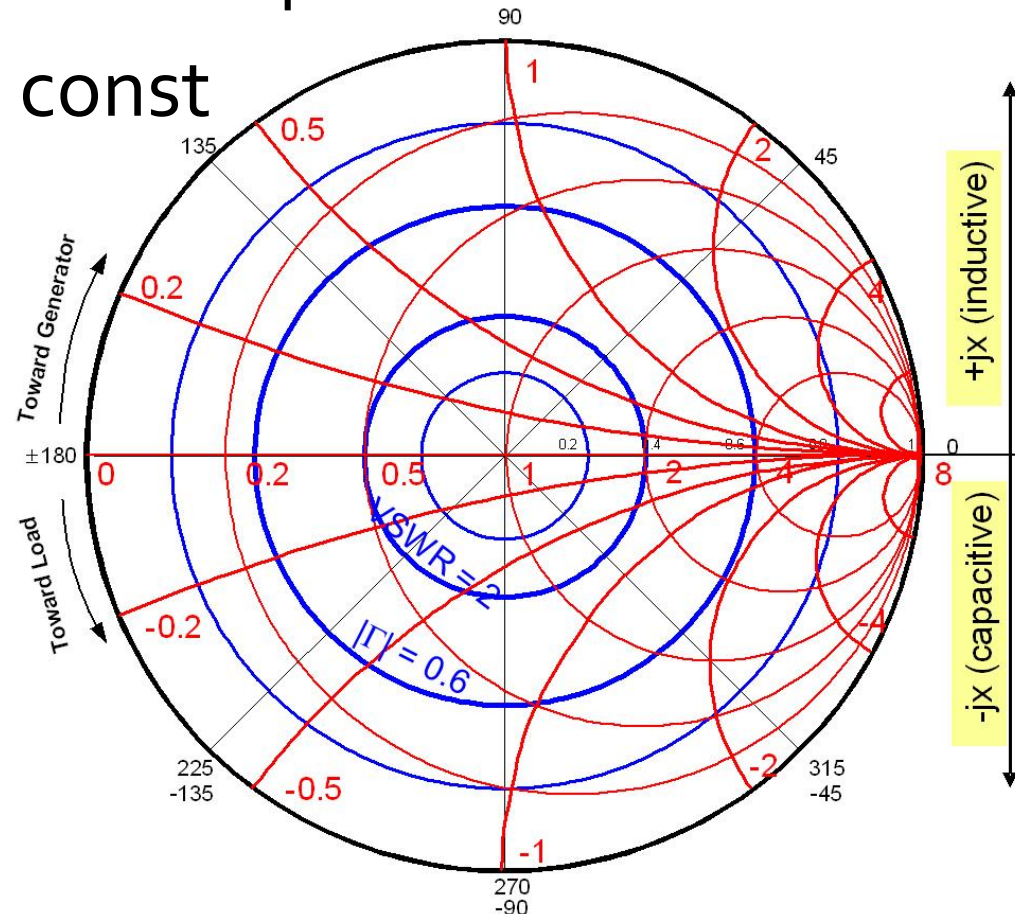
# Proiectare pentru castig impus

- Deseori este necesara o alta abordare decat "forta bruta" si se prefera obtinerea unui **castig mai mic** decat cel maxim posibil pentru:
  - conditii de zgomot avantajoase ( $L_3 + C_{10-11}$ )
  - conditii de stabilitate mai bune
  - obtinerea unui VSWR mai mic
  - controlul performantelor la mai multe frecvente
  - banda de functionare a amplificatorului

# VSWR

- Anumite aplicatii pot impune un raport intre tensiunile maxime/minime pe linii
- $VSWR = \text{const} \rightarrow |\Gamma| = \text{const}$

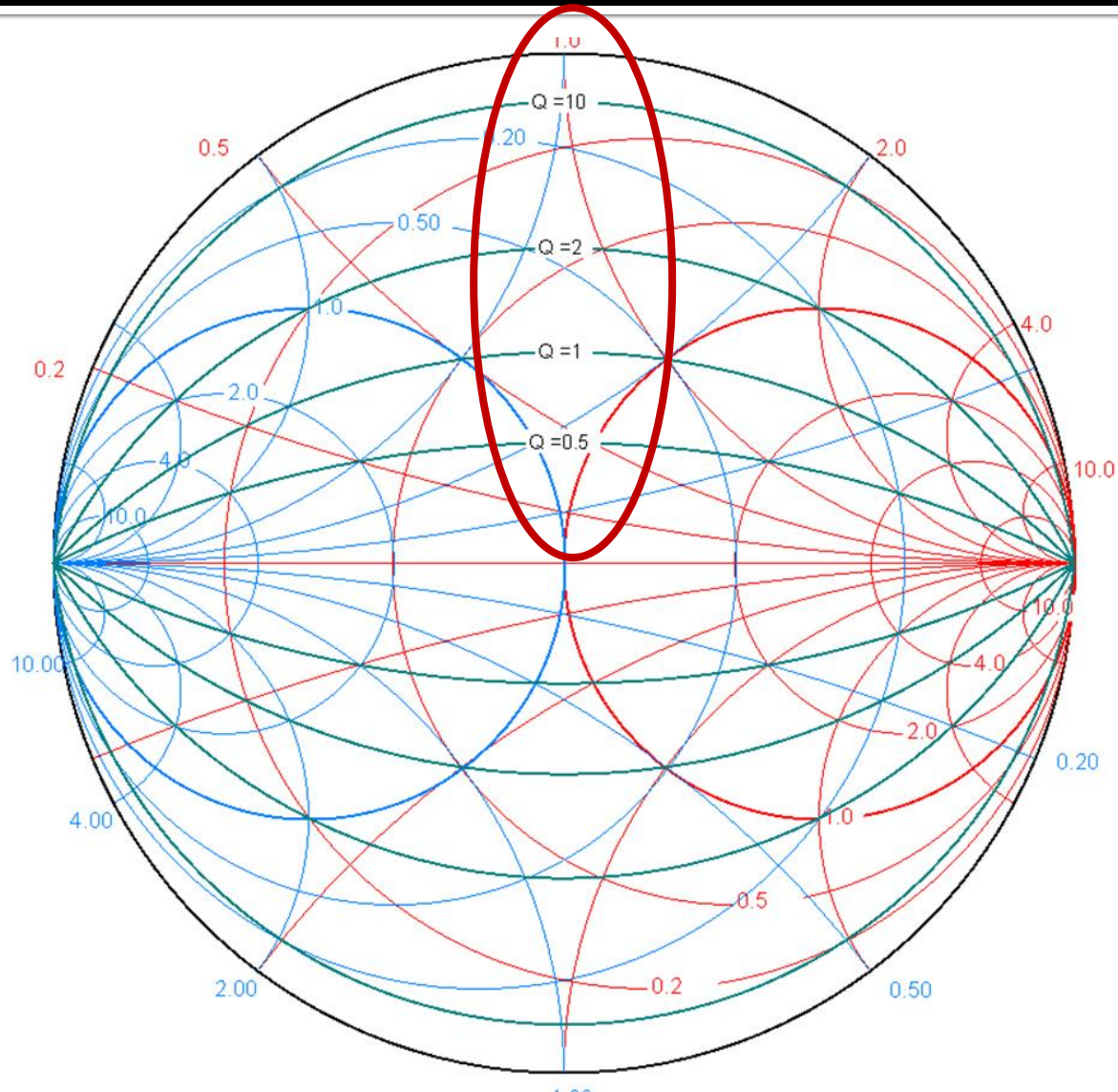
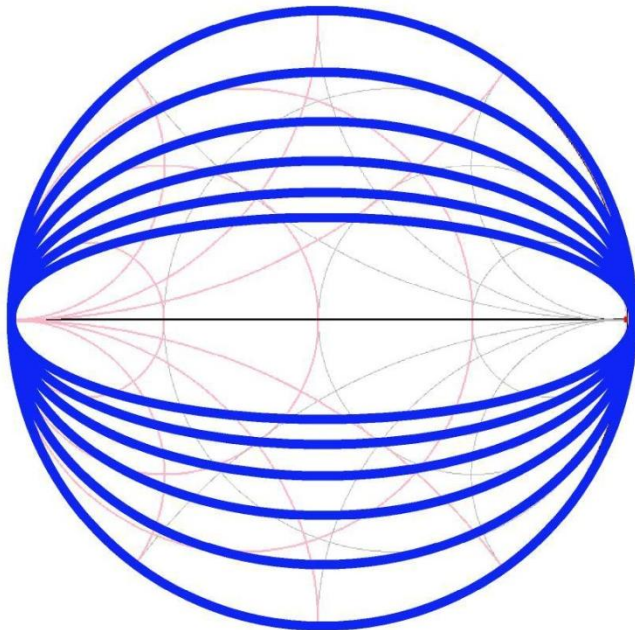
$$VSWR = \frac{V_{\max}}{V_{\min}} = \frac{1 + |\Gamma|}{1 - |\Gamma|}$$



# Cercuri de factor de calitate constant

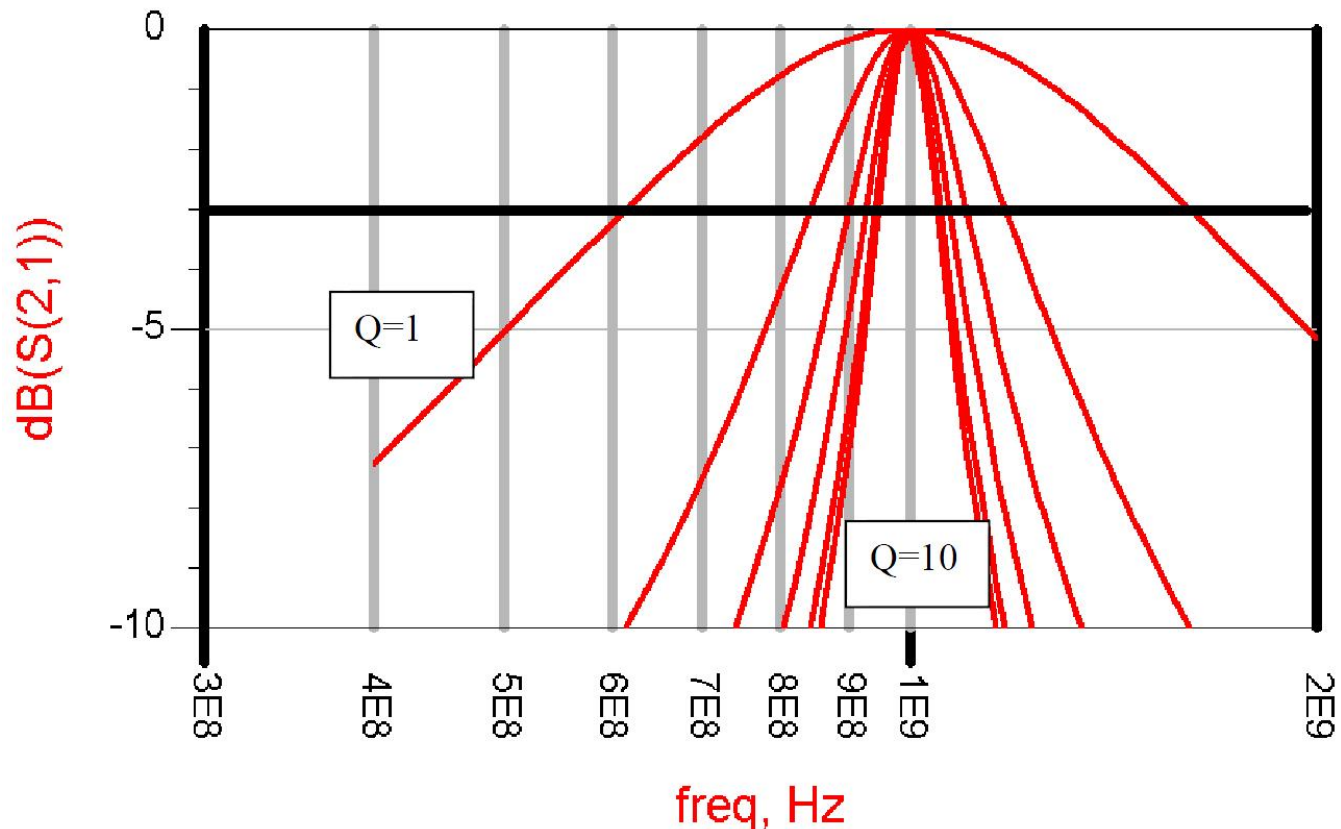
- Diagrama Smith

$$Q = \frac{X}{R} = \frac{G}{B} = \text{const}$$



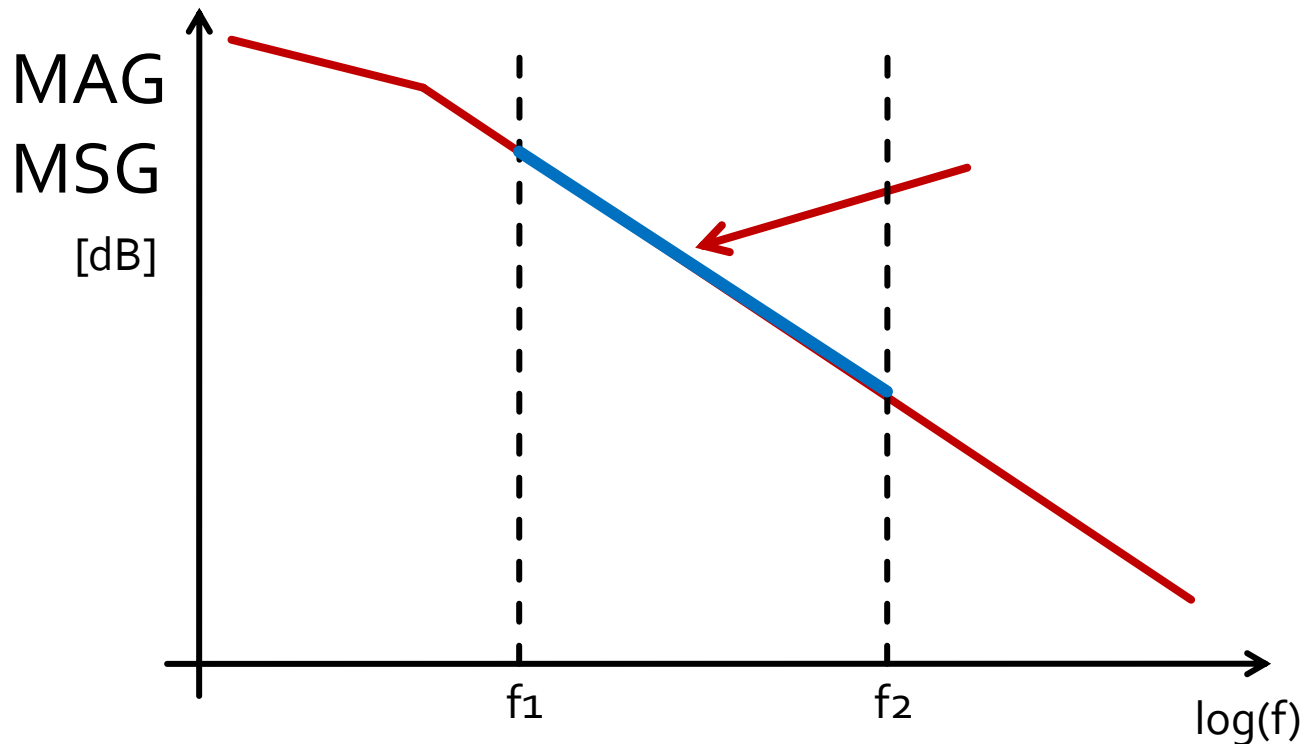
# Factor de calitate - banda

- Factor de calitate ridicat echivalent cu banda îngusta



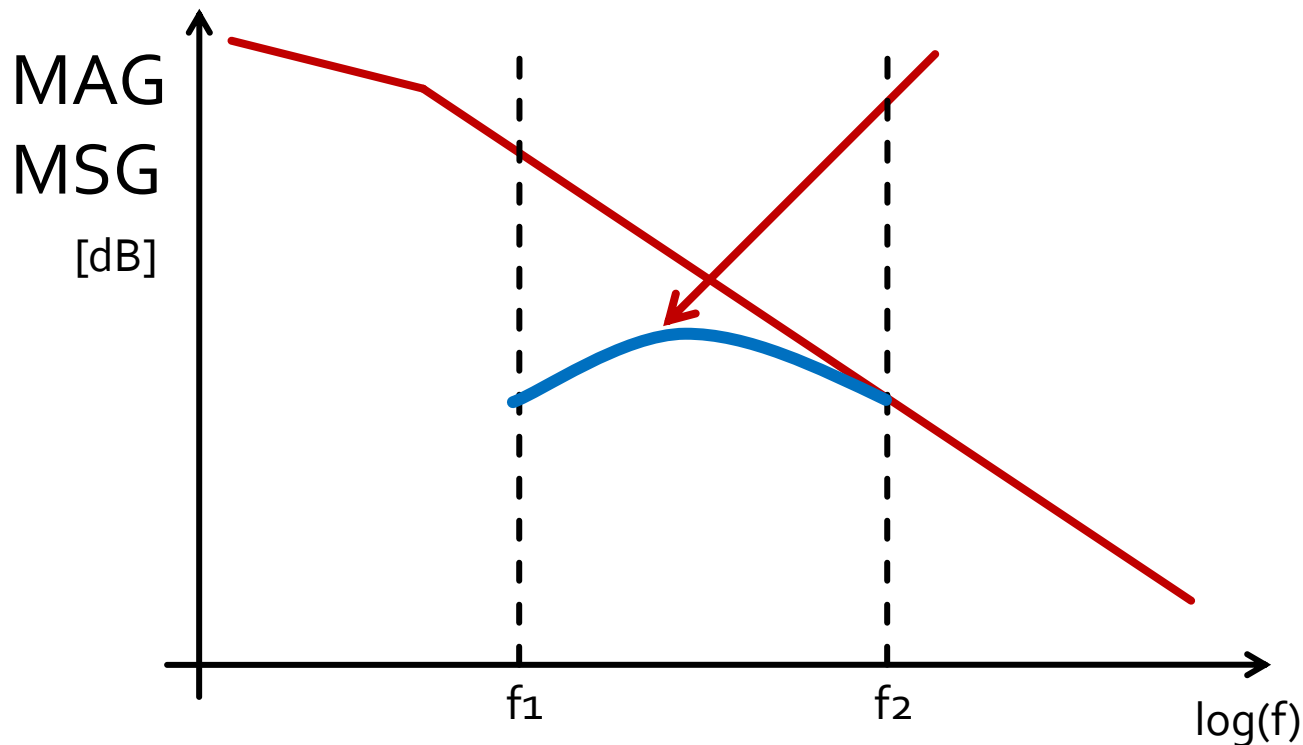
# Amplificator de banda larga

- Adaptarea pentru castig maxim la doua frecvente genereaza o comportare dezechilibrata



# Amplificator de banda larga


- Adaptare pentru castig maxim la frecventa maxima
- Dezadaptare controlata la frecventa minima
  - eventual la mai multe frecvente din banda



# Proiectare pentru castig impus

- Se realizeaza cu asumarea **unilaterală** a amplificatorului

Permite tratarea separata a intrarii si iesirii


$$G_{TU} = |S_{21}|^2 \cdot \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2} \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

$$S_{12} \cong 0$$

$$\Gamma_{in} = S_{11}$$

- Castig maxim

$$\Gamma_S = S_{11}^*$$

$$\Gamma_L = S_{22}^*$$

$$G_{TU \max} = \frac{1}{1 - |S_{11}|^2} \cdot |S_{21}|^2 \cdot \frac{1}{1 - |S_{22}|^2}$$



# Factor de merit unilateral

- Permite estimarea erorii induse de ipoteza tranzistorului unilateral

$$S_{12} \cong 0$$

$$\frac{1}{(1+U)^2} < \frac{G_T}{G_{TU}} < \frac{1}{(1-U)^2} \quad U = \frac{|S_{12}| \cdot |S_{21}| \cdot |S_{11}| \cdot |S_{22}|}{(1-|S_{11}|^2) \cdot (1-|S_{22}|^2)}$$

- Se calculeaza U si abaterea maxima si minima a lui  $G_{TU}$  fata de  $G_T$ 
  - aceasta abatere trebuie prevazuta in proiectare ca rezerva pentru castigul maxim

$$-20 \cdot \log(1+U) < G_T [dB] - G_{TU} [dB] < -20 \cdot \log(1-U)$$

# Exemplu

- ATF-34143 **at  $V_{ds}=3V$   $I_d=20mA$ .**
- @5GHz

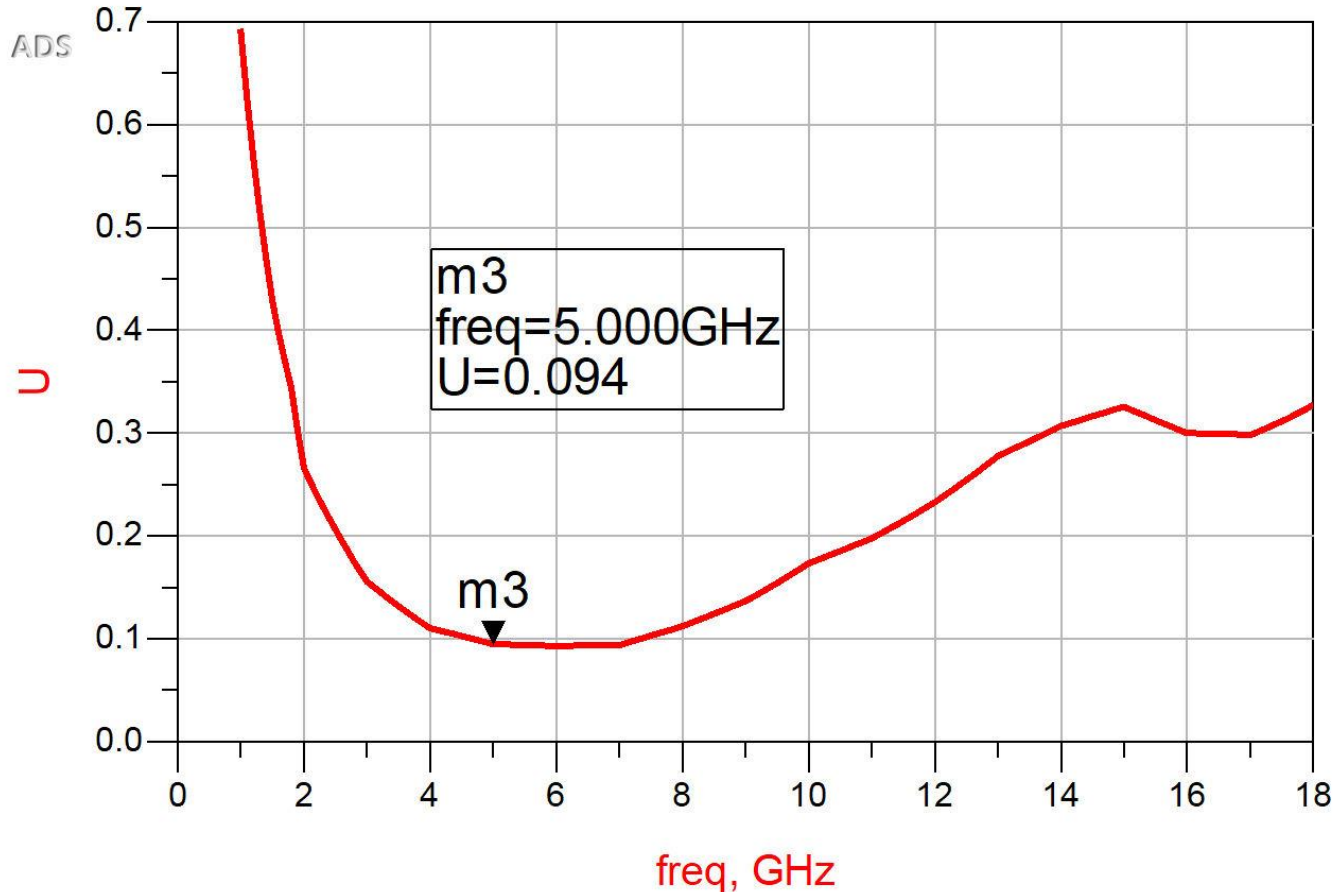
- $S_{11} = 0.64 \angle 139^\circ$
- $S_{12} = 0.119 \angle -21^\circ$
- $S_{21} = 3.165 \angle 16^\circ$
- $S_{22} = 0.22 \angle 146^\circ$

$$U = \frac{|S_{12}| \cdot |S_{21}| \cdot |S_{11}| \cdot |S_{22}|}{(1 - |S_{11}|^2) \cdot (1 - |S_{22}|^2)} = 0.094$$

$$-0.783 \text{ dB} < G_T [\text{dB}] - G_{TU} [\text{dB}] < 0.861 \text{ dB}$$

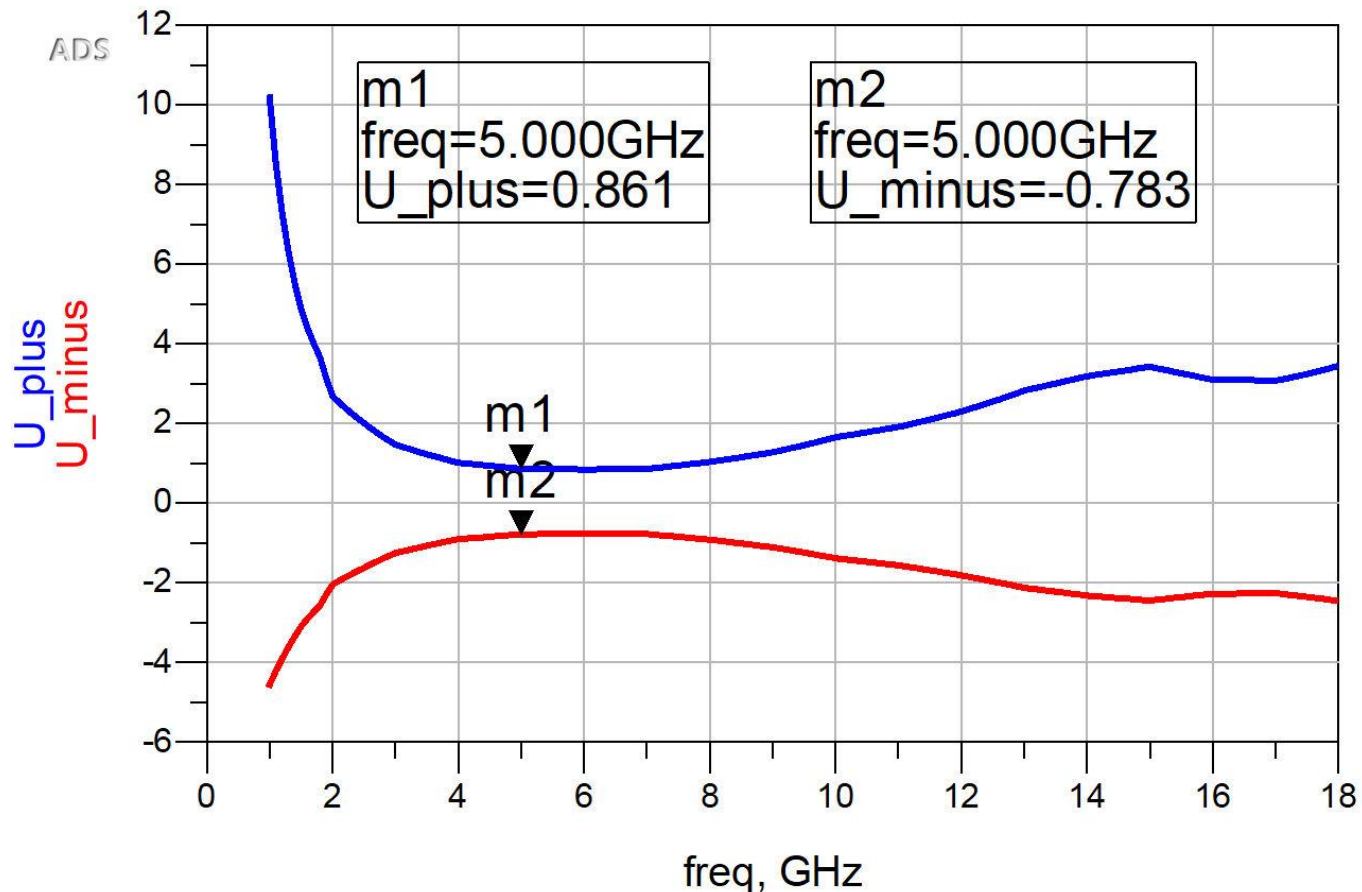
# Exemplu

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @5GHz

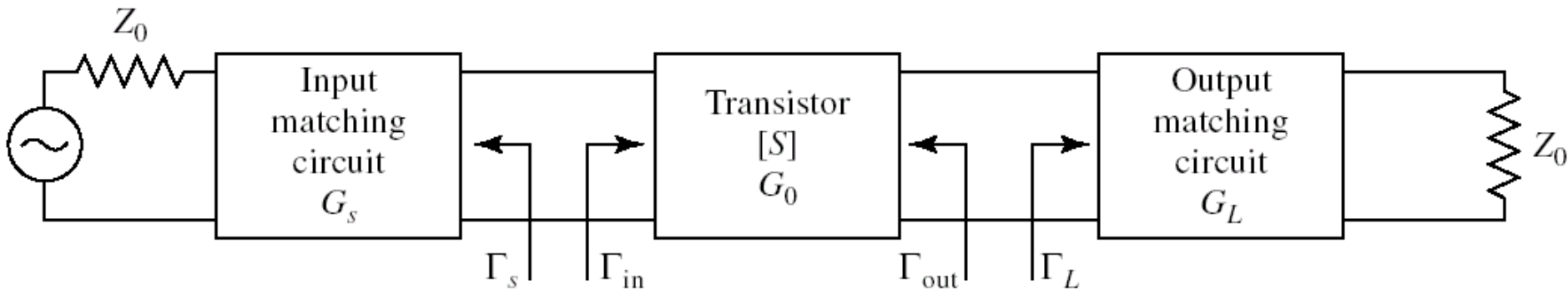


# Exemplu

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @5GHz



# Proiectare pentru castig impus



- Daca ipoteza tranzistorului unilateral este justificata:

$$G_{TU} = \frac{1 - |\Gamma_s|^2}{|1 - S_{11} \cdot \Gamma_s|^2} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

$$G_S = \frac{1 - |\Gamma_s|^2}{|1 - S_{11} \cdot \Gamma_s|^2}$$

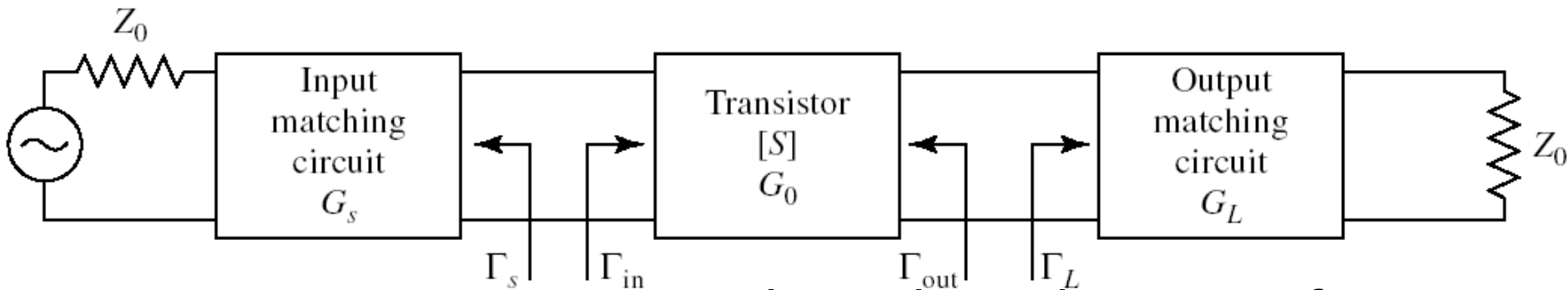
$$G_S = G_S(\Gamma_s)$$

$$G_0 = |S_{21}|^2$$

$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

$$G_L = G_L(\Gamma_L)$$

# Proiectare pentru castig impus

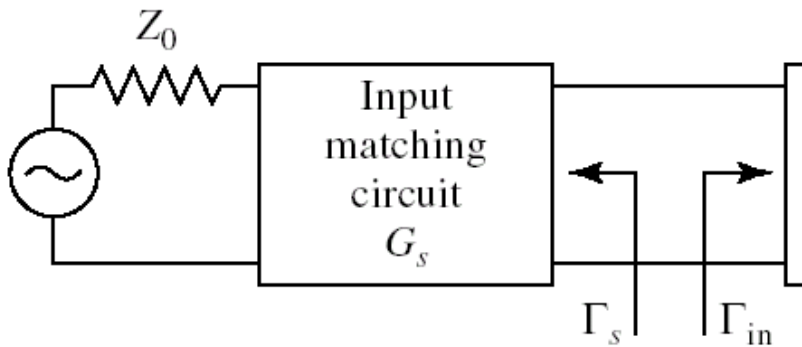


- **Daca** ipoteza tranzistorului unilateral este justificata:
  - castigul adaugat prin adaptare mai buna la intrare **nu** depinde de adaptarea la iesire  $G_s = G_s(\Gamma_s)$
  - castigul adaugat prin adaptare mai buna la iesire **nu** depinde de adaptarea la intrare  $G_L = G_L(\Gamma_L)$
- Adaptarile la intrare/iesire pot fi tratate independent
  - Se pot impune cerinte diferite intrare/iesire
  - se tine cont de compunerea castigurilor generate

$$G_T = G_s \cdot G_0 \cdot G_L$$

$$G_T[dB] = G_s[dB] + G_0[dB] + G_L[dB]$$

# Adaptarea la intrare



$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2}$$

- Castig maxim pentru adaptare complex conjugata (putere) la intrare

$$\Gamma_S = S_{11}^* \Rightarrow G_{S \max} = \frac{1}{1 - |S_{11}|^2}$$

- Pentru oricare alta retea de adaptare

$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2} < G_{S \max} = \frac{1}{1 - |S_{11}|^2}$$

# Exemplu

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @5GHz

- $S_{11} = 0.64 \angle 139^\circ$
- $S_{12} = 0.119 \angle -21^\circ$
- $S_{21} = 3.165 \angle 16^\circ$
- $S_{22} = 0.22 \angle 146^\circ$

$$U = \frac{|S_{12}| \cdot |S_{21}| \cdot |S_{11}| \cdot |S_{22}|}{(1 - |S_{11}|^2) \cdot (1 - |S_{22}|^2)} = 0.094$$

$$-0.783 \text{ dB} < G_T [\text{dB}] - G_{TU} [\text{dB}] < 0.861 \text{ dB}$$

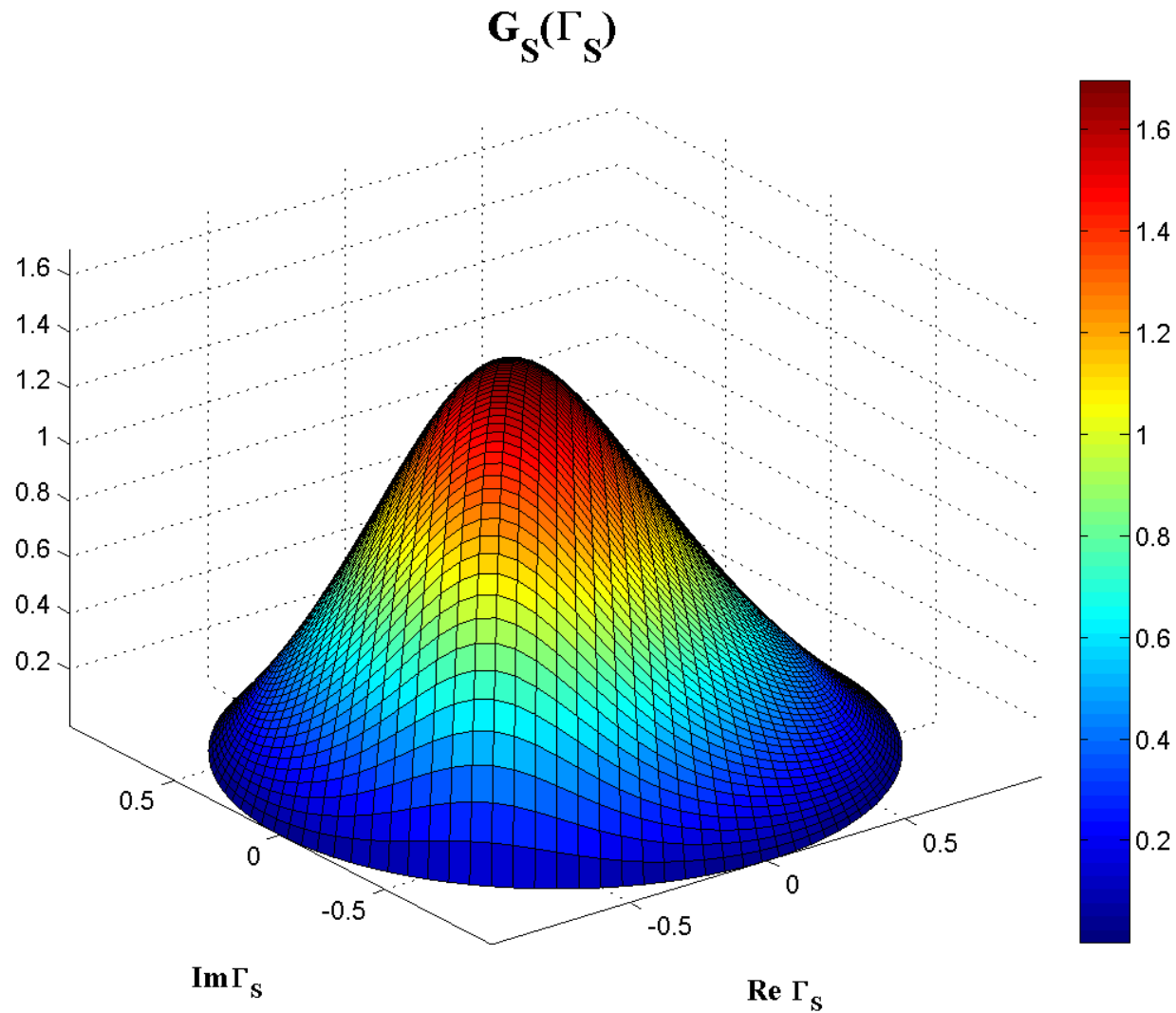
$$G_{TU \max} = \frac{1}{1 - |S_{11}|^2} \cdot |S_{21}|^2 \cdot \frac{1}{1 - |S_{22}|^2} = 17.83$$

$$G_{TU \max} [\text{dB}] = 12.511 \text{ dB}$$

$$G_{S \max} = \frac{1}{1 - |S_{11}|^2} = 1.694 = 2.289 \text{ dB}$$

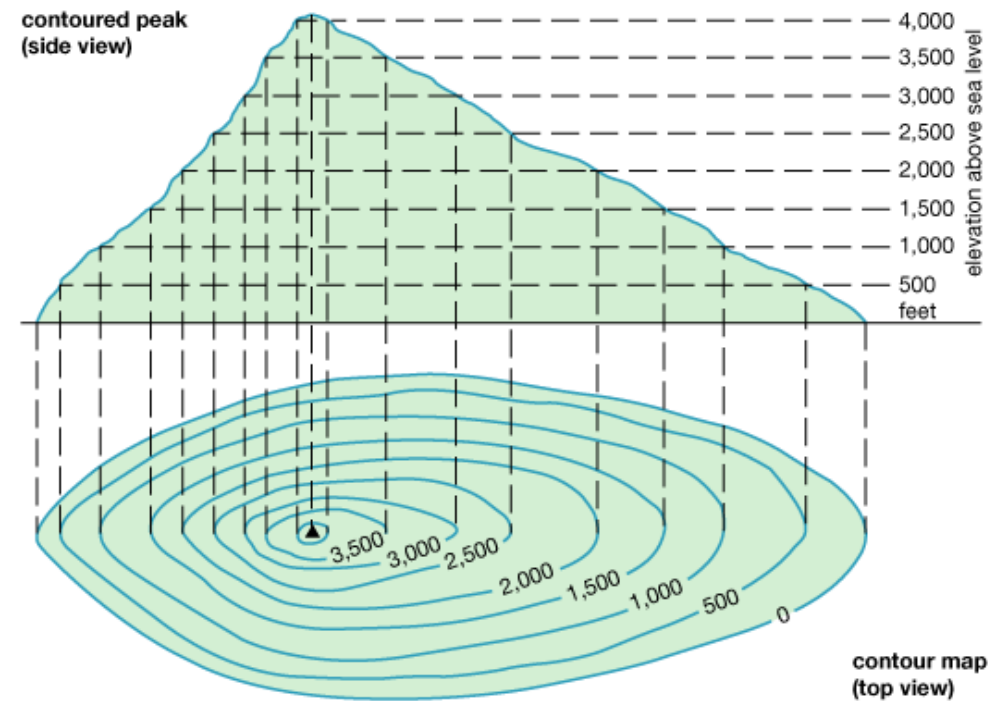


# $G_S(\Gamma_S)$

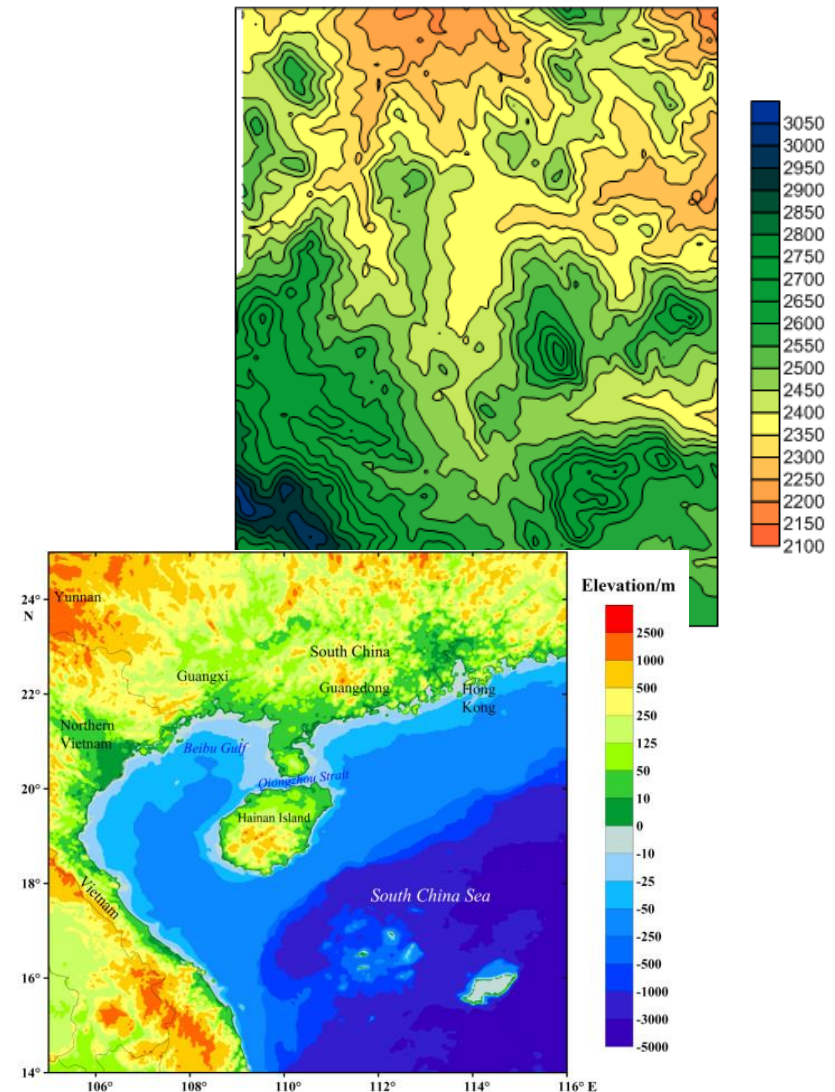


$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2}$$

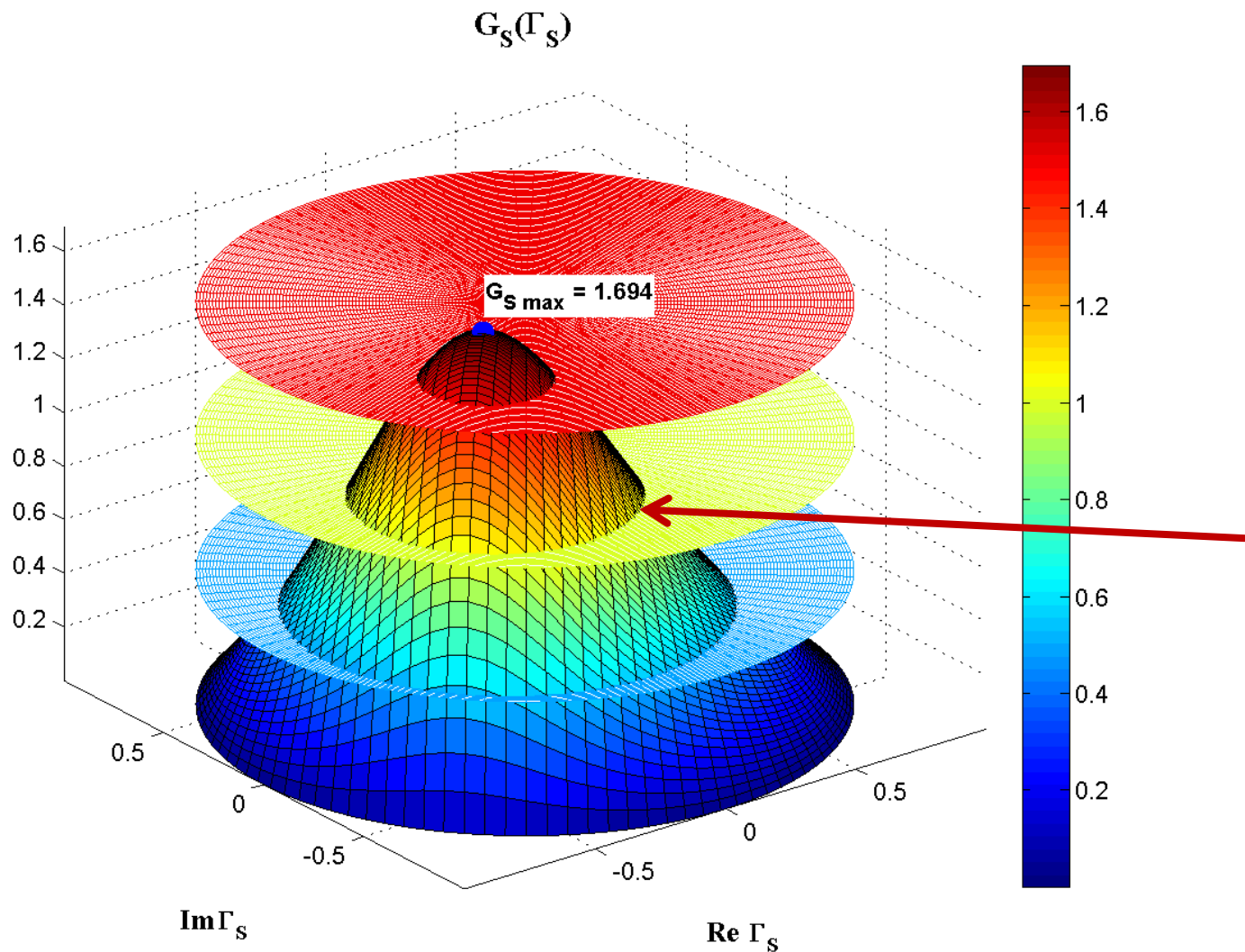
# Contour map/lines



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# $G_S(\Gamma_S)$ , nivel constant



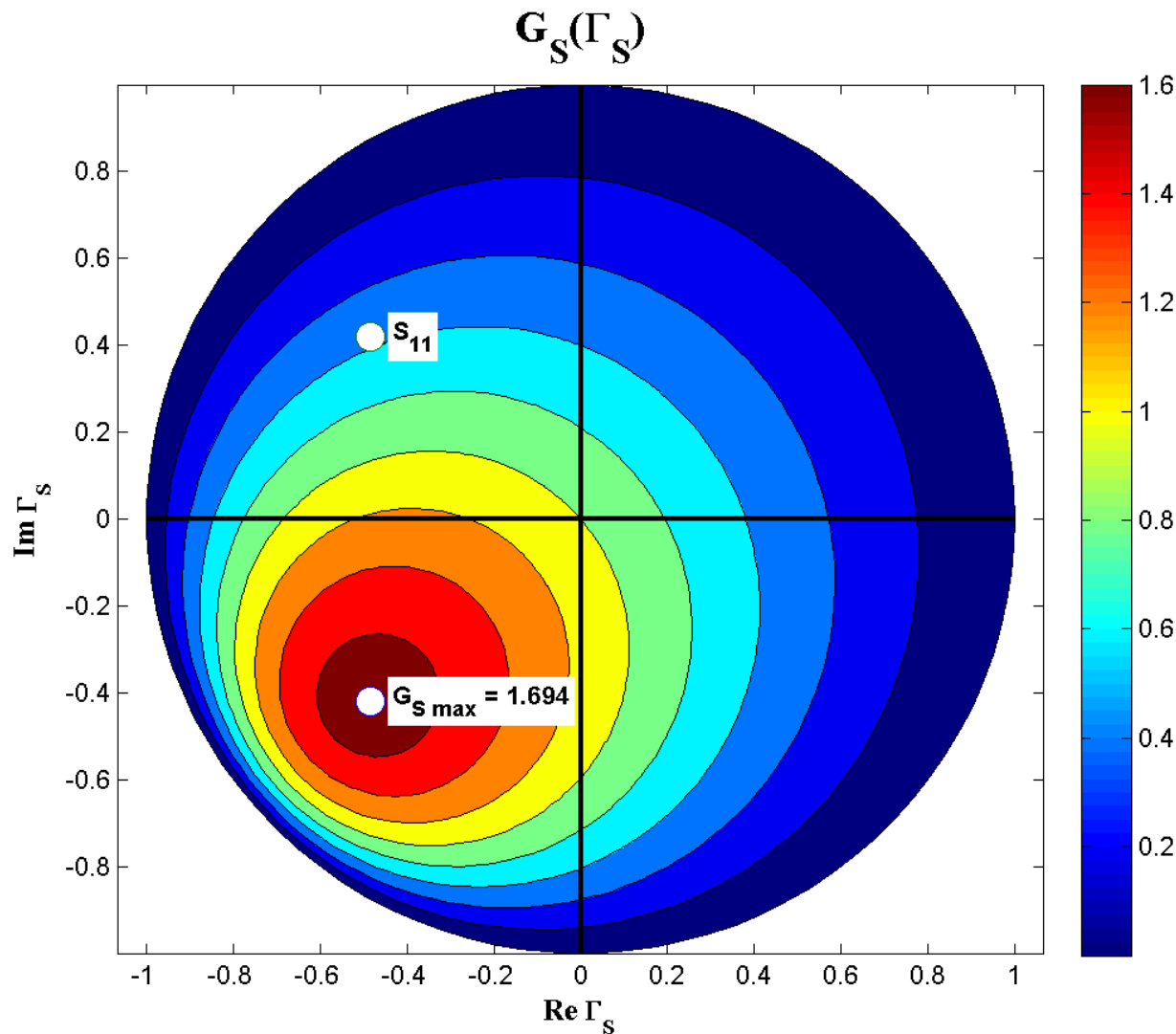
$$G_S = 1.5$$

$$G_S = 1.0$$

$$G_S = 0.5$$

**Cercuri**

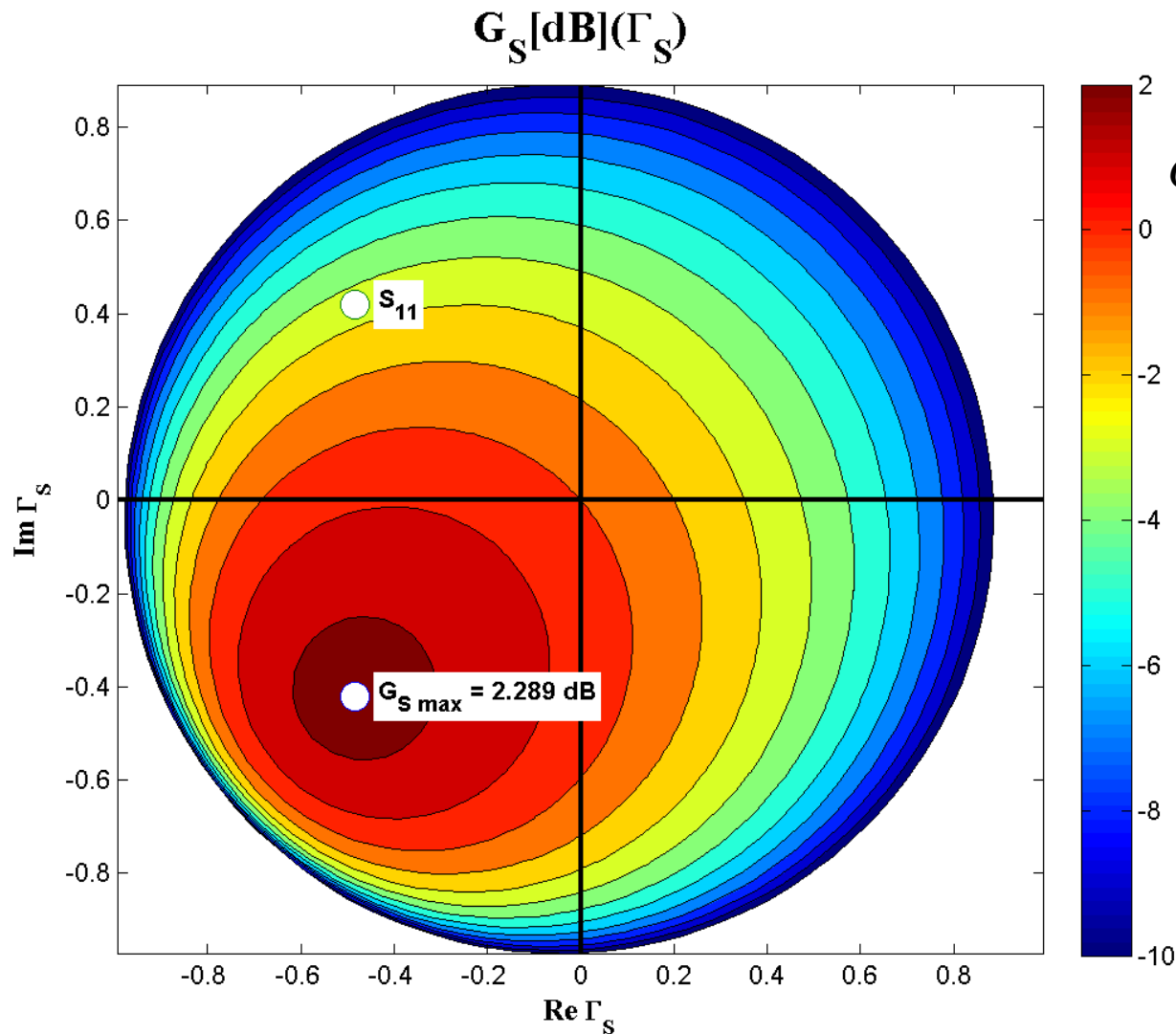
# $G_S(\Gamma_S)$ , diagrama de nível



$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2}$$

$$G_{S \max} = G_S|_{\Gamma_S = s_{11}^*}$$

# $G_S[dB](\Gamma_S)$ , diagrama de nivel



$$G_S[dB] = 10 \cdot \log \left( \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2} \right)$$

$$G_{S \max} = G_S|_{\Gamma_S = S_{11}^*}$$

# Cercuri de castig constant la intrare

- Castig normal (coordonate liniare)

$$g_S = \frac{G_S}{G_{S_{\max}}} = \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2} \cdot (1 - |S_{11}|^2) < 1$$

- Punctele de nivel constant, pentru un  $g_S < 1$  fixat

$$g_S \cdot |1 - S_{11} \cdot \Gamma_S|^2 = (1 - |\Gamma_S|^2) \cdot (1 - |S_{11}|^2)$$

$$(g_S \cdot |S_{11}|^2 + 1 - |S_{11}|^2) \cdot |\Gamma_S|^2 - g_S \cdot (S_{11} \cdot \Gamma_S + S_{11}^* \cdot \Gamma_S^*) = 1 - |S_{11}|^2 - g_S$$

$$\Gamma_S \cdot \Gamma_S^* - \frac{g_S \cdot (S_{11} \cdot \Gamma_S + S_{11}^* \cdot \Gamma_S^*)}{1 - (1 - g_S) \cdot |S_{11}|^2} = \frac{1 - |S_{11}|^2 - g_S}{1 - (1 - g_S) \cdot |S_{11}|^2} \bigg/ + \frac{g_S^2 \cdot |S_{11}|^2}{[1 - (1 - g_S) \cdot |S_{11}|^2]^2}$$

# Cercuri de castig constant la intrare

$$\left| \Gamma_S - \frac{g_S \cdot S_{11}^*}{1 - (1 - g_S) \cdot |S_{11}|^2} \right| = \frac{\sqrt{1 - g_S} \cdot (1 - |S_{11}|^2)}{1 - (1 - g_S) \cdot |S_{11}|^2} \quad |\Gamma_S - C_S| = R_S$$

$$C_S = \frac{g_S \cdot S_{11}^*}{1 - (1 - g_S) \cdot |S_{11}|^2} \quad R_S = \frac{\sqrt{1 - g_S} \cdot (1 - |S_{11}|^2)}{1 - (1 - g_S) \cdot |S_{11}|^2}$$

- Ecuația unui cerc în planul complex în care reprezintă  $\Gamma_S$
- **Interpretare:** Orice punct  $\Gamma_S$  care este reprezentat în planul complex se găsește **pe** cercul desenat pentru  $g_{\text{cerc}} = G_{\text{cerc}}/G_{S_{\text{max}}}$  va conduce la obținerea câștigului  $G_S = G_{\text{cerc}}$ 
  - Orice punct **în exteriorul** acestui cerc va genera un câștig  $G_S < G_{\text{cerc}}$
  - Orice punct **în interiorul** acestui cerc va genera un câștig  $G_S > G_{\text{cerc}}$

# Cercuri de castig constant la intrare

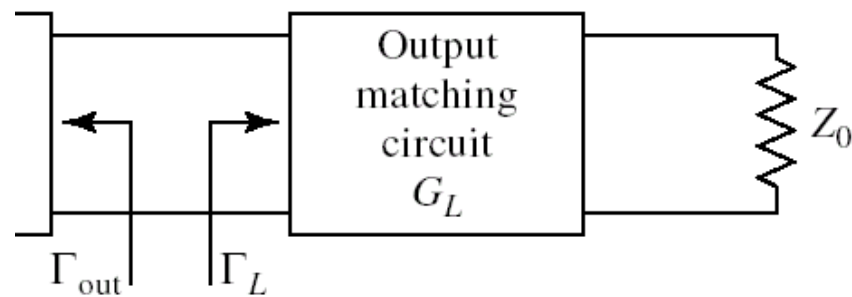
$$C_S = \frac{g_S \cdot S_{11}^*}{1 - (1 - g_S) \cdot |S_{11}|^2}$$

$$R_S = \frac{\sqrt{1 - g_S} \cdot (1 - |S_{11}|^2)}{1 - (1 - g_S) \cdot |S_{11}|^2}$$

- Centrele cercurilor se gasesc pe segmentul care uneste  $\Gamma_S = S_{11}^*$  cu centrul diagramei Smith
- Cercurile se traseaza (traditional, CAD) in **coordonate logaritmice** ([dB])
  - relatiile de calcul sunt in coordonate **liniare** !
- Cercul corespunzator lui  $G_S = 0$  dB trece prin origine



# Cercuri de castig constant la iesire



$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

■ Castig maxim  $\Gamma_L = S_{22}^* \Rightarrow G_{L\max} = \frac{1}{1 - |S_{22}|^2}$

$$g_L = \frac{G_L}{G_{L\max}} = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2} \cdot (1 - |S_{22}|^2) < 1$$

■ Calcul similar

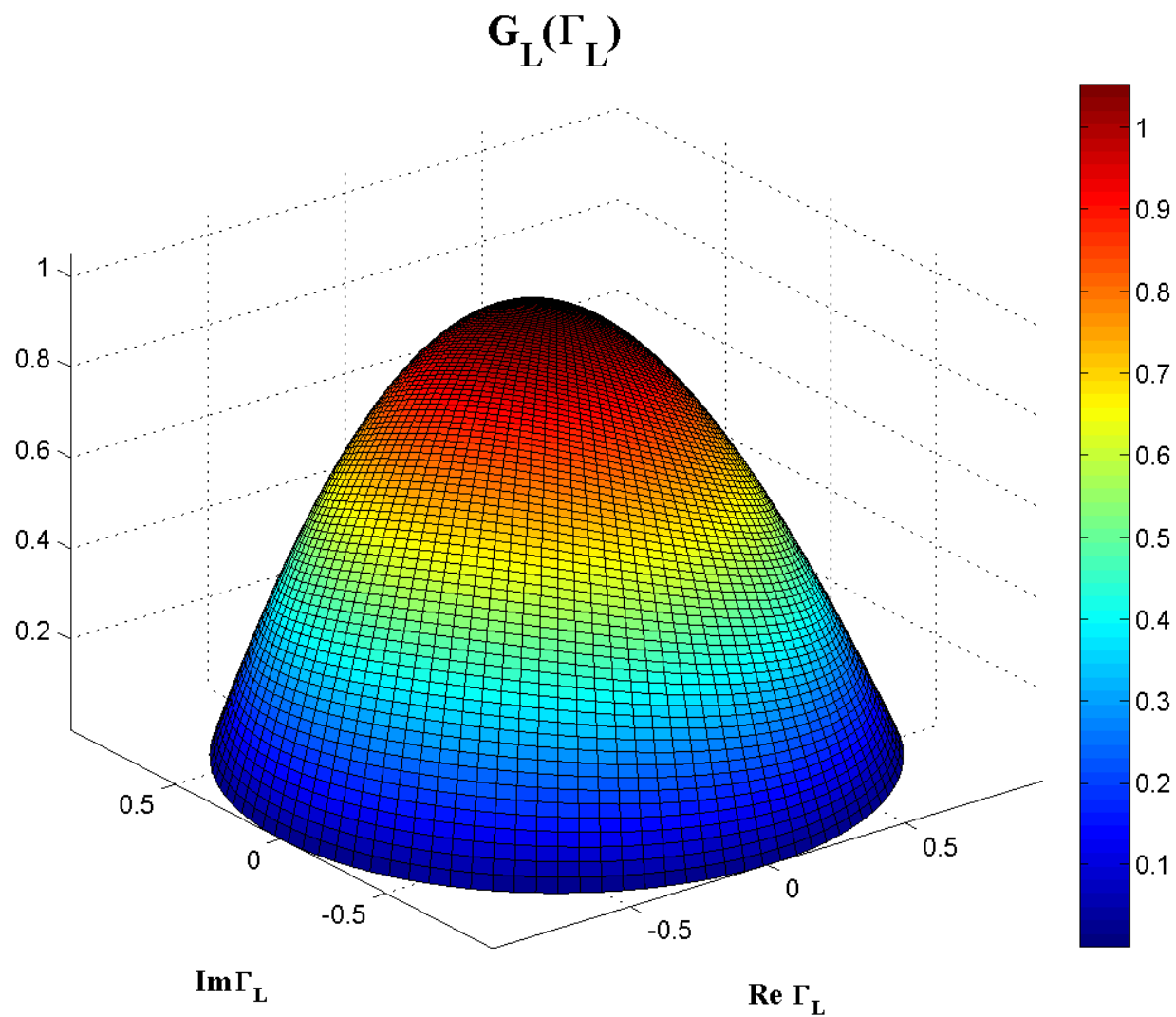
$$C_L = \frac{g_L \cdot S_{22}^*}{1 - (1 - g_L) \cdot |S_{22}|^2}$$

$$R_L = \frac{\sqrt{1 - g_L} \cdot (1 - |S_{22}|^2)}{1 - (1 - g_L) \cdot |S_{22}|^2}$$

■ Exemplu

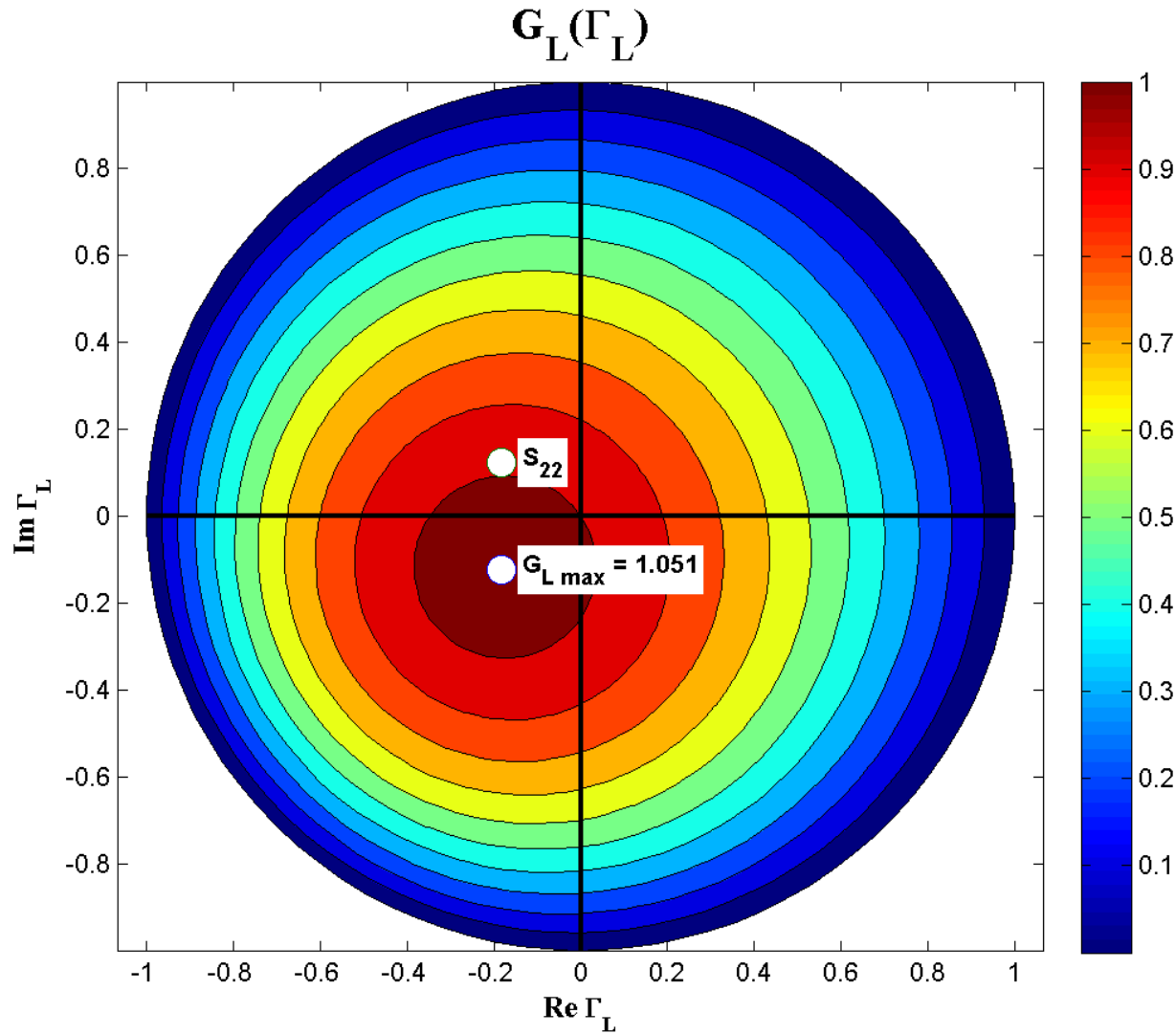
$$G_{L\max} = \frac{1}{1 - |S_{22}|^2} = 1.051 = 0.215 \text{ dB}$$

# $G_L(\Gamma_L)$



$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

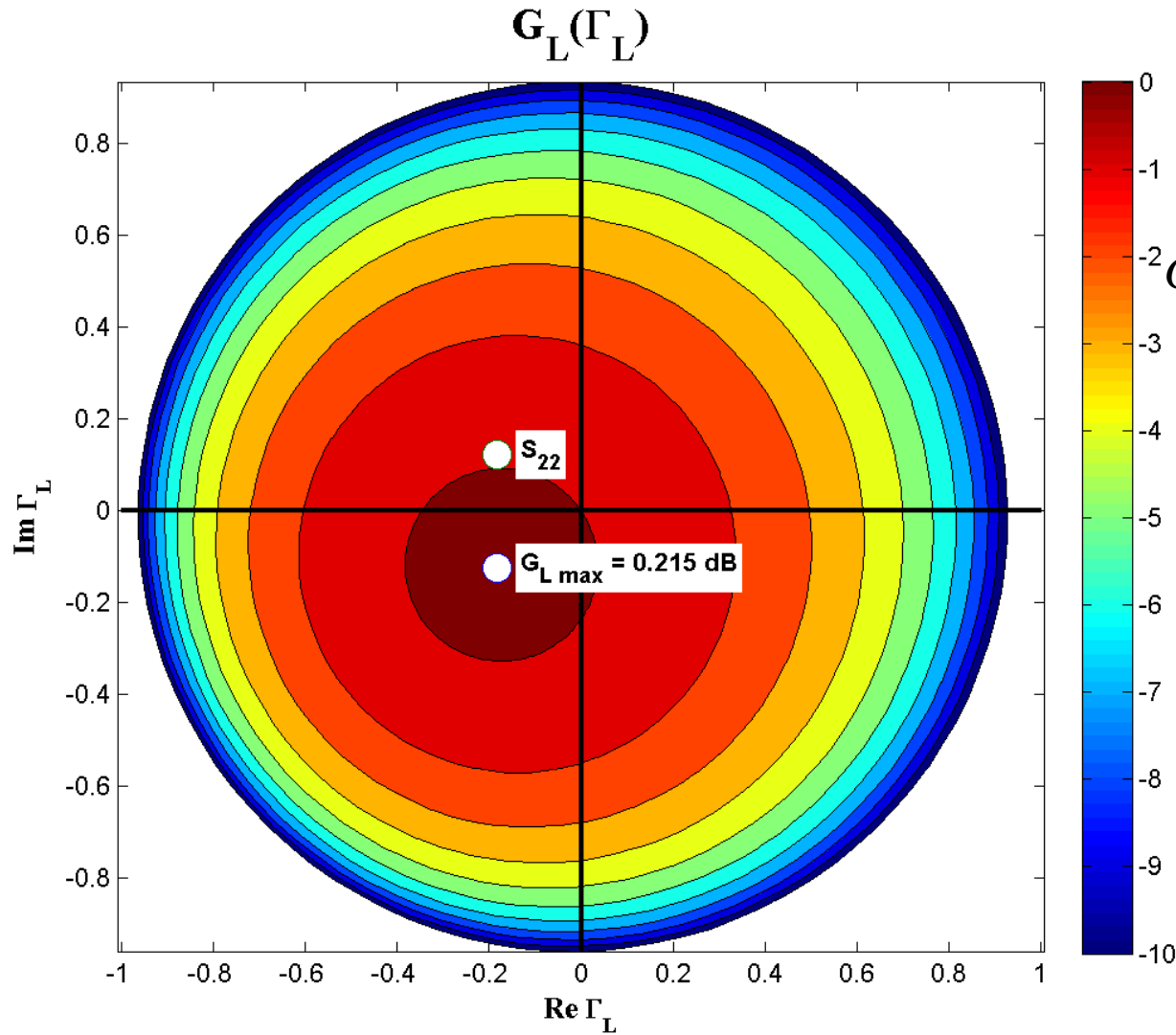
# $G_L(\Gamma_L)$ , diagrama de nível



$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

$$G_{L \max} = G_L \big|_{\Gamma_L = S_{22}^*}$$

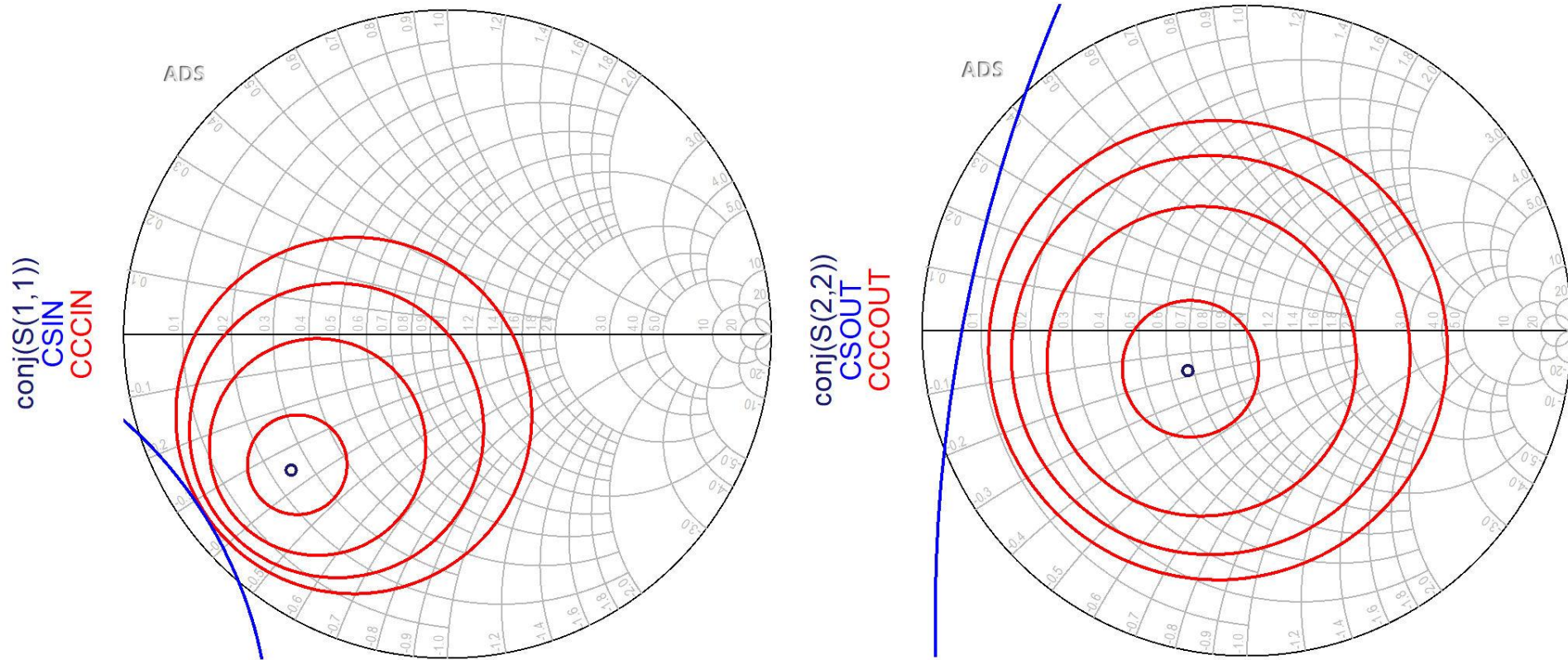
# $G_L[\text{dB}](\Gamma_L)$ , diagrama de nivel



$$G_L[\text{dB}] = 10 \cdot \log \left( \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2} \right)$$

$$G_{L \max} = G_L|_{\Gamma_L = S_{22}^*}$$

# ADS



- Cercurile se reprezinta pentru valorile cerute in dB
- Este utila calcularea  $G_{S_{\max}}$  si  $G_{L_{\max}}$  anterior

# Proiectare pentru castig impus

- Se calculeaza  $G_o$ ,  $G_{S_{\max}}$ ,  $G_{L_{\max}}$
- Pentru obtinerea castigului impus se **aleg** valorile suplimentare necesare (suplimentar la  $G_o$ )
  - se tine cont de abaterea caracterizata de factorul de merit U

$$G_{dorit}[dB] = G_{S\_dor}[dB] + G_o[dB] + G_{L\_dor}[dB]$$

- Se reprezinta cercurile de castig pentru valorile alese  $G_{S\_dor}$ ,  $G_{L\_dor}$
- Se proiecteaza retelele de adaptare care muta coeficientul de reflexie **pe** sau **in interiorul** cercurilor dorite (in functie de aplicatie)

# Contact

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